Performance Analysis and Improvement of OFDM System Based on BCH Channel Coding and DCT Technique

Ali Jawad Ibada and Muntadher Kadhim Abdullah
Department of Computer Technical Engineering, College of Technical Engineering,
The Islamic University, Najaf, Iraq

Abstract: Principles of Orthogonal Frequency Division Multiplexing (OFDM) are widely used in wireless communication. In OFDM system, many digital data are transmitted as sub-carriers. All sub-carriers are orthogonal to each other. High spectral efficiency are obtained due to the spectrum are quite narrow. OFDM also has advantages of saving of bandwidth, easy to implement modulation and demodulation, easy equalization, protection against Inter-Symbol Interference (ISI) and so on. However with all these advantages, there is a major disadvantage that it has large Peak-to-Average Power Ratio (PAPR). Large PAPR value makes system performance quite sensitive to distortion introduced by nonlinear amplifier, caused by nonlinear components. These non-linear components make the Bit Error Rate (BER) performance degraded. In this study, a proposed OFDM system based on BCH channel coding and Discrete Cosine Transform (DCT) technique are used to enhance performance of OFDM system by reducing the PAPR value without serious increasing in computational complexity and this leads to reduce the BER. BER performance also will be improved over Additive White Gaussian Noise (AWGN) and fading channels. All these are obtained with low cost of implementation, simple hardware and no require side information. Finally, results of simulation show the proposed system performance are much better comparing with that of the conventional OFDM system.

Key words: OFDM, DCT, PAPR, ISI, BCH, hardware

INTRODUCTION

The definition of frequency-selective channel is either the symbol period T is lower than the maximum delay of the channel’s impulse response T_d or the channel’s bandwidth B_c is large than the coherence band B_c. The receiver will be exposed to ISI when the channel is frequency-selective. To reduce ISI, equalizer must be used in the receiver. It is difficult to build an equalizer practically. To avoid channel equalization, each channel separated to several sub-bands, so that, B_c=0.1 B_c. Thus, ISI will be eliminated in each sub-band. This is the principle of multi-carrier communication system (Pischella and Ruyet, 2015). There are several multi-carrier modulations exist, one of these types is OFDM. In broadband wireless communication, OFDM are vastly used. Multi sub-carriers are used to send data. The sub-carriers are orthogonal one to another. High spectral efficiency is obtained because of orthogonality (Patidar and Parikh, 2011). OFDM also has advantages of saving of bandwidth, easy to implement modulation and demodulation, easy equalization, protection against ISI and so on. The orthogonality property is shown in Fig. 1. Inverse Discrete Fourier Transform (IDFT) is used to get modulation process also the demodulation process is achieved by using Discrete Fourier Transform (DFT) (Edfors et al., 1995). There is a problem with using these transforms, the problem is very large number of complex multiplications.

To solve this problem, Fast Fourier Transform (FFT) is used to reduce the number of complex multiplications (Minallah and Raja, 2006).
Unfortunately with all advantages of OFDM, there is a major disadvantage. It has large PAPR value. Large PAPR value occurs when all subcarriers are added. Thus, the peak power is N times higher than the average power. Large PAPR value leads to degrade the performance of OFDM system by making the analog amplifier operates in the nonlinear range. This degrades the BER performance because the signal will be distorted also the amplifier will consume extra power (Natalia and Mathar, 2008). Many previous researchers had studied PAPR reduction techniques (Alkhdran et al., 2012, Pradeep et al., 2013, Jayashri et al., 2015, Chih-Peng et al., 2010, Alekya and Mohana, 2016; Koudoungnon et al., 2012; Gupta and Saxena, 2013; Gupta and Bhaduria, 2013; Garg et al., 2017) including clipping, coding, companding transform, Partial Transmit Sequence (PTS), Selective Mapping (SLM) and so on. However, most of these proposed schemes have either low BER performance or a high complex mathematical operations as well as higher hardware complexity of transmitter and receiver. This research is proposed a method based on BCh channel coding and DCT technique. MATLAB Software is used to build the proposed system and the simulation results show clearly the reduction in the PAPR value which leading to reduce BER. The BER is improved also over AWGN and multipath channels.

**OFDM system model:** The traditional OFDM transceiver block diagram is shown in Fig. 2. In a chain of transmission, generate a binary data series representing the voice, data, image or analog information. At the beginning, the serial binary data will convert to parallel stream according to number of sub-carriers (N). The individual parallel data streams are modulated into digital modulation format (QAM, QPSK, BPSK, etc.). At this point, constellation mapper is achieved. Then, orthogonal subcarriers are required for transmission (Viswanathan, 2013). IDFT is used to get these orthogonal subcarriers. Same operation can be performed by Inverse Fast Fourier Transform (IFFT) but IFFT requires less multiplication hardware. Equation 1 and 2 for FFT/IFFT function are shown below:

\[
Y(k) = \sum_{n=0}^{N-1} y(n)e^{-j2\pi kn/N} \\
y(n) = \sum_{k=0}^{N-1} Y(k)e^{j2\pi kn/N}
\]

Where:
- \(y(n)\) = The discrete time domain of OFDM signal
- \(Y(k)\) = The frequency domain

Equation 1 is used to calculates the FFT and Eq. 2 for IFFT. The OFDM time domain signal is carried by the required frequency (Gupta and Bhaduria, 2013).

The final part of the samples is copied to the beginning of OFDM signal before transmission, this operation called Cyclic Prefix (CP). CP is used to reduce IISI. At receiver part, all these process are reversed to get back information. CP is discarded before FFT is applied. After the FFT is performed, a simple equalizer is used to estimate the transmitted OFDM symbols. Finally, bit stream recovered by decoding the complex symbols (Sajed, et al., 2014).

**Peak to Average Power Ratio (PAPR):** PAPR in OFDM signal is defined as a ratio of the instant peak power of the signal to mean power as shown in Eq. 3:

\[
\text{PAPR} = \frac{\max \{ y(n)^2 \}}{E\{y(n)^2\}}
\]

Where:
- \(\max \{ y(n)^2 \}\) = The instant peak power of \(y(n)\)
- \(E\{y(n)^2\}\) = The average power of \(y(n)\) (Choudhary and Gupta, 2013)

The large PAPR value in OFDM system is the main disadvantage because of it produces distortion in signal
and poor efficiency of power (Joshi, 2012). The reason of large PAPR is the large dynamic range of input signal. To design any system has to research with large dynamic range of the signal, large linear region is required. To deal with large PAPR, it requires highly efficient High Power Amplifier (HPA) that work in large linear region. Because of large linear region, the components of HPA are failed to build, thus, result in saturation (Khalid, 2009; Cho et al., 2010). The saturation produces in band distortion which increasing BER and out of band which causes Adjacent Channel Interference (ACI). Therefore, it is important to reduce PAPR value before transmitting the signal into nonlinear Digital to Analog Converter (DAC) and HPA to improve both BER vs. $E_b/N_0$ performance of the system and the power efficiency (Khalid, 2009; Cho et al., 2010).

**MATERIALS AND METHODS**

**Proposed OFDM system:** The proposed OFDM System is shown in Fig. 3. This system consists of two extra components compared with conventional OFDM system. The first component is adding channel coding to the system and the second component is adding the Discrete Cosine Transforms (DCT) before IFFT block in the transmitter and adding Inverse DCT (IDCT) after FFT block in the receiver.

**Channel coding:** In practical, no transmitted signal can reach its destination without affected by noise. To make the transmitted signals to better combat of different channel deterioration, therefore a channel coding is used (Sklar, 2001). The process of channel coding is putting additional bits (called parity check or correction bits) to data before transmission that makes the receiver find out or correct errors in capable limitations. The classification of channel codes are: convolutional codes and block codes. A separate mathematical structure is used in convolutional codes. On the other hand, block codes are used abstract algebra and arithmetical finite field. The k information block bits are converted to n block coded bits which produce (n, k) block codes. Examples of block codes are Bose Chaudhuri Hocquenghem (BCH) codes and hamming codes (Sklar, 2001). However, in this research the BCH codes are chosen as a channel coding method. The block length in BCH is unlimited with different code rates. Class of BCH codes is a large class of cyclic multiple error correcting codes. Binary BCH code has the parameters: $n = 2^m - 1$, $n - k = rsmt$, minimum Hamming Distance $HD = 2t + 1$ for $m = 3$ and $t < 2^{m-i}$, where $r$ is parity check or correction bits, $t$ is the number of error correcting capability and $m$ is integer positive number. So, $n$ takes only the values 7, 15, 31, 63, ..., these values are the dimension of the non-zero elements of Galois Fields ($GF(2^m)$) (Sklar, 2001).

The decoding algorithm of BCH is simple and easily realized that is capable of correcting all random patterns of $t$ errors.

**BCH code generation:** The parity check matrix $[H]$ of this BCH code with $n = 2^m - 1$ can be written in terms of the primitive non-zero elements of $GF (2^m)$. The general form of it is Eq. 4:

$$[H] = \begin{bmatrix}
1 & \alpha & \alpha^2 & \ldots & \alpha^{k-1} \\
1 & \alpha^2 & \alpha^4 & \ldots & \alpha^{2k-2} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \alpha^m & \alpha^{2m} & \ldots & \alpha^{2^{m-1}-1}
\end{bmatrix}$$

(4)

where, $\alpha$ is a primitive non-zero element in $GF (2^m)$. Notice that it is written such that the elements of the 2nd row are the squares of the 1st row and the elements of the 3rd row are the cubic of the elements of the 1st row and so on. Also, the number of rows is twice the error correction capability ($2t$). The generator polynomial $g(x)$ will Eq. 5:

$$g(x) = \text{LCM} \left\{ M^{t}(x), M^{2t}(x), \ldots, M^{2^{m-1}t}(x) \right\}$$

(5)

Fig. 3: Proposed OFDM system
Where:
\[
\text{LCM} = \text{The Least Common Multiple}
\]
\[
\text{M}^{i}(x) = \text{The Minimal polynomial for the non-zero elements } a^i \text{ for } i = 1, 2, ..., 2t \quad (Khalid, 2009)
\]

A systematic (n, k) cyclic code word is generated from a generator polynomial \( g(x) \) of order \( r \) such that if \( \text{Data} (D) = [d_0, d_1, ..., d_d] \), then, \( d(x) \) is the data polynomial
\[
d(x) = d_0 + d_1x + d_2x^2 + d_3x^3 + \cdots + d_d x^d \quad (6)
\]

Whereas the data digits, then, the codeword output will be Eq. 7:
\[
C(x) = \text{Rem} \left( \frac{x^d d(x)}{g(x)} \right) + x^d d(x) \quad (7)
\]

where, \( \text{Rem} \) is the Remainder of long division.

**Binary BCH codes:** For binary BCH coding, then, it can show that the minimal polynomials for every even power of \( a \) is the same as some previous odd power, then Eq. 8:
\[
g(x) = \text{LCM} \left\{ M^1(x)M^2(x)M^3(x), ..., M^{2t}(x) \right\} \quad (8)
\]

And parity check matrix used for code generation is Eq. 9:
\[
\begin{align*}
[H] = & \begin{bmatrix}
1 & \alpha & \alpha^2 & \cdots & \alpha^{n-1} \\
1 & \alpha^2 & \alpha^3 & \cdots & \alpha^{n-2} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \alpha^{n-3} & \alpha^{n-4} & \cdots & \alpha^{n-1} \alpha^{n-1}
\end{bmatrix}
\end{align*} \quad (9)
\]

**Decoding of BCH codes:** Suppose that transmitted polynomial is Eq. 10:
\[
C(x) = c_0 + c_1 x + c_2 x^2 + \cdots + c_{n-1} x^{n-1} \quad (10)
\]

If the received polynomial is Eq. 11:
\[
R(x) = r_0 + r_1 x + r_2 x^2 + \cdots + r_{n-1} x^{n-1} \quad (11)
\]

Let \( E(x) \) be error polynomial, then \( R(x) = C(x) + E(x) \). To decode BCH codes efficiently, it must be firstly calculate the syndromes elements in \( GF(2^n) \) \( [S] = [S_0, S_1, S_2, S_3] \) by multiplying the received codeword \( [R] \) with \( [H] \), secondly find the error location polynomial from \( [S] \) and finally determine the locations of errors by finding the roots of the error location polynomial (Ryan and Lin, 2009).

**DCT:** It is a one type of fourier transformation family such as DFT. The calculation of DCT is fast, real, separable and orthogonal. Its transformed data has better energy and compression. Compare to DFT, DCT has lower energy, less complexity, real symmetric transformation (Gupta and Saxena, 2013). One dimensional-DCT \( Z[k] \) is given Eq. 12:
\[
Z(k) = \sum_{n=0}^{N-1} Z(n) \cos \left( \frac{2\pi nk}{N} \right) \quad (12)
\]

where, \( k = 0, 1, 2, 3, ..., N-1 \). And one dimensional inverse discrete cosine transform (1D-IDCT) \( x(k) \) is given (Jagadeesh, 2007) Eq. 13:
\[
Z(n) = \sum_{k=0}^{N-1} Z(n) \cos \left( \frac{2\pi nk}{N} \right) \quad (13)
\]

Where \( n = 0, 1, 2, 3, ..., N-1 \). Discrete-time sinusoids are given Eq. 14:
\[
C(N, K) = \cos \left( \frac{2\pi nk}{N} \right) \quad (14)
\]

where, \( n = 0, 1, 2, 3, ..., N-1, k = 0, 1, 2, 3, ..., N-1 \). DCT matrix \( C(n, k) \) are orthogonal matrix vectors (Rows or Columns), this is used to decrease autocorrelation between the OFDM signals. Thus, less PAPR is obtained (Hsu and Do, 2007). So that, the relationship between PAPR and autocorrelation is given below Eq. 15:
\[
PAPR = 1 + \frac{2}{N} \sum_{k=0}^{N-1} |p| \quad (15)
\]

where, \( p \) is the autocorrelation of the OFDM signal.

**RESULTS AND DISCUSSION**

Studying performance of the proposed OFDM system is performed using MATLAB program. Table 1 shows simulated parameters that were used in OFDM system as defined in IEEE 802.11 specifications. Firstly, the simulation result of PAPR when using the conventional OFDM system is shown in Fig. 4.

The PAPR is large value, so that, it equals to 16 dB. Remind that a larger PAPR value makes system complex, increasing BER and the efficiency of power amplifier is decrease. When placing DCT technique before FFT in the system, PAPR approximately equals to 4.94 dB as shown in Fig. 5. PAPR here has an advantage over conventional OFDM, it has lower value because of DCT reduces the autocorrelation between the OFDM signals which is one of root cause to PAPR reduction.
The proposed OFDM system in this research uses both DCT and BCH channel coding. DCT used here to reduce PAPR while BCH used for detecting and correcting errors as well as reducing PAPR because of the redundant bits. Therefore, PAPR when using the proposed OFDM system is shown in Fig. 6. PAPR here equals to 4.233 dB which reduced by 11.767 dB in compared with conventional OFDM system while it is reduced by 0.707 dB in compared with using DCT only. This proposed method is compared with another research which used Selective Mapping (SLM) method (Mhatre and Khot, 2015). In this research, PAPR is approximately 4.233 dB while PAPR in SLM method is 6.391 dB at U = 16 (number of phase sequences) and PAPR = 7.1 dB at U = 8. Also in this study, the reduction of PAPR value is obtained without serious increasing in computational complexity as well as low hardware complexity.

Now, the system performance widely improved after reducing the PAPR value. But AWGN and fading channels also degrade the performance of OFDM system.
Performance of OFDM system is degraded due to Large PAPR value, this problem makes high power amplifier operate in nonlinear region which distorting the signal. Thus, BER will be increased and consuming extra power by amplifier. Many previous research has studied PAPR reduction. But most of them have either poor BER performance or computational and hardware complexity. In this research, it proposed OFDM system based on BCH channel coding and DCT technique to enhance OFDM system performance. Here, BCH is used for both detecting and correcting errors as well as to reduce PAPR because of the redundant bits. While, DCT in the proposed system is used to extremely reduce the PAPR. From results, it is shown that acceptable PAPR value is obtained, so that, PAPR is approximately 4.233 dB. PAPR when using the proposed system is reduced by 0.707 dB in compared with using DCT only while it is reduced by 11.767 dB in compared with the conventional system. This reduction in PAPR guarantee leads to reduce BER because HPA will not produce any distortion. BER also is improved over AWGN and fading channels when using the proposed OFDM system because of using BCH channel coding which correct four errors in each OFDM signal. So that, the BER value equals to $10^{-7}$ at $E_b/N_0=4$ dB over AWGN channel while smallest BER value equals to $10^{-9}$ at $E_b/N_0=26$ dB is obtained over fading channel. Finally, the proposed OFDM system performance is better than conventional OFDM system. In comparing with the exist study in method (Mhatre and Khot, 2015; Muraliabu et al., 2012), the reduction of PAPR in this study is better. So that, heavily reduction in PAPR value is obtained without serious increasing in computational complexity, low cost and simple hardware implementation.
ACKNOWLEDGEMENT

This research was supported by the Islamic University research grant PRG-IUNAJAF-2019.

REFERENCES


