A Modified Energy Detection Algorithm for S-band Electronic Surveillance

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Abstract: Spectrum sensing techniques have gained much attention due to their capabilities to improve the utilization of the spectrum and lay the foundation of cognitive radio. In this paper, a new kind of modified energy detection algorithm is proposed for the application on S-band uplink electronic surveillance. In this scheme, first, the uplink signal of Unified S-band Telemetry Tracking and Control is derived from Matlab simulation which is a multi-modulation signal of PCM-BPSK-PM. Then, a new kind of modified method is proposed based on the study of classical energy detection algorithm which makes use of ratio threshold and the coefficient of kurtosis. Simulation shows that the proposed method offers better performances than classical energy detection method to a certain extent. At last, some filters are used to confirm the central frequency of the uplink signal which is unified S-band telemetry tracking and control signal. The simulation results show that the proposed method is able to offer low estimation errors.

Key words: S-band uplink, energy detection, central frequency, kurtosis

INTRODUCTION

Cognitive Radio (CR) was proposed by Doctor Joseph Mitola III in his PhD. dissertation in 1999 (Mitola III et al., 2012). CR techniques have gained much attention due to their capability to reuse the spectrum and to solve the spectrum congestion nowadays. CR is often considered as the key to next generation communication system (Mao and Wolf, 2010; Liang et al., 2010). In classical spectrum management mechanism, most of the spectrum bands are exclusively allocated to a few particular customers which results in the exhaustion of limited frequency resource as wireless applications grow. However, in contrast to spectrum scarcity, many results show that spectrum utilization is often very low (Zhao and Swami, 2007). For example, in the U.S., only 2% of the spectrum is used at any given time and location (Chen et al., 2011). One feasible solution to solve the spectrum scarcity is opportunistic spectrum access which needs the help of spectrum sensing technique. Generally speaking, there are largely three categories of methods: energy detection, matched filter and cyclo-stationary feature detection (Ozdemir et al., 2008; Maleki and Leus, 2013; Appadwedula et al., 2008; Wang et al., 2011). Among them, the first one, energy detection, doesn’t need any priori information, resulting in low complexity. It can be affected by noise uncertainties easily, so the detection probability can’t meet our requirements in low SNR (the ratio of signal to noise).

Most of the previous work on energy detection focused on setting absolute threshold. However, in this paper, a new method is presented to make it work well under low SNR. As coefficient of kurtosis is adopted, the new method differed from previous work in threshold setting. First, this study analyses the classical energy detection algorithm and proposes a modified method, where “Ratio threshold” is adopted. Simulations are run by using a multi-modulation signal of PCM-BPSK-PM which is used in S-band uplink. Secondly, this paper compares the two methods, classical algorithm and modified algorithm. The results prove the feasibility of the modified algorithm. At last, we use “adding windows” method to estimate the central frequency of the carrier signal. The overall structure diagram is showed as follows. Figure 1 shows that: after receiving the signal of S-band uplink, we should carry out spectrum sensing by using energy detection algorithm. If there is no one using S-band, go on searching. If we find S-band uplink is used by someone, we will use “adding windows” method to estimate the carrier frequency.

SYSTEM MODEL

The input signal: In fact, S-band uplink monitoring and control signal (2025-2110 MHz) is modulated in PCM-PSK-PM or PCM-PSK-FM form. In this paper, we use the former form: PCM-PSK-PM.
Fig. 1: Overall structure diagram of S-band uplink electronic surveillance

The signal modulated by BPSK can be written as car = carr.cos (2πf_s t), where carr is the baseband code sequence, f_s is subcarrier; the whole signal is:

\[ x(t) = \cos(2\pi f_s t + m_c \text{car}) \]

where, \( f_s \) is carrier, \( m_c \) is phase modulation ratio.

**The classical algorithm:** The situation of interest is shown in Fig. 2. The energy detector consists of a square law device followed by finite time integrator. The output of the integrator at any time is the energy of the input to the squaring device over the interval T in the past (Hao and Zu, 2009). The pre-filter serves to limit the noise bandwidth; the noise at the input to the squaring device has a band-limited, flat spectral density.

The detection is a test of the following two hypotheses. (a) \( H_0 \): The input \( y(t) \) is noise alone: \( y(t) = n(t) \); (b) \( H_1 \): The input \( y(t) \) is signal plus noise: \( y(t) = n(t) + s(t) \). The output of the integrator is denoted by \( V \) which will be compared with \( V_r \). If \( V > V_r \), it represents that there exists primary users (that is \( H_1 \)); or \( V < V_r \) it represents that there doesn’t exist any primary users (that is \( H_0 \)).

According to the sampling theorem, the noise and signal process can be expressed as (Dottie and Kohno, 2011):

\[ n_0 = \sum_{k=1}^{N} a_k \text{sinc}(2\pi f_s t - k), 0 < t < T, a_k = n_k(i/2W) \quad (1) \]

\[ s(t) = \sum_{k=1}^{N} a_k \text{sinc}(2\pi f_s t - k), 0 < t < T, a_k = s_k(i/2W) \quad (2) \]

\[ b_k = \frac{a_k}{\sqrt{2WN_0}} \quad (3) \]

\[ \beta_k = \frac{b_k}{\sqrt{2WN_r}} \quad (4) \]

- When there is no signal, that is \( H_0 \), \( y(t) = n(t) \):

\[ V = \int_0^T y^2(t)dt / N_m = \sum_{k=1}^{N} \frac{a_k^2}{(2WN_0)} = \sum_{k=1}^{N} b_k^2 \quad (5) \]

So \( V \) can be viewed as the sum of the squares of 2TW standard Gaussian variables with zero mean and unit variance. Therefore, \( V \) follows a central Chi-square distribution with 2TW degrees of freedom.

- When there exists signal, that is \( H_1 \), \( y(t) = n(t) + s(t) \):

\[ y(t) = \sum_{k=1}^{N} (a_k + s_k) \text{sinc}(2\pi f_s t - k) \quad (6) \]
\[
\int_0^T y^2(t) dt = \frac{TW}{\lambda} \sum_n (b_n + v_n)^2 
\]

Then:
\[
V = \int_0^T y^2(t) dt / N_0 = \frac{TW}{\lambda} \sum_n (b_n + v_n)^2
\]

Where:
\[
1 = \sum b_n^2 = \int_0^T s^2(t) dt / N_0 = E_s / N_0
\]

So the decision statistic \( V \) in this case will have a non-central \( \chi^2 \) distribution with \( 2TW \) degrees of freedom and a non centrality parameter \( \lambda \). Following the shorthand notations mentioned in the beginning of this section, we can describe the decision statistic as:
\[
V = \frac{\chi^2_{2TW}}{\chi^2_{2TW}(\lambda)}, H_0
\]
\[
\frac{\chi^2_{2TW}(\lambda)}{\chi^2_{2TW}}, H_1
\]

The detection probability \( Q_t \) and false probability \( Q_f \) can be written as follows:
\[
Q_t = \text{Prob}(V > V_t | H_0) = \text{Prob}(x^2_{2TW} > V_t)
\]
\[
Q_f = \text{Prob}(V > V_t | H_1) = \text{Prob}(x^2_{2TW} > V_t)
\]

where, \( s(t) \) is signal waveform, \( n(t) \) is noise waveform, \( T \) is observation time interval, \( W \) is bandwidth, \( \lambda \) is the ratio of signal to noise, \( N_0 \) is two-side noise power density spectrum and \( V_t \) is the threshold.

The modified algorithm: Most of the articles about energy detection concentrate on the process of noise and dual-threshold (Kalamkar and Banerjee, 2013; Song et al., 2010; Wu et al., 2009) while few pay attention to the main algorithm. Due to the disadvantage of the classical energy detection algorithm, in this study the squaring device and the threshold setting in frequency domain are modified as follows. Figure 3 shows classical frequency-domain energy detection algorithm and Fig. 4 shows modified frequency-domain energy detection algorithm which is proposed in this study.

As is known that the amplitude of the received signal represents the size of the margin of the received signal, the sum of the square represents the energy of the received signal and the coefficient of kurtosis (the fourth order) reflects the concentration and dispersion of random variables (the degree of tip level). Here coefficient of kurtosis is adopted to describe the degree of centralization and decentralization of signal. As a result, it is easy to find out the maximum of the signal spectrum in frequency domain (Zhao and Swami, 2007; Zhao et al., 2010). When noise is only input:
\[
N(w) = \sum_{i=1}^{2W} \bar{n}_i \phi\left(\frac{w}{2W}\right) \exp(-j\omega w)\]
\[
- \bar{\phi}\left(\frac{w}{2W}\right) \sum_{i=1}^{2W} \bar{n}_i \exp(-j\omega w)
\]

where, \( \phi(x) = \text{sinc}(x) \), \( \bar{\phi}(w) \) is the Fourier transform of \( \phi(x) \) and \( j^2 = -1 \). Then the amplitude of noise can be described as:
\[
|N(w)|^2 = \phi\left(\frac{w}{2W}\right)^2 \sum_{i=1}^{2W} |\bar{n}_i|^2
\]

Fig. 3: Classical frequency-domain energy detection

Fig. 4: Modified frequency-domain energy detection
The same approach is applied when the signal $s(t)$ is present, then:

$$ S(w) = \sum_{-\frac{W}{2}}^{\frac{W}{2}} e^{-j\omega t} \sum_{i} a_i \exp(-j\omega) $$

$$ |S(w)|^2 = |\sum_{-\frac{W}{2}}^{\frac{W}{2}} a_i|^2 $$

$$ \lambda = \frac{\sum |S(w)|^2}{\sum |N(w)|^2} = \frac{S_o(w)}{N_o(w)} = \frac{\sum a_i^2 B_s}{\sum a_i^2 B_n} = \frac{\sum a_i^2 \varepsilon}{\sum a_i^2 \varepsilon} $$

$$ \Rightarrow \frac{S_o(w)}{N_o(w)} = \frac{\lambda}{\varepsilon} $$

where, $\lambda$ is signal to noise ratio, $S_o(w)$ and $N_o(w)$ is separately the equivalent value of $S(w)$ and $N(w)$, $B_s$ and $B_n$ is the bandwidth of signal and noise separately and $B_s = \varepsilon B_n$ that is to say $0 \leq \varepsilon \leq 1$.

We denote Th.1 and Th.2 as:

$$ \text{Th.1} = \frac{|S(w)|^2}{|N(w)|^2} = \frac{\lambda}{\varepsilon} \quad \text{and} \quad \text{Th.2} = \frac{|S(w)|^2}{|N(w)|^2} = \left(\frac{\lambda}{\varepsilon}\right)^2 $$

When Th.1 > 1, that is to say $\lambda > \varepsilon$, Th.2 > Th.1. It means that the kurtosis algorithm can make the signal notable among the noise and it's also confirmed by the following simulation results. In fact, the signal is a kind of narrowband signal. If we set $\frac{\lambda}{\varepsilon}$ as the classical signal to noise ratio, $\left(\frac{\lambda}{\varepsilon}\right)^2$ is the modified signal to ratio, then the improvement in SNR(dB) is:

$$ \Delta \text{SNR} = 10 \log \left(\frac{\lambda^2}{\varepsilon^2} - 10 \log \left(\frac{\lambda}{\varepsilon}\right)^2 - 10 \log (\lambda) - 10 \log (\varepsilon)\right) $$

Figure 5 shows the spectrum of ideal signal, where there is no noise. Figure 6 shows the spectrum of signal which noise is added into. From Fig. 5 and 6, we can see that the useful signal is drowned in the noise. Figure 7 shows the modified signal spectrum, where the fourth order of signal is used. Compared with Fig. 6, we can see that the useful signal is more obvious from the background noise in Fig. 7. The result is the same as Eq. 17: using the fourth order instead of square can make the useful signal more obvious from the background noise.

In classical energy detection algorithm, the threshold is a single-value or dual, so when background noise changes, the threshold has to be changed. However a ratio threshold is developed in this paper which can void the influence of the noise changes.

- First, input noise only and FFT it, then calculate the fourth order
Secondly, the spectrum is divided into fixed bandwidth groups and sum each group, denoted by $S_k$.

Thirdly, find the maximum value among $S_k$ and denoted by $S_{\text{max}}$, then the rest of $S_k$ denoted by $S_l$.

Fourthly, take the average of $S_{\text{max}}$ and $S_l$ separately and then defined $R$ as both the ratio of $S_{\text{max}}$ and $S_l$.

Fifthly, carry out the Monte Carlo simulation 10,000 times.

Finally, after sorting the results, we can obtain correspondence between the threshold and the probability of false alarm.

From Fig. 8, when there is noise only, $R$ is very low, while when there exist signal and noise together, $R$ will become obviously higher than before which means that mean of signal only and mean of signal with noise can be easily separated from each other. It is obvious that when the SNR is too low, the modified algorithm does not work, too. It can be explained in “SNR Wall” theories. Somebody may say why you don’t use the eighth order. In fact, if we use the fourth order to simulate, we need to simulate about $3N$ more multiplication than classical algorithm; if we use the eighth order, we have to simulate about $7N$ more multiplication than algorithm ($N$ is the number of FFT). The larger $N$ is, the more complex the eighth order is and the more time it will cost, at the same time it can’t improve the algorithm forever because of the “SNR Wall” theory (Marian et al., 2011; Ji and Zhu, 2010). Taking these factors into account, kurtosis is used to modify the algorithm.

In fact, $R$ in Fig. 8 is just the ratio threshold in our algorithm. The ratio threshold should be between 2 and 10 and the simulation result is showed below. In Table 1, SNR is the ratio of signal and noise and $R$ denotes the threshold. When the threshold $R$ is too low, for example $R = 3$, the false alarm probability $P_f$ is higher than 90%. And $P_f$ becomes lower as $R$ becomes higher. It’s obvious to see that when ratio threshold is 9 or 10, the false alarm probability can be lower than 5%. If the threshold is higher, the missed alarm probability will be higher, too, so we choose threshold = 9 or 10.

"Adding windows" way to estimate the carrier frequency:
Besides all the things mentioned above, this paper also proposes an “adding windows” way to estimate the central frequency.

Butterworth filter has monotonic and smooth frequency characteristics, but under the same transition bandwidth conditions, the higher the required filter order results in the higher corresponding costs; Chebyshev filter has ripples in pass-band or resistance, but under the same pass-band conditions, the required filter order is lower. Although the type I Chebyshev analog prototype filter has a narrower, steeper transition zone, this feature is at the expense of the smooth monotonic pass-band characteristics (and results in ripples). So we choose type II Chebyshev filter.

For type I Chebyshev filters and type II Chebyshev filters, the gain (or amplitude) response as a function of angular frequency $\omega$ of the $n$th-order low-pass filter is given by:

$$G_n(\omega) = \frac{1}{1 + e^{-T_0(\omega)/\omega_0}}$$

(18)

$$G_n(\omega, \omega_s) = \frac{1}{1 + e^{-T_0(\omega/\omega_s)}}$$

(19)

Fig. 8: Correlation between threshold $R$ and SNR

Table 1: Under different thresholds $R$, correlation between false alarm probability and SNR

<table>
<thead>
<tr>
<th>SNR (dB)</th>
<th>-20 dB</th>
<th>-18 dB</th>
<th>-16 dB</th>
<th>-14 dB</th>
<th>-12 dB</th>
<th>-10 dB</th>
<th>-8 dB</th>
<th>-6 dB</th>
<th>-4 dB</th>
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<td>5</td>
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<td>6</td>
<td>0.20</td>
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where, \( r \) is the ripple factor, \( \omega_c \) is the cutoff frequency and \( T_n(x) \) is Chebyshev polynomial of the nth order with variable \( x \).

Make the input signal pass through a few groups of "window" filters and each group has a different center frequency. Find out which group’s output energy is the maximum, then divide this group’s bandwidth again into new groups and go on as the first step. At last, we use the last filter’s center frequency to estimate the input signal’s center frequency.

**SIMULATION AND ANALYSIS**

**Input PCM-PSK-PM signal:** Generally speaking, paper will set the signal modulated by BSK, FM or any other. After all, they just pay attention to the algorithm itself and have no background of application. In this paper, we use the system to simulate S-band uplink electronic surveillance. Depending on the particular background of application in this study, the signal of this paper is multi-modulated by PCM-PSK-PM and the variables are set as follows: the baseband code rate is 200 kHz, the subcarrier is 2 MHZ, the main carrier is 2070MHZ, \( m \) is 1.5 and sampling frequency is 184MHZ.

Figure 9 shows the PCM-PSK-PM signal in frequency domain which is used for simulation later. After undersampling by 184 MHZ, carrier frequency of signal can be moved to 46 MHZ which can be got as Eq. 20:

\[
2070-184\times11 = 46 \text{ MHZ}
\]  

**Detection performance of the modified algorithm:** Above in Table 2 and 3, respectively, when threshold = 9 and threshold = 10, the false alarm probability \( P_f \) and undetected probability \( P_m \) and the error probability \( P_e \) (the sum of \( P_f \) and \( P_m \)) are measured. According to Table 2 and 3, we can find that, when threshold = 9, the error probability \( P_e \) can be about 5% at -10dB, while the \( P_e \) is only 0.074 when threshold = 10. However if SNR become higher than -8dB, the performance under threshold = 10 is better than the performance under threshold = 9. It’s easy to understand that the higher threshold is, the lower the \( P_e \) is. In this study, we want to make the system work well as low SNR as possible, at the same time \( P_e \) is lower than 5%. So we here take threshold = 9.

Figure 10 shows that the detection probability \( P_i \) changes with the SNR in the classical and modified energy detection algorithm. It’s obvious that when SNR = 4 dB, the classical detection probability can reach 95%; however the modified algorithm shows that when even SNR = -10 dB, the detection probability can reach 95% and meanwhile the error probability is less than 5%.

![Fig. 9: PCM-PSK-PM signal in frequency domain](image)

95% and meanwhile the error probability is less than 5%. So the improved algorithm is at least 10 dB better than the classical energy detection algorithm. In theory, according to Eq. 14, \( r \) is about 0.25, so the improvement is about 10log(r) = 14 dB. The two results coincide. In this study Song et al. (2010) which uses two thresholds for energy detection, the detection probability can reach about 95% at SNR = -7dB which is not better than the result of this study. The algorithm just needs one threshold. Since the variability only needs to compare with threshold just once, it will be faster than two thresholds algorithm and it will not leave signal into area of uncertainty as two
thresholds algorithm. Meanwhile, most previously published studies just pay attention to false alarm probability $P_f$ without considering undetected probability $P_a$. In fact, we should take total error probability $P_e$ in account which is the sum of $P_f$ and $P_a$, which is used in this study.

**Estimate the center frequency of the carrier signal:** We use an “adding windows” way to confirm carrier frequency which consists of a set of filters. Figure 11 shows the frequency range of six filters in digital domain. In Fig. 11a shows an all-pass filter in digital domain (b)-(f) show filters of different frequency in digital domain. It can be considered that filter (a) is separated into filters (b)-(f). In simulation of this study, we find that signal that passes through filter (d) has the maximum of energy. It is clear that the carrier frequency is in the range of this filter. Then filter (d) is separated into new filters just as what is done to filter (a) above. At last, we can get the carrier frequency by the last filter’s center frequency. In Fig. 12a shows the
Fig. 12(a-b): Estimation of carrier frequency, (a) Carrier frequency in digital domain and (b) Carrier frequency in frequency domain

last filter’s center frequency in digital domain and (b) shows the same result in frequency domain. From (b) of Fig. 12, we can see that the estimate of carrier frequency is 2070. 0275 MHz which is obtained by the inverse of Eq. 14 and the error of estimation is only 0.0275 MHz.

CONCLUSION

The main contribution of this study is that energy detection algorithm in cognitive radio spectrum sensing technology has been improved and an "adding windows" way is proposed to confirm the signal’s center frequency. After simulation on the S-band monitoring and control signal, we come up with the conclusion that the improved energy detection method can effectively overcome the shortcomings of the classical energy detection method which is sensitive to background noise. The measuring results show that the improved algorithm is at least 10 dB better than the classical energy detection algorithm and the error of carrier frequency estimation is only 0.0275 MHz.

REFERENCES


