

## Wavelet-Based Medical Augmented Reality CSG Objects Watermarking

H. Djaghloul

Departement d'Informatique, Université Ferhat Abbès, Sétif, Algérie

**Abstract:** Augmented reality systems can lead to major improvement of patient care by using the preoperative CT-Scan or MRI medical data intraoperatively during the intervention. In this study we propose to model human organs and laproscopic instruments using constructive solid geometry (CSG) objects and we give some algorithms to watermark CSG modelled objects by finding an empty box in the bounding box of the object, then considering another CSG modelled object. We create a new CSG object with left leaf the original object and right leaf the other one, linked by minus operator. A great deal is to multi-resolution analysis and trees.

**Key words:** Watermarking, copyright, CSG modeling, security, wavelet, multi-resolution analysis

### INTRODUCTION

The numeric marking is a relatively new and very attractive research domain that can be applied on a multitude of formats<sup>[1-3]</sup> and presentations of pictures and images. Its objective is to solve problems related with security and protection of publications and the numeric productions that can be stored on supports not secured as Internet. Fields landed by the numeric marking cover all formats that can exist practically: text, audio, picture, video<sup>[3-8]</sup>, but few works have been led for watermarking geometric 3D objects<sup>[9-11,7]</sup>.

Watermarking a media is hiding information in the media itself without major modification. Thus, we don't need supplementary elements like header files or plug-ins added to documents to contain the mechanism of security or to change the structure and the format of documents completely as with the cryptography. The exponential evolution of Internet and the necessity to present the conceived electronic work the most quickly give back watermarking the more profitable economically and technically with regard to competitor solutions.

In augmented reality systems<sup>[12,13]</sup> applied on medical imagery such as MRI or CT-Scan as principal sources of preoperative data and video-coloured images in the case of laparoscopic mini-invasive surgery, watermarking techniques can be used to control the 2D/3D registration step or embedding medical information such as surgical planning actions or physical an chemical properties.

The watermarking must be the most robust against all types of attacks. Therefore, transformations as rotation, translation, scaling or cropping applied to the original work must not destroy the hidden information. In addition, the system of marking must be able to mix the added information intimately and to recover it without damaging the quality of the original media.

This study deals with watermarking CSG modelled objects<sup>[1,14]</sup>. We propose new methods for public watermarking 3D objects based on solid modelling using either CSG objects or numerical data represented by a collection of spheres. In the second section, we use multi-resolution analysis by wavelets for more robustness against local attacks and transformations. The method of analysis by wavelets is relatively new although its theoretical foundations come back to the works of Joseph Fourier in the 19th century (see<sup>[2,15,17,18]</sup> for more details).

#### Watermarking algorithms for CSG modelled objects:

Four steps are needed for watermarking: finding an empty bounding box in the hull bounding box of the object, positioning the mark, choosing and extracting it.

**Finding an empty bounding box:** In order to embed the watermark data, an empty bounded volume is selected so that it will not be deformed by topological and set operators. For the watermark to be robust, we propose to bound the CSG primitives (CSG tree leafs) using boxes. Then, by making a projection on the laparoscopic view plan we can find the totally empty bounding boxes in which the surgical planning or the physical constraints can be hidden.

**Positioning the mark:** In this study, we suggest to put the mark in any empty box  $B_o$  included in the bounding box  $BB$  of the CSG object. This technique may be used to mark every 3D object or even a scene if one can find such a  $B_o$  in the bounding box of the object or the scene (for example: by subdivision). For this aim, we create a new CSG object whose left leaf is the object and right leaf is the mark.

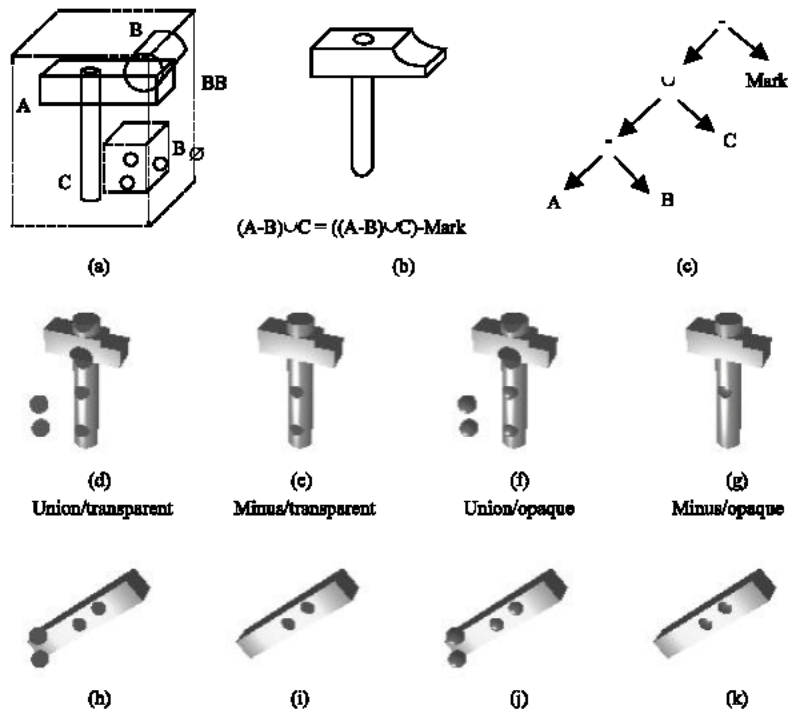


Fig. 1: Marked object

Figure 1(d-g) (resp. (h-k)) shows a marked hammer (resp. a single object) with four spheres in the four cases: (union/minus) operator with (opaque/transparent) spheres. Two of the spheres do not intersect the objects, while the two others intersect them. Holes appear in each of Fig. 1 (f,g,j,k). Then, to mark efficiently the objects, the spheres (either opaque or transparent) must not intersect them, so they must be in an empty box included in the bounding box.

**Choosing the mark:** We choose another fictive CSG object as the mark with  $B_\circ$  as its bounding box. Then we create a CSG object whose root is minus operator, left leaf is the original CSG object and right leaf is the mark. This method does not affect the original object.

The mark may be any CSG object like in Fig. 2(a) or a set of  $2^n$  fictive spheres sufficiently near from each other with sufficiently small diameter (Fig. 2(b)). This case is treated by a multi-resolution analysis like in wavelets techniques.

To ensure properties of a good watermarking, we propose using distances between the spheres.

Let  $S_0 = \{1, 2, \dots, 2^n\}$  be an ordered set of  $2^n$  spheres and  $x_i$  be the x-coordinate of the  $i$ th centre,  $i=1, \dots, 2^n$ . Let  $R_0 = D_0 = \emptyset$  and for  $i = 1, \dots, n$ ,  $S_i = \{1, 2, \dots, 2^{n-i}\}$ ,  $R_i = \{2^{n-i} + 1, 2^{n-i} + 2, \dots, 2^{n-i} + 2^{n-i}\}$ ,  $D_i = \{d_{2^{n-i}+1}, d_{2^{n-i}+2}, \dots, d_{2^{n-i}+2^{n-i}}\}$ , where  $d_{2^{n-i}+j} = x_{2^{n-i}+j} - x_j$ ,  $j = 1, \dots, 2^{n-i}$ .  $S_i$  is the first half of  $S_{i-1}$  and  $R_i$  is the second.  $D_i$  is a set of distances between

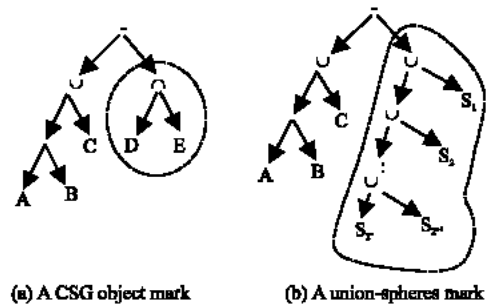


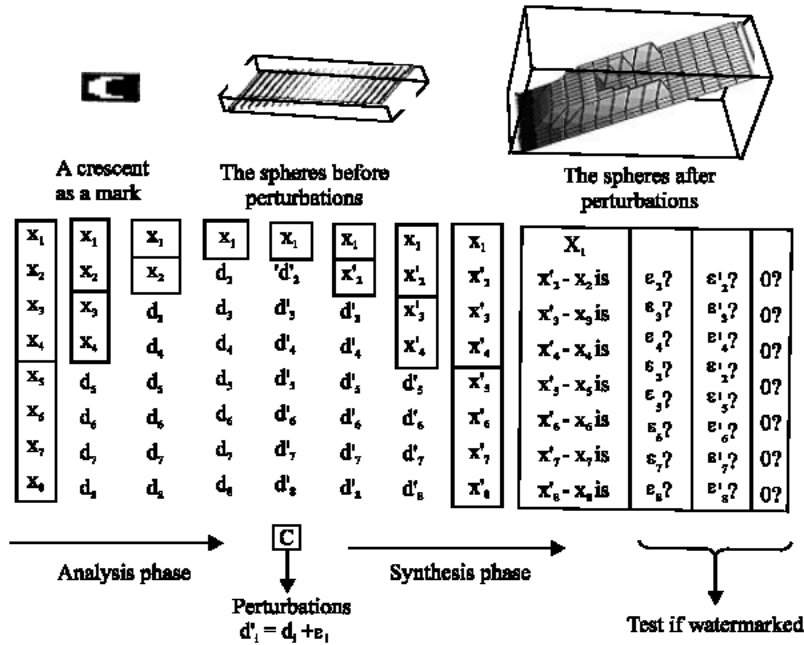
Fig. 2: Possible mark types

Table 1: Data for  $2^3$  spheres

$x_1$	$X_1$	$S_1$	$x_1$
$x_2$	$X_2$	$R_1$	$d_1 = x_2 - x_1$
$x_3$	$X_3$	$S_2$	$d_2$
$x_4$	$X_4$	$R_2$	$d_3 = x_4 - x_2$
$x_5$	$d_4 = x_5 - x_1$	$D_1$	$d_4$
$x_6$	$d_5 = x_6 - x_2$		$d_5$
$x_7$	$d_6 = x_7 - x_3$		$d_6$
$x_8$	$d_7 = x_8 - x_4$		$d_7$

centres of the spheres in x-direction. We note that the order in  $S_0$  induces the same order in all the  $S_i$ 's,  $R_i$ 's and  $S_i \cup R_i \cup R_{i-1} \cup \dots \cup R_1$ . Table 1 shows how to store these data. However, same tables can be created for y,z-directions.

Table 2: Perturbations of the spheres in x-direction using a crescent as a mark



If  $I_r$  denotes the identity matrix and  $\Theta_r$  the null matrix with order  $r$ , then  $S_j$  and  $D_j$ ,  $j = 1, \dots, n$ , are computed as follows in the analysis phase:

$$S_j = (I_{2^{n-j}}, \Theta_{2^{n-j}}) S_{j-1}$$

$$D_j = (-I_{2^{n-j}}, I_{2^{n-j}}) S_{j-1}$$

while  $S_{j-1}$ ,  $j = n, n-1, \dots, 1$ , is computed as follows in synthesis phase:

$$S_{j-1} = \begin{bmatrix} I_{r'} & \Theta_{r'} \\ I_{r'} & I_{r'} \end{bmatrix} \begin{bmatrix} S_j \\ D_j \end{bmatrix}$$

**Insertion of the mark:** Now, let us perturb last column  $D$  in Table 1 by adding (or subtracting) a small vector  $\epsilon$  in such a way that the spheres stay in  $B_o$  (Table 2). Some types of perturbation exist<sup>[3,7,8,2]</sup>, we give another ones:

- Let  $\epsilon$  be the maximal authorized error vector. The mark  $M = [b_0 b_1 \dots b_m]$  is a binary representation of the mark. Then,  $D_i$  is replaced by  $D_i + \epsilon_i$  if  $b_i = 1$  and by  $D_i - \epsilon_i$  if  $b_i = 0$ ,  $i=0, \dots, m$ . This method requires  $m = 2^n - 1$ .
- Another method consists of representing each line  $L_i$  of the mark by a sequence of bits  $M_i = [b_{i0} b_{i1} \dots b_{im}]$  and embedding  $M_i$  in the decimal part of  $D_i$ ,  $i=0, \dots, m$ .
- $\epsilon$  may be respectively the red, green, blue-component of pixel colors in an image in the  $x, y, z$ -direction.
- A method of perturbations based on trees and multi-resolution techniques.

**Robustness:** The method is robust against rotation and translation attacks since distances are not affected by these transformations.

If a scale transformation with factor  $\alpha$  in  $x$ -direction is applied, then we show easily that distances are multiplied by  $\alpha$ . So, column  $C$  in Table 2 will be multiplied by  $\alpha$  and it is easy to make the test.

**Extraction of the mark:** If the mark is any CSG object, it is extracted by only considering the right leaf of the new object. The mark is inserted in the bounding box of the initial object but is not concerned with ray tracing. So, the extraction does not need the original object, this technique is robust and rotation, translation and scaling have no effect, invisibility is ensured since the root of the CSG tree is minus operator.

If the mark is the set of spheres, Table 2 is all what we need. The object is watermarked if the last column is  $\epsilon$ , not watermarked if it is 0 and attacked otherwise.

### CONCLUSION

In this study, we propose new methods for very high capacity watermarking 3D objects using multi resolution techniques based on wavelets. The mark is embedded in topological properties of the model. Our algorithms give robustness to various attacks like affine transformations. However, other attacks like projections and cropping have to be studied with more detail.

**REFERENCES**

1. Huw, J., 2001. Computer Graphics through Key Mathematics, Springer-Verlag, 2001.
2. Stephan, D., 2001. Distributed Virtual Worlds: Foundations and Implementation Techniques Using VRML, Java and CORBA, Springer-Verlag (2001), ACM Computation Classification (1998): 1.3.6-7, H.5.3, H.5.1, C.2.4, D.2.
3. Dugelay, J.L., C. Rey and S. Roche, Introduction au Tatouage d'Images, <http://www.eurecom.fr/~image>.
4. Roche, S. and J.L. Dugelay, 1998. Image watermarking based on the fractal transform, IEEE Multimedia Signal Processing-MMSP (1998), L.A., CA, pp:358-362.
5. Philippe, N. and S. Baudry, 1999. Système temps-réel de tatouage de flux video 4:2:2 et MPEG-2," CORESA 99.
6. Frank, H., P. Eisert and B. Girod, 1998. Digital Watermarking of MPEG-4 Facial Animation Parameters, Computers and Graphics, 22: 3.
7. Michael, A. and Dr. C. Busch, 2003. Watermarking of Audio, Music Scores and 3D Models, CG Topics 2003.
8. Jian-Chyn, L. and S.Y. Chen, 2001. Fast two-layer image watermarking without referring to the original image and watermak, Elsevier, Image and Vision Computing, 19: 1083-1097.
9. Oliver, B., 1999. Geometry-Based Watermarking of 3D Models, IEEE Computer Graphics and Applications, pp: 46-55.
10. Satoshi, K., H. Date and T. Kishinami, 1998. Digital Watermarking for 3D Polygons using Multi-resolution Wavelet Decomposition, Proc. of the sixth IFIP WG 5.2 GEO. 60, Tokyo, Japan, pp: 296-307.
11. Ohbuchi, R., A. Mahaiyama and S. Takahashi, 2002. A Frequency-Domain approach to Watermarking 3D Shapes, Computer Graphics Forum, 21: 373-382.
12. Azuma, R., 1997. A Survey of Augmented Reality. In Presence: Teleoperators and Virtual Environments, 6: 355-385.
13. Azuma, R., Y. Baillot, R. Behringer, S. Feiner, S. Julier and B. MacIntyre, 2001. Recent Advance in Augmented Reality, In Proc. IEEE Computer Graphics and Applications, 21: 34-47.
14. Mel Slater and Anthony Steed and Yiorgos Chrysanthou, 2002. Computer Graphics and Virtual Environments: From Realism to Real-Time, Pearson Education.
15. Amr, A., A. Hilton and F. Mokhtarin, 2002. "Adaptative Compression of Human Animation Data, EUROGRAPHICS 2002.
16. ISO/IEC 14772-1, 1997. Virtual Reality Model Language (VRML), International Standard Organisation (ISO).
17. Mallat, S., 1989. A Theory for Multi-resolution Signal Decomposition: The Wavelet Representation, IEEE Pattern Anal. and Machine Intel., 11: 674-693.
18. Mallat, S., 1998. A Wavelet Tour of Signal Processing, Academic Press.