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## Mechanized Verification of Security Properties of Transport Layer Security 1.2 Protocol with Crypto Verif in Computational Model

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**Abstract:** In modern society, many transactions have been processed through web-based applications. In order to protect those critical applications against attacks, Transport Layer Security (TLS) protocol has been implemented and widely deployed. The related literatures show that security analysis of TLS 1.2 protocol where cipher suite is RSA encryption has not been implemented with mechanized tool in computational model. Hence in this study, Blanchet calculus is used to analyze TLS 1.2 protocol where cipher suite is RSA encryption with mechanized tool crypto verif in computational model. The term, process and correspondence are used to model authentication in TLS 1.2 protocol where cipher suite is RSA encryption. The result shows that TLS 1.2 protocol where Cipher suite is RSA encryption has the pre master key confidentiality and authentication from server to client. The first mechanized analysis on TLS 1.2 protocol where Cipher suite is RSA encryption is implemented in computational model with active adversary in this study.

**Key words:** Verification, confidentiality, authentication, correspondence, protocol security

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### INTRODUCTION

With the rapid development of network technology and Web technology, Internet has a strong influence on all kinds of aspects in society. Many transactions have been processed through web-based applications. In order to protect the web-based applications against passive and active attacks, TLS protocol (<http://tools.ietf.org/html/rfc5246>) is widely deployed. The latest version is TLS 1.2. The objective of TLS 1.2 protocol is to provide confidentiality and authentication between two communicating parts. So, people have paid a close attention to analysis and verification of its security properties and want to get more confidence on it.

For the sake of analyzing and proving the security properties of security protocols and strengthening the confidence of the people, two approaches have been proposed from the beginning of the 1980s (Meng, 2011). One is symbolic model which is also called Dolev-Yao model and in which cryptographic primitives are abstracted as perfect black boxes. Until now lots of mechanized tools in this model have been developed, for example, Casper, Isabelle, ProVerif and Scyther. In 2005 Ogata and Futatsugi (2005) formally analyzed in symbolic model TLS protocol with CafeOBJ method based on equational reasoning. But the results of proof based on symbolic model are not quite clear.

The other approach is computational model based on complexity and probability. The attacker in computational model is modeled as a probabilistic polynomial-time machine. The computation model is more realistic but it is difficult to mechanized proof until the introduction of mechanized tool Crypto verif (Blanchet, 2008) which is the first mechanized tool with computational model. In 2012, (Jager *et al.*, 2012) firstly analyzed by hand TLS protocol where Cipher suite is ephemeral Diffie-Hellman key exchange protocol in standard model. In 2013, (Fournet *et al.*, 2013) used F7 refinement typechecker to verify security properties of TLS protocol implementation.

According to the related references, analysis of security of TLS 1.2 protocol where Cipher Suite is RSA encryption with mechanized tool in computational model is not found.

Owing to the previous analysis of TLS 1.2 protocol is not quite clear, in this study, Blanchet calculus is used to analyze TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool Crypto verif.

### CONTRIBUTION AND OVERVIEW

During the past several years TLS protocol has been implemented and widely deployed in many web-based applications. For the sake of verifying the security properties of security protocols and improving the

confidence on its security, symbolic model and computational model have been developed. Symbolic model is also called Dolev-Yao model; computational model is based on complexity and probability. The later model is more realistic owing to that the attacker is modeled as a probabilistic polynomial-time machine. According to the related references, until now it is not existence that security analysis of TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool in computational model.

So analysis of security properties of TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool in computational model plays an important role in security protocol field and is a significant work. Hence in this study, Blanchet calculus is used to analyze TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool.

The main contributions of this study are summarized as follows:

- The status of analysis in TLS1.2 protocol including in symbolic model and in computational model is presented. Until now it is not existence that analysis security of TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool in computational model
- Applying Blanchet calculus in computational model with active adversary for mechanized verification of TLS 1.2 protocol where Cipher suite is RSA encryption. Authentication is expressed by non-injective or injective correspondence. Figure 1 shows the model of mechanized verification of TLS 1.2 protocol where Cipher suite is RSA encryption
- The result shows that TLS 1.2 protocol where cipher suite is RSA encryption has confidentiality of

pre master key and authentication from server to client. The first mechanized verification on TLS 1.2 protocol where cipher suite is RSA encryption in computational model of in active adversary is implemented in this study

### RELATED WORK

In this part the status quo of the proof in TLS protocol and its implementation based on symbolic model and on computational model is presented. Until now there does not exist that analysis of TLS 1.2 protocol with mechanized tool in computational model.

In 1996, Wagner and Schneier (1996) analyzed Secure Sockets Layer (SSL) 3.0 which is the former version of TLS protocol with informal method. They found some active attacks which mainly include change cipher spec-dropping, Key exchange algorithm spoofing and version roll-back attack.

In symbolic model (Paulson, 1999) uses Isabelle to automatically analyze TLS protocol and proves its security claimed in TLS specification; in 2005 (Ogata and Futatsugi, 2005) formally analyzed TLS protocol with CafeOBJ method based on equational reasoning. The results are that TLS protocol has the security properties with the condition pre-master secrets cannot be leaked.

In computational model (Jonsson and Kaliski, 2002) present an analysis of a variant of TLS hand shake protocol where Cipher suite is RSA by hand. They argue that TLS should use Tagged Key-Encapsulation Mechanism (TKEM) 1 rather than TKEM2; In 2008, (Morrissey *et al.*, 2008) analyzed TLS hand shake protocol in random model by hand. They firstly proposed a security model for key agreement protocol and then analyzed TLS hand shake protocol with the condition that Message Authentication Code (MAC) value is send in

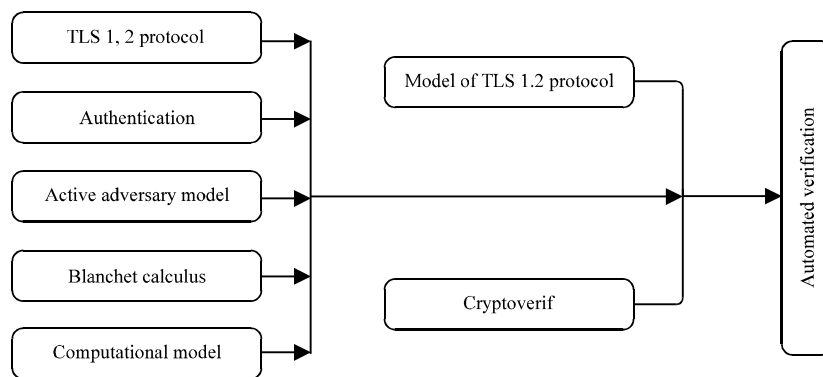


Fig. 1: Model of mechanized verification of TLS 1.2 protocol where Cipher suite is RSA encryption

the plaintext and showed that TLS key agreement protocol is secure. However the version of TLS protocol with Diffie-Hellman Key Exchange is not analyzed; In 2011 (Paterson *et al.*, 2011) presented the scheme of length-hiding authenticated encryption to analyze security of TLS Record Protocol by hand. They found a new distinguishing attack against TLS where variable length padding and short MACs are used; in 2012 Jager *et al.* (2012) firstly analyzed by hand TLS protocol where Cipher suite is ephemeral Diffie-Hellman key exchange in the standard model. They introduced the authenticated and confidential channel establishment security model and showed that the combination of the TLS hand shake protocol with the TLS Record Layer can be proven secure.

Here the aspect of security properties of implementation of TLS protocol is discussed. In 2009 Chaki and Datta (2009) presented the first framework to automatically analyze authentication and secrecy of the hand shake in Open SSL. In 2012, (Bhargavan *et al.*, 2012) firstly implemented TLS protocol 1.0 with language F#. And then they designed a model extraction method to extract the abstract model. Finally, they used Crypto verif to analyze security properties of TLS implementation in F#. In 2013 (Fournet *et al.*, 2013) developed a new, verified, reference implementation of TLS protocol 1.2 with functional language F#. And then they used the F7 refinement type checker to verify its security properties and find a few new attacks.

**REVIEW OF BLANCHET CALCULUS  
AND MECHANIZED PROOF  
TOOL CRYPTO VERIF**

In this section there is a brief overview of Blanchet calculus (Blanchet, 2008) and the mechanized prover Crypto verif, formalize TLS 1.2 protocol using it (<http://www.Crypto.verif.ens.fr>). Blanchet calculus is a probabilistic polynomial calculus and has been developed for the automated proof security protocols. In this calculus, messages are bitstrings and cryptographic primitives are functions operating on bitstrings. Blanchet calculus includes terms and processes.

The mechanized prover Crypto verif can directly prove security properties of cryptographic protocols in the computational model in which the cryptographic primitives are functions on bit-strings and the adversary is a polynomial-time Turing machine. It also can prove secrecy properties and events that can be executed only with negligible probability.

Crypto verif can works in two modes: A fully automatic and an interactive mode. The interactive mode, requires a Crypto verif user to provide commands that indicate the main game transformations. Crypto verif is sound about the security properties it shows in a proof but properties it cannot prove are not necessarily invalid.

**REVIEW OF TLS 1.2 HAND SHAKE PROTOCOL**

TLS 1.2 protocol mainly consists of hand shake protocol and Record protocol which play a very important role in TLS protocol. TLS Record Protocol is a layered protocol and accepts messages from higher level layer to be transmitted and partitions the data into blocks and transmits the result. Received data is processed inversely and then delivered to higher level clients. TLS 1.2 hand shake Protocol is one of the defined higher-level clients of TLS 1.2 Record protocol and is used to establish a secure session between server and client. In other words TLS 1.2 hand shake protocol can provide the authentication from server to client and confidentiality of pre master key. Figure 2 describes the messages exchanged between server and client in the simplification of TLS 1.2 hand shake protocol.

In TLS 1.2 hand shake protocol there are two communicating parties involved. One is client, the other is server. Client and server use TLS 1.2 hand shake protocol to share a common key and server use TLS 1.2 hand shake protocol to authenticate identity of client. The simplification of TLS 1.2 hand shake protocol contains seven messages which are client hello, Server hello, Server certificate, Server hello done, client key exchange, Client finished and Server finished:

Client Hello: = client\_version  
 ||client\_random||session\_id||  
 cipher\_suites||compression\_methods||extensions (1)

When a client wants to connect to a server, TLS 1.2 hand shake protocol requires client to send the Client hello message. Client hello mainly includes client\_version, client\_random, session\_id, cipher\_suites, compression\_methods and extensions. Client\_version parameter describes the version of the TLS protocol through which the client wants to communicate with server during this session. Client\_random parameter describes the structure generated by client who is used to prevent against replay attacks and to compute the master key. Session\_id parameter is an important parameter in client hello message. It describes the Identity (ID) of a

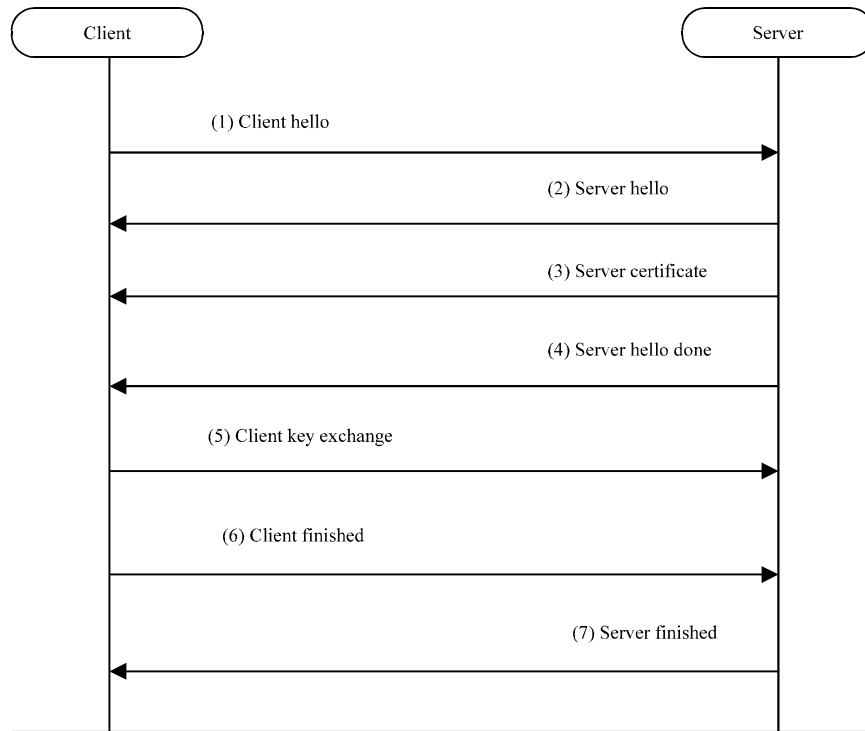


Fig. 2: TLS 1.2 hand shake protocol

session that the client wants to use for this connection. Cipher\_suites parameter describes that a list of the cryptographic options supported by the client. Compression\_methods parameter describes the compression methods supported by the client. Extensions parameter describes some extended functions need to be supported by server. The client generates Client hello message and sends it to server:

Server hello: =c server\_version  
 ||server\_random||session\_id||  
 cipher\_suites||compression\_methods||extensions (2)

When the server receives the Client hello message, it then constructs the Server hello message. Server hello message mainly includes server\_version, server\_random, session\_id, cipher\_suites, compression\_methods and extensions. Server generates message Server hello according to the message Client hello. Server\_version parameter is generated with the condition that the lower of that required by the client in client\_version in message Client hello and the highest supported by the server. Server\_random parameter describes the structure generated by server which is used to prevent against replay attacks and to calculate the master key. Session\_id parameter describes that the server finds the session id

from the cache according to the session id from the Session\_id in message Client hello. Cipher\_suites parameter is from the cipher\_suites in Client hello message. Here the value of Cipher\_suites is RSA public encryption. Compression\_methods parameter is from the compression\_methods in Client hello message. Extensions parameter is from the extensions in Client hello message. After the server constructs message server hello, it sends it to the client.

Server certificate: = version||serial number  
 ||algorithm identifier||issuer||utc time||  
 server\_subject\_name  
 ||server\_subject\_key\_info||signature (3)

After the server sends the message server hello to the client, he constructs the message Server certificate to the client. The message Server certificate is used to tell the public key of the server to the client. The message Server certificate mainly contains version, serial Number, algorithm identifier, issuer, utcTime, server\_subject\_name, server\_subject\_key\_info and signature. Here the server\_subject\_name and server\_subject\_key\_info parameters are mainly introduced. Server\_subject\_name parameter is the name of server which is the owner of certificate. Server\_subject\_key\_info parameter mainly

```

Expand IND_CCA2_public_key_enc (rsakeyseed, rsapkey, rsaskey, cleartext , message, seed, )
                                (rsaskgen, rsapkgen, enc,dec, injbot, Z, Penc, Pencoll )
Expand Collision_resistant_hashh (hashkey, hashinput, input , hash, phash)
Expand PRF_new (key seed, key, input, output, kgen, f, Pprf)
Define IND_CPA_sym_enc (key seed, key, cleartext, ciphertext, seed, kgen, enc,dec, injbot, Z, Penc)
Define PRF_new (key seed, key, input, output, kgen, f, Pprf)
Param N1, N2, N3.
Fun fkey, label, input: output
Fun kgen (key seed): key
Equiv N3 new r: keyseed, new label:label; N1 of (x: input): = f(kgen(r), label, x)
<=(N3 *Pprf (time+(N3-1)*(time(kgen)+N1 *time (f, maxlength(x), N1, maxlength(x))=>
N3 new r: keyseed; !N1 of (x:input): =
    Find[unique] j<=N1 such that defined(x[j],r2[j]) && otheruses(r2[j]) && x = x[j] then r2[j]
    Else new r2: output; r2

```

Fig. 3: Cryptographic assumptions

includes the public key of the server and the related information on the public key:

$$\text{Server hello done:} = \text{Server hello done} \quad (4)$$

After the server sends the message server certificate, he constructs the message server hello done and sends it to the client. The server hello done message is sent by the server to show that the end of the server hello and associated messages. After sending server hello done message, the server will wait for a client response:

$$\begin{aligned} \text{Client key exchange:} &= \text{Client key exchange} \\ \parallel \text{Encrypted pre master secret} & \end{aligned} \quad (5)$$

After it receives the server hello done message, client key exchange message is sent by the client. Client key exchange message is the key message in TLS 1.2 hand shake protocol which is used to tell the pre Master key to the client in a secure way. Client key exchange message mainly includes key exchange algorithm and encrypted pre master secret parameters. With this message, the pre master key confidentiality is implemented by transmission of the RSA-encrypted pre Master key used here. Key exchange algorithm parameter describes the key exchange algorithm. The value of key exchange algorithm is RSA. Encrypted pre Master secret parameter describes the structure of pre Master key confidentiality. Pre\_master\_secret is generated by the client and is used to generate the master secret:

$$\text{Client finish:} = \text{Client finish} \quad (6)$$

Client finished message is always sent immediately to the server when the verification of the key exchange and authentication processes were successful. The server must verify that the contents are correct. Once the client has sent client finished message and received and validated the Server finished message from the server, the client may begin to send and receive application data over the connection:

$$\text{Server finished:} = \text{Server finished} \quad (7)$$

A Server finished message is always sent immediately to the client when the verification of the key exchange and authentication processes were successful. The client must verify that the contents are correct. Once the server has sent server finished message and received and validated the client finished message from the client, the server may begin to send and receive application data over the connection.

### FORMALIZING TLS 1.2 HAND SHAKE PROTOCOL IN BLANCHET CALCULUS

When TLS 1.2 hand shake protocol is formalized it assumes that public-key encryption is indistinguishability under adaptive chosen ciphertext attacks. Public key signature is unforgeable against chosen-message attack. Symmetric encryption is indistinguishability under chosen-plaintext attacks and probabilistic symmetric encryption. Hash function including hash functions defined by us according to the requirements is collision resistant and unforgeability against adaptive chosen messages attacks. Figure 3 describes the cryptographic assumptions in our analysis of TLS 1.2 hand shake protocol.

```

Event server (output).
Event client (output).
Query x:output; event server (x) ==> client (x)
Query x:output; inj:event server(x) ==> inj: client(x)
Query secret pre Master secret
    
```

Fig. 4: Query events and secret

```

Let TLS 1.2 process = initiator process (|(!n1client process)
|(!n2(server process)))
    
```

Fig. 5: TLS 1.2 hand shake protocol process

```

Let initiator process =
Start ();
New seed one: rsakey seed;
Let pkeyrsa: Rsapkey = rsapgen (seed one) in
Let skeyrsa: Raskkey = raskgen (seed one) in
New seed two: Keyseed;
Let signpkey: Pkey = pkgen (seed two) in
Let signskey: Skey = skgen (seed two) in
New keyhash:hash key;
c̄ pkeyrsa, signpkey, key hash
    
```

Fig. 6: Initiator process

Here non-injective correspondences and injective correspondences are used to model authentication from server to client. Firstly non-injective correspondences are used: Event server(x) =>inj: client(x) is used to authenticate client by server. Then injective correspondences are used: Event inj: event server(x) => inj: client(x) is used to authenticate client by server. Figure 4 describes the events and correspondence. Query secret pre master secret is used to query the secrecy of pre master secret.

The complete formal model of TLS 1.2 hand shake protocol where Cipher suite is RSA encryption in Blanchet calculus is given in Figure. Figure 5-8 reports the basic processes include initiator process, client process and server process in authentication and secrecy forming the model of TLS 1.2 protocol. The process TLS 1.2 process in Fig. 5 is assumed to run in interaction with an adversary which also models the network.

Initiator process generates server's public key pkeyrsa and private key signp key for encryption in RSA scheme and public key signs key and private key signs key, for digital signature in RSA cryptosystem. Finally, it sends signp key hash by the public channel c.

In detail initiator process in Fig. 6 firstly generates server's public key rsakey seed in the following procedure: Initiator process receives a null message on channel start, sent by the adversary. Then, it chooses randomly with uniform probability a bitstring seed one in the type rsakey seed, by the construction new seed one: Rasakey seed. A type T, such as rasakeyseed, aims at denoting a set of bitstrings. Then, initiator process generates the server's public key pkeyrsa corresponding to the coins seed one, by calling the public-key generation algorithm rsapgen (seed one). Similarly, initiator process generates the secret key skeyrsa by calling rsaskgen(seed one).

After that initiator process generates the server's public key signp key and private key signs key for digital signature in RSA scheme in the following procedure: Initiator process chooses randomly with uniform probability a bitstring seed two in the type by the construction new seed two: Key seed. Then, initiator process generates the server's public key signp key corresponding to the coinsseed two, by calling the public-key generation algorithm pkgen (seed two). Similarly, initiator process generates the secret key signs key by calling skgen (seed two). At the same time it produces the hash key key hash in type hash key by the construct new key hash: Hash key. Finally, it sends pkeyrsa, signp key, hash by the public channel c. After sending this message, the control passes to the receiving process which is part of the adversary. Several processes are available, which represent the roles of client and server process. (|(!<sup>n1</sup>client process)|(!<sup>n2</sup>server process)) is the parallel composition of client process |!<sup>n1</sup>client process, server process |!<sup>n2</sup>Server process. It makes simultaneously available the processes.

Client process is modeled as client process in Blanchet calculus in Fig. 7. Client process generates the client-version Client version in type version by the construct new client version: Version, client-random client random in type by the construct new client random: random and cipher-suites client Cipher suitesin type cipher\_suites by the construct new client cipher suites: Cipher\_suites. And then it produces Client Hello message message one in type message using the function concat A (client version, client random, null, client cipher suites) by the construct let message one: Message = concat A (client version, client random, null, client phersuites) in. Finally, it sends message one, one message on by the public channel through the construct c̄⟨one, message one⟩.

After that client process receives the message two, message two\_s in type message from the public channel

```

Let client process =
C ();
(*Client hello*)
New clientversion: Version;
New clientrandom: Random;
New client cipher suites: cipher_suites;
Let message one: message = concat Aclient
Version, clientrandom, null, clientCipher suites in
c1(one, messageone);
c2(=two, message two_s:message);

Let concatA (Agreement_version:version,server_random:random,
sessionid_s:session_id,suites_s:chiper_suites
) =message two_s in

C();
c3 = (three, message three_s:message, signone_s:signature);
Iif check(message three_s, signpkey, signone_s) then
Let concatB (Certify Version: Certificate Version,
name_s:subjectname,certify_info: certificate
) =message three_s in

Let concatinfo(pkeyrsa_s:rsapkey, name_algorithm:algorithmname)=certify_info in
c();
c4 = (four, messageour_s:message);
If messageour_s = Server hello done then
(*Client exchange*)
New pre Master secret:key;
New r2:seed;
Let messagefive:message = enc(key to clear text (pre Master secret), pkeyrsa_s, r2) in
c5(five, messag efive);
(*Client Finished*)
C ();
Let c_s_random_c:input = concat prf (clientrandom, server_random) in
Let hash message_c:hash input = cocat hash one(message one, message five) in

Let key to output (Master secret_c:key)=f (premastersecret,mastersecret,
c_s_random_c
) in

Let verify data: Output = f (masteseecret,clientfinished,
hash(keyhash,hashmessage_c)
) in

Event client(verify data);
c6(six, verify data).

```

Fig. 7: Client process

c2 through the construct c2 (= two, message two\_s: Message). And then it gets the version agreement\_version in type version, server\_random in type random, sessionid\_s in type session\_id and cipher\_suites suites\_s in type cipher\_suites through the function concat A (Agreement\_version: Version, server\_random: random, sessionid\_s: Session\_id, suites\_s: Cipher\_suites) by the construct let concat A (Agreement\_version: Version, server\_random: Random, sessionid\_s: Session\_id, suites\_s: Cipher\_suites) = message two\_s in. Client process sends the message = three, message three\_s: Message, sign one\_s: Signature in the public channel c3 by the construct \*\*\*\*\*.

And then client process gets the digital signature sign one\_s: Signature of message message three\_s: message through the public channel c3 by the construct c3 = (= three, message three\_s: message, signone\_s: signature. It uses the function check () to verify the

digital signature signone\_s: signature of message emessage three\_s: message. If the verification is successful, then it gets certificate version certify version: Certificate version, server subject name name\_s: subject name and certificate certify\_info: Certificate using the construct let concat B (Certify version: Certificate version, name\_s: subject name, certify\_info: Certificate) = message three\_s: in. Then it gets the public key pkeyrsa\_s: rsapkey of the server and the algorithm name\_algorithm: algorithm name from certificatecertify\_info: Certificate using the construct let concatinfo (pkeyrsa\_s: rsapkey, name\_algorithm: algorithm name) = certify\_info.

After that client process receives the message message our\_s: message through the public channel c4 by the constructc4 (= four, message our\_s: Message). If the message message our\_s: Message is server hello Done then it creates the pre master key pre master secret



```

Let Server process =
  c7 (=one, messageone_c: message);

  Let concat A (client_version:version,client_random:random,
  id:session_id,ciphersuites:cipher_suites) = message one_c in

  (*Session*)
  find i<=N such that defined (sessionid [i] && (sessionid [i] =id) then
    let id_store: Session_id=id in
    if id = null then
      new session id: Session_id;
    let id_store = Session id in
    If client_version = Agreement version then
      new server random: Random;
    Let message two: Message = concat A(Agreement version,server random, id_store, suites) in
  c8 (two, message two);
  (*Server certificate*)
  c ();
  New name: subjectname;
  New subject algorithm: Algorithmname;
  Let certificate info: Certificate = concat info (pkeyrsa,subject algorithm) in
  Let message three: Message = concat B (certify, name, Certificate info) in
  new r1: Seed;
  Let sign one: Signature = Sign (message three, signs key, r1) in
  c9 (three, message three, signone);
  (*Server hello done*)
  c ();
  c10 (four, server hello don);
  e ();
  c11(= five, message five_c: message);
  Let inbot (key to clear text (pre Master_secret: Key)) = dec (message five_c, skeyrsa) in
  c ();
  (*Server finished*)
  c12 (= six, verify data_fc: Output);
  Let c_s_random_s: Input = concatprf (client_random, server random) in
  Let key to out put (Master_secret_s: Key) = f(pre Master_secret, maste secret,c_s_random_s) in
  Let hash message_fc: Hash input = cocat hash one (message one_c, message five_c) in
  if f (Master_secret_s, client finished, hash (key hash, hash message_fc)) = verify data_fc then
  Let hash message: Hash input = cocat hash two (message two, message three, Server hello done) in
  event server (verify data_fc);
  c13 , (seven, f (Master_secret_s, server finished, hash (key hash, hash message)))

```

Fig. 8: Server process

in type using the construct new pre Master secret: key and uses the RSA encryption one() to encrypt it with public key pkeyrsa\_s by the construct let message five: Message = one (key toclear text (pre Master secret), pkeyrsa\_s, s2 and gets the message message five in type message. Finally, it sends message message five by the public channel c5 using the construct c3 (three, message three\_s: message, sign one\_s: Signature).

Client process uses the function concatprf() to compute the hash input\_s\_random\_c: Input of message client random, server\_random by the construct let c\_s\_random\_c: Input = concatprf (client random, server\_random) in. And then it uses the function cocat hash one () to calculate the hash input cocathashone of message message one, message five by the construct let hash message\_s: Hash input = cocat hash one (message

one, message five) in. Client process gets the master key master secret\_c: Key and uses the PRF function f() to generate the master key master secret\_keyc: Key by the construct let key to output (message secret\_c: Key) = f (pre master secret, master secret, c\_s\_random\_c in. Also it use the PRF function f() to compute by the construct let verify data: Output = f (master secret\_c, client finished, hash (key, hash, hash message\_c)). Finally, it executes the event event client (verify data) and send it through the public channel c6 by the construct c6 (six, verify data).

Server process is modeled as server process in Blanchet calculus in Fig. 8. Server process receives the message one, message one\_c: Message from the public channel c7 through the construct c7 (= one, message one\_c: Message). And then it uses the function concat A to parse the message message one\_c and gets client

versionclient version: Version, client random client\_random: Random, session id id: Session\_id and cipher suite cipher\_suites: Cipher\_suites by the construct let concat A(client\_version: Version, client\_random: random, id, cipher\_suites)-message one\_c in Server process checks id whether it defined and is equal to sessionid or not by the construct find I<=N such that defined (session id [i] && (session id [i] = id). If the result is ok, then it stores id into id\_store: Session\_id using the construct let id\_store: Session\_id = id in. If is null, then server process generates a new session id in type session\_id by the construct new session id: session\_id and stores it into id\_store by the construct let id\_store = session id. At the same time if client\_version is equal to agreement version, then it creates a random number server random by the construct new server random: random and use the function concat A () to compute the message message two: Message by the construct let message two: message two: Message = concat A (Agreement version, server random, id\_store, suites in. Server process sends message message two by the public channel c8 through the construct c8.

Server process generates the subject name name: Subject name of certificate by the construct new name: Subject name and the subject algorithm of certificate subject algorithm: Algorithm name by the construct new subject algorithm: Algorithm name. At the same time it uses function concatinfo () to generate certificate information certificate info: Certificate by the construct let certificate info: Certificate = concatinfo (pkeyrsa, subject algorithm in and uses the function concat B() to compute the message message three: Message by the construct let message three: Message = concat B (certify name, certificate info) in. And then it generates the digital signature sign one: signature of the message message three: Message using the digital signature function sign () by the construct let sign one: Signature = sign (message three, signs key, r1) in. It also sends message three, sign one through the public channel c9 by the construct c9 <three, message three, sign one> and sends four, server Hello Done through the public channel c10 by the construct c10.

Server process receives the message message five\_c: Message from the public channel c11 by the construct c11 (= five, message five\_c: message). It uses the RSA decryption dec() to decrypt message five: Message and gets the pre master key pre master\_secret: key by the construct let injbot (key to clear text (pre master\_secret: key)) = dec (message five\_c, skeyrsa) in.

After that server process receives the message verify data\_fc: Output from the public channel c12 with the construct c12 (= six, verify data\_fc: Output). It uses the function concatprf to compute the c\_s\_random\_s by the

construct let c\_s\_random\_s: input = concatprf (client\_random, server random) in and uses the PRF function to calculate the master key master\_secret\_s: key by the construct let key to output (master\_secret\_s: key) = f(pre master\_secret, master\_secret, c\_s\_random\_s) in. At the same time it computes the hash input hash message\_fc by the function cocat hash one() through the construct let hash message\_fc: Hash point = cocat hash one (message one\_c, message five\_c) in. If verify\_data\_fc is equal to output of the function f(master\_secret\_s, client finished, hash (key hashm hash message\_fc)), then it uses the function cocat hash two () to compute the hash input hash message: hash input by the construct let hash messageL hash input = cocat hash two (message two, message three, server hello, done) in. Finally, it executes the event event server (verify\_data\_fc) and sends the message f(master\_secret\_s, server finished, hash(key hash, hash message)) by the public channel c13 by the construct c13 (seven, f(master\_secret\_s, server finished, hash (key hash, hash message))).

**MECHANIZED VERIFICATION OF SECRECY AND AUTHENTICATION IN TLS 1.2 HAND SHAKE PROTOCOL WITH CRYPTO VERIF**

The inputs of Crypto verif have two formats. One is channels Front-end. The other is oracles Front-end. In both cases, the output of Crypto verif is same. The main difference between the two inputs is that the oracle front-end is based on oracles and the channel front-end is based on channels.

In this study, channel Front-end is used as the input of Crypto verif. Hence formal model of TLS 1.2 hand shake protocol where Cipher suite is RSA encryption must transform into the syntax of Crypto verif and generate the Crypto verif inputs in the form of channels Front-end.

Here non-injective correspondences and injective correspondences in Table 1 are used to model the authentication from server to client. First non-injective correspondences are used: event event server(x) ==> client(x) authenticate client by server. And then Injective correspondences are then used: event inj: event server(x)==>inj client(x) authenticate client by server.

From Fig. 9-11, the inputs of verification of authentication and secrecy in Crypto verif are presented. The analysis was executed by Crypto verif and succeeded.

Table 1: Correspondences in TLS1.2 protocol

Correspondences
Event server(x)==>client(x)
Inj: Event server(x)==> inj: Client (x)

param N	Const Agreementversion: Version. (*protocol version*)
	Const suites:cipher_suites.(*cryptographic suite*)
	Const certify: certificate version.(*certifi cate verson*)
	Const server hello done:message.(*Server hello done*)
	Const mastesecret: Label.
	Const server finished: Label.(*h:label"server finished"*)
	Const client finished:label.(*h:label"client finished"*)
	Const null:session_id.(*session_id is null*)
	Const one:host
	Const two:host
	Const three:host
	Const four:host
	Const five:host
	Const six:host
	Const seven:host
Type version [large, fixed, bounded]	
Type random [large, fixed, bounded]	
Type seed [fixed]	
Type rsakeyseed [large, fixed]	
Type rsapkey [bounded]	
Type rsaskey [bounded]	
Type clear [textlarge, bounded]	
Type ciphertext [large]	
Type keyseed [large, fixed]	
Type pkey [bounded]	
Type skey [bounded]	
Type signinput [fixed]	
Type signature [bounded]	
Type hashkey [fixed]	
Type hashinput [fixed]	
Type hashoutput [bounded, fixed]	Fun key to clear text (key): Clear text [compos]
Type label [fixed]	Fun key to out put (key): Output [compos]
Type keyfixed, [bounded]	Fun concat A $\left( \begin{matrix} \text{Version, Random,} \\ \text{Session\_id, Cipher\_suites} \end{matrix} \right)$ : Message [compos]
Type session_id [large, fixed]	
Type cipher_suites [large, fixed, bounded]	Fun concat B $\left( \begin{matrix} \text{Certificate version,} \\ \text{subjectname, certificate} \end{matrix} \right)$ : Message [compos]
Type CertificateVersion [large, bounded]	
Type Certificate [large]	
Type subjectname [large, fixed]	Fun concat info(rsapkey, algorithmname): Certificate [compos]
Type algorithmname [large, fixed]	Fun concatprf [random, random]: Input [compos]
Type Exchange algorithm [large, fixed]	Fun cocat hash one (message, message): Hash input [compos]
Type pre Master secret [large, fixed, bounded]	Fun cocat hash two (message, message, message): Hash input [compos]
Type message [large, fixed, bounded]	
Type host [bounded]	
Type input [large, bounded]	Proba penc
Type output [fixed, bounded]	Proba penccoll
	Proba psign
	Proba psig
	ncoll
	Proba phash
	Proba pprf

Fig. 9: Inputs of TLS1.2 protocol in cryp to verif

```

Define PRF_new (key seed, key, input, output, kgen, f, Pprf) {
Param N1, N2, N3.
Fun f (key, label, input): Output.
Fun kgen (key seed): Key.
Equiv N3 new r: key seed; new label: Label; N1 of (x:input): = f (kgen(r), labelc, x)
<=(N3 *Pprf (time+(N3-1)*(time(kgen) + N1 *time (f, max length (x))), N1, max length (x)))=>
N3 new r: Key seed; N1 of(x:input): =
Find [unique] j<=N1 such that defined (x[j],r2[j]) and other uses(r2[j]) and x = x[j] then r2[j]
Else new r2: output; r2.
}
Expand IND_CCA2_public_key_enc (rsakey seed, rsapkey, rsaskey, cleartext, message,
Seed, rsaskgen, rsapkgen, enc.dec, injbot, Z,Penc,Penccoll).
Expand UF_CMA_signature (key seed, pkey, skey, message, signature, seed, skgen, pkgen, sign, check,
Psign,Psigcoll).
Expand collision_resistant_hash(hashkey, hashinput, input, hash,Phash).
Expand PRF_new (key seed, key, input, out put, kgen, f,Pprf).
Event server (output). event client (output).
Query x:output; event server (x)==>client(x).query x:output; inj:event server(x)==>inj:client(x).
Query secret premastersecret.
Chaunel start, c, c1, c2, c3, c4, c5, c6, c7, c8, c9, c10, c11, c12, c13

```

Fig. 10: Continue

```

Let Client process=
  in(c, ());
  (*Client Hello*)
  New client version: Version; new client random: Random; new client cipher suites: Cipher_suites;
  Let message one: Message = concat A (client version, client random, null, client cipher suites) in
  Out (c1, (one, message one));
  In(c2, (=two, message two_s: Message));
  Let concat A (Agreement_version: Version, server_random: Random,
Session id_s: Session_id, suites_s: Cipher_suites) = message two_s in
  Out(c, ());
  In (c3, (=three, messagethree_s:message, signone_s:signature));
  If check(messagethree_s, signpkey, signone_s) then
  Let concat B (Certify version: Certificate version,
Name_s: Subject name, certify_info: Certificate) = message three_s in
  let concat info(pkeyrsa_s: Rsapkey, name_algorithm: Algorithmname) = certify_info in
  out(c, ());
  In(c4, (=four, message our_s: Message));
  If message our_s = server hello done then
  (Client exchange)
  New premaster secret:key; new r2: seed;
  Let message five: message = enc (key to clear text (premaster secret, r2) in
  [fixed][fixed** *
  [fixed][fixed astersecret), pkeyrsa_s, r2) in
  out(c5, (five, message five));
  (Client finished)
  in(c, ());
  Let c_s_random_c: Input = concat prf (client random, server_random) in
  Let hash message_c: Hash input = cocat hash one (message five) in
  [fixed][fixed** *
  [fixed][fixed geone, message five) in
  Let key to output (masters ecet_c: Key) = f (pre master secret, maste secret, c_s_random_c) in
  Let verify data: Output = f(maste rsecret_c, client finished, hash (key hash, hash message_c)) in
  Event client (verify data);
  out(c6, (six, verify data)).
  
```

Fig. 10: Inputs of TLS1.2 protocol in cryp to verif

```

Let server process=
  in(c7, (=one, message one_c:message));
  Let concat A (client_version: Version, client_random: Random, id: Session_id,
Cipher suites: Cipher_suites) = message one_c in
  (* SessionId *)
  Find i<=N suchthat defined (session id[i]) && (session id[i] = id) then let id_store: Session_id = id in if id = null then
  New sessionid:session_id;
  Let id_store = session id in if client_version=Agreement version then new server random: Random;
  Let message two: Message = concat A (Agreement version, server random, id_store, suites) in out (c8, (two, message two));
  (* Server certificate *)
  In(c, ()); new name: Subject name; new subject algorithm: Algorithmname;
  Let Certificate info: Certificate = concatinfo (pkeyrsa, Agreement version) in
  Let message three: Message = concatB(certify, name, Certificateinfo) in new r1:seed;
  Let signone: Signature = sign (message three, signskey, r1) in out(c9, (three, message three, signone));
  (* Server hello done *)
  In(c, ());
  Out(c10, (four, server hello done));
  In(c11, (= five, message five_c:message));
  Let injbot (key to clear text (pre Master_secret:key)) = dec (messagefive_c, skeyrsa) in out(c, ());
  (* Server finished *)
  In(c12, (= six, verifydata_fc:output));
  Let c_s_random_s: Input = concatprf(client_random, server random) in
  Let key to output (Master secret_s: Key) = f(pre Master_secret, mastesecret, c_s_random_s) in
  
```

Fig. 11: Continue

```

Let hash message_fc: Hash input = cocat hash one (message one_c, message five_c) in
if f(mastersecret_s, clientfinished, hash(keyhash, hash message_fc)) = verifydata_fc then
let hash message:hash input = cocathash two(message two, message three, server hello done) in event server (verify data_fc);
out(c13, (seven, f(maste rsecret_s, server finished, hash (key hash, hash message)))).
process
  In(start, ());
  New seedone:rsakey seed;
  Let pkeysa: Rsapkey = rsapgen (seed one) in
  Let skaysa: Rsaskey = rsaskgen (seed one) in new seedtwo:key seed;
  Let signpkey: Pkey = pkgen (seed two) in
  Let signskey: Skey = skgen (seed two) in new keyhash:hashkey;
  Out(c, (pkeysa, signpkey, keyhash));
  ((!N Client process) (!N Server process))

```

Fig. 11: Inputs of TLS1.2 protocol in crypto verif

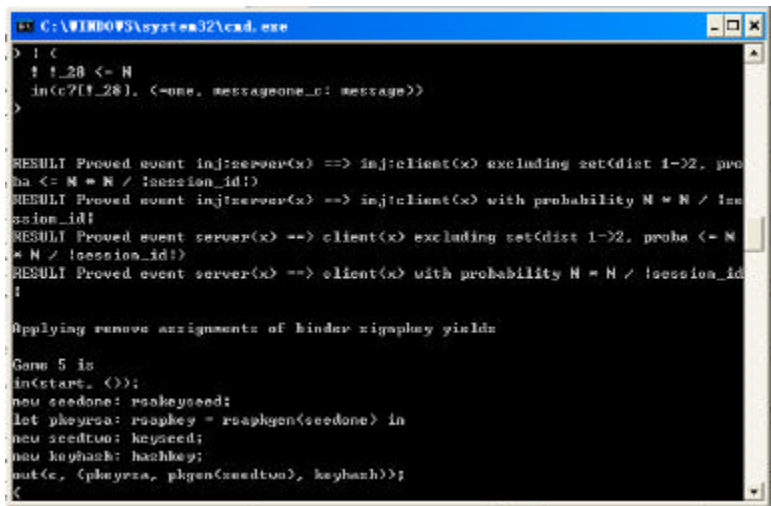


Fig. 12: Authentication of TLS 1.2 protocol in crypto verif

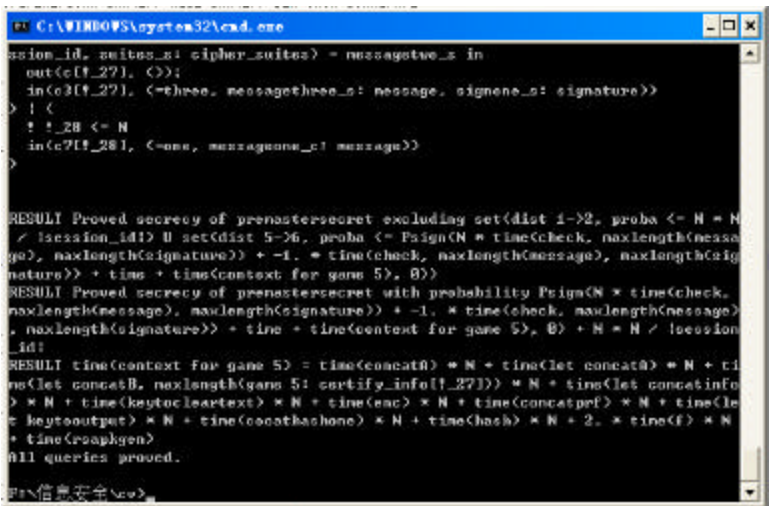


Fig. 13: Secrecy of TLS 1.2 protocol in crypto verif

The results show in Fig. 12 and 13. TLS1.2 protocol where Cipher Suite is RSA encryption is proved to

guarantee authentication from server to client and the secrecy of pre master key in computation model.

## CONCLUSION

During the past several years TLS protocol has been implemented and deployed widely in many web-based applications. According to the related references, until now it is not found that security analysis of TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool in computational model. Hence, in this study, Blanchet calculus in computational model is used to analyze TLS 1.2 protocol where Cipher suite is RSA encryption with mechanized tool. The result shows that it has confidentiality of pre master key and authentication from server to client. The first mechanized verification on TLS 1.2 protocol where Cipher suite is RSA encryption in computational model of in active adversary is executed.

In the near future the verification of the Java implementation of TLS 1.2 protocol in computational model is very interesting.

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