# Digital Image Watermark Authentication Using DWT-DCT 

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#### Abstract

Multimedia communication is widely used nowadays; it has been used in most of life fields. Great importance has been given to a new art concerns about hiding a secret message inside pictures. The watermarking is as a method of concealing digital information security in the middle of the multimedia data that is the host image. Discrete Wavelet Transform (DWT) when joined together with discrete Cosine Transform (DCT) delivers the powerful digital watermarking image. There are different types of intrusions that either plunder the actual ownership or demolish the appearance. In this study, the DWT-DCT approach has been proposed so as to establish the secure appearance by concealing the watermark inside the actual image and validate the proprietor's image. Using DWT-DCT and low-bit percentage, the watermark image is inserted and abstracted. Results have been displayed based on the hybrid DWT-DCT for excellent capable digital watermarking image. The expected conclusion of this research is a technique that has the ability to hide the secret data (message) inside the image by using DWT to avoid all the different types of attacks and finally extract the secret data from the image. Two techniques has been used to achieve imperceptibility and robustness of the watermark against certain geometric and non-geometric attacks.


key words: Digital image, watermarking, authentication, multimedia, DWT and DCT

## INTRODUCTION

In this work we study the digital watermarking technique, the current proliferation of technology, accessible internet and different image transformation equipment's are susceptible to a large extent, the feasibility of downloading an image from the internet and administering it with the acknowledgement of the actual owner. Hence, validating the image is not only considered as dynamic but also an important research area (Mishra et al., 2014). In a watermarking approach, there are two kinds of algorithms: embedding algorithm and extracting algorithm. The embedding algorithm is a mechanism of fastening the digital data with the watermark which can either be a text or an image. In this mechanism, both the host image and the watermark are considered together and the watermark image is embedded inside the host image, therefore safeguarding the host image. Hence, the inserted image can demolish the features of the actual data. Nevertheless, the abstraction algorithm is a mechanism of abstracting the watermark from the watermarked image which is dissimilar to the host image. Hence, the performance of the watermark image is evaluated on the basis of different
characteristic specifications, for instance, Normalized Correlation (NC), Peak-Signal-to-Noise-Ratio (PSNR), mean square error (Mishra et al., 2014; Lim, 2015).

An advantageous watermarking pattern should captivate the powerfulness and imperceptibility. The first one signifies that the non-cognitive distinctness between the watermarked and the actual report is not noticeable to the human eye. Also, the watermark should not intervene the media that is being safeguarded. Agility highlights that the un-authentic individual should not demolish the watermark nor should make the report not valuable. The watermarks also should be powerful and strong enough to signal execution and intended intrusions. Powerful watermarking has been constructed in a way that is invulnerable against intrusions for instance, noise, cropping, filtering etc. that aim to erase or demolish the watermark apart from deteriorating the viewable feature of the watermarked image considerably. In this manner, it is utilized to safeguard and ascertain the authorship. On contrary, breakable watermarking is introduced to guarantee the adherence and image authorization instead of validating the real ownership. It discovers un-authentic amendment which will either destroy or change the watermark. Semi delicate watermarking integrates the

[^0]characteristics of both delicate and powerful watermarking so as to discover un-authentic handling while still being powerful and resistant against authentic handling. The most vital operation for watermarking is the preserving of electronic information ownership authorization. Electronic watermarking supports in the verification of the ownership authorization of the presented image. For frequency realm watermarking, values of precise densities are altered from their actual two distinct arrangement (Cox et al., 1997).

Typically in electronic image watermarking, an individual value of the scaling determinant is utilized to introduce the watermark in the complete host image. The local allocation of the actual image is not acknowledged during the introduction process. Nevertheless, this kind of introduction can direct to some unwanted naked relics inside watermarked image (Cox et al., 1997; Li et al., 2007; Waleed et al., 2014). These distortions are recorded mainly in sleek domains because these domains are susceptible to sounds. To lessen these distortions, the scaling determinant should be reduced in the plain domains, therefore influencing the powerfulness of the introduced process. In other domains, enhancing the scaling determinant above a definite margin can cause naked disruptions inside the marked image. Choosing scaling determinant has become an important concern of agreement between imperceptibility and powerfulness (Cox et al., 1997) has induced that an individual scaling determinant may not be suitable for disturbing all the coefficients of cover image as various illusory factors may display additional or smaller strength to alteration. Digital watermarking mechanism come under spatial and frequency category depending upon the class in which they are used for introducing the watermark. Spatial category watermark alters the pixels of one or two unplanned chosen subsets of images (Waleed et al., 2014). This kind of mechanism proves powerless across average image processing and intrusions such as sound, filtering, compression which might be demolished with less effort by disruption (Waleed et al., 2014). The deformities caused by damaged image compression, signal processing function and other intrusions are the average difficulties faced during the utilization and allocation of watermarked image. Therefore, a powerful watermarked image is needed to form support across image deformities of enduring intrusions (Zhang et al., 2011). Frequency category is also recognized as transform category for instance, Discrete Wavelet Transform (DWT), Discrete Cosine Transform (DCT), Discrete Fourier Transform (DFT) and Singular Valued Decomposition (SVD) are some of the ordinary categories being introduced (Waleed et al., 2014; Shensa, 1992).

These categories can be joined together to enhance the efficiency of the frequency category and the powerfulness under the intrusions. Still ordinary research on image watermarking has restricted its analysis to the utilization of accepted mathematical creations for example DCT, DWT and some other composite variants for example DWT-DWT and DWT-DCT. In this study, we highlight the efficiency of hybrid watermarking mechanism for the two joint methods: DWT-DCT and DWT-DWT.

## Literature review

Discrete Wavelet Transform (DWT) and Discrete Cosine Transform DCT: Discrete Wavelet Transform (DWT) is a mechanism that is utilized in uncontrolled watermarking mechanism and collateral to transform region watermarking. Wavelet based watermarking is a well-known domain due to its potential against vulnerable intrusions (Gupta and Shrivastva, 2010). DWT partitions the signal in two dimensions: high frequency and low frequency(Dharwadkar and Amberker, 2010; Lim, 2015). A signal is made to pass in between the high pass filter and then access low pass filter to examine the low frequency filter. Outcome from the high and low pass filters deliver DWT coefficients that are employed on the modified real image, acknowledged as Inverse Discrete Wavelet Transform (IDWT) (Karniawan and Purnama). Typically, the introduction of watermark inside the image is gained by contemplating the DWT coefficients of the disintegrated image with the coefficients that have the sufficient area suitable enough for the introduction of the watermark. Kumar et al. (2012) Suggested against the intrusion categories so as to ignore image deformities created by intrusions and the utilization of sub band coefficients may alter it by channel sound. According to Gupta and Shrivastva (2010), correlation coefficient values do not get enhanced amid the actual watermarking and the extorted watermarked.

DCT is a well-known mutation function that alters a signal from the spatial to the frequency realm and so far it has been utilized in the JPEG class for the abstraction of image due to its efficiency. It alters actual data into the actual spectrum ignoring the difficulties of repetition. The well-known block dependent DCT alters the segments into un-stretched blocks and employs the DCT to every individual block.

DCT and DWT (Shefali et al., 2008; Lal et al., 2015) alterations, so far have been widely used in profuse digital signal processing functions. Discrete cosine transform is a mechanism for altering a signal into basic frequency categories (Dharwadkar and Amberker, 2010; Migdadi et al., 2015). An image is highlighted as an
average of sinusoids of different densities and weights. ' $x$ ' which is being utilized as an input image, DCT coefficients for the altered output image ' $y$ ' are calculated according to Eq. 1 as represented below. In the given equation, ' $x$ ' is an input image of $N \times M$ pixels and $x(m, n)$ is the strength of the pixel in row $m$ and column $n$ of the image while $y(u, v)$ signifies the DCT coefficient in row $u$ and column $v$ of the DCT matrix.

$$
\begin{align*}
y(u, v) & =\sqrt{\frac{2}{M}} \sqrt{\frac{2}{N}} \alpha_{u} \alpha_{v} \sum_{u=0}^{M-1} \sum_{v=0}^{\mathrm{N}-1} \\
& x(\mathrm{~m}, \mathrm{n}) \cos \frac{(2 \mathrm{~m}+1) \mathrm{u} \Pi}{2 \mathrm{M}}  \tag{1}\\
& \cos \frac{(2 \mathrm{n}+1) \mathrm{v} \Pi}{2 \mathrm{~N}}
\end{align*}
$$

Where:

$$
\begin{aligned}
& \alpha_{u}= \begin{cases}\frac{1}{\sqrt{2}} & u=0, \mathrm{u}=1,2, \ldots, \mathrm{~N}-1 \\
1\end{cases} \\
& \alpha_{\mathrm{v}}= \begin{cases}\frac{1}{\sqrt{2}} & \mathrm{v}=0, \mathrm{v}=1,2, \ldots, \mathrm{~N}-1 \\
1\end{cases}
\end{aligned}
$$

The image is reorganized by employing opposite DCT application according to the given equation:

$$
\begin{array}{r}
x(m, n)=\sqrt{\frac{2}{M}} \sqrt{\frac{2}{N}} \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} \alpha_{u} \alpha_{v} y(u, v)  \tag{2}\\
\cos \frac{(2 m+1) u \Pi}{2 M} \cos \frac{(2 n+1) v \Pi}{2 N}
\end{array}
$$

A hybrid DWT-DCT approach watermarking domain for the utilization of the mother wavelet, the legibility and imperceptibility of the abstracted/introduced watermark and the image feature indicator for every wavelet family. The host image is disintegrated into four sub-bands and the sub-band LH2/HL2 is selected which employ DWT to every single sub-band and introduce individual watermark value in these sub-bands. In one of the research works (Kumar et al., 2012), the introduction mechanism in the Horizontal (HL) deliver efficient outcome then the vertical sub-band (LH). In another research study (Shefali et al., 2008; Mohamed and El-Mohandes, 2012) researchers employed orthogonal two-fold realm of DCT and DWT alteration and utilized the image characteristics to organize the watermark but the clipping and circulation create maximum disintegration. Furthermore (Lim, 2015; Migdadi et al., 2015) utilized a tremendous frequency to the introduced watermark image dependent on DCT-DWT. The outcome delivered efficient capacity for some ordinary image processing applications.

## MATERIALS AND METHODS

The grey scale watermark image with possessing the dimensions $50 \times 20$ will be hidden inside a grey scale cover image with dimensions $512 \times 512$ with the watermark image, that is the message is the wavelet. Haar level 2 is condensed and then it is introduced in the bits of the cover image. The watermark image is the altered wavelet Haar level 2. The distinct coefficients of the altered wavelet are counted into 3 bits each where there are actually 8 bits. At the same time, the grey scale watermark image may be concealed inside the points of the original cover image. The introduced action is done by concealing a piece of a sector where concealing every section of the grey scale watermark image inside the cover image sector is done (Mohamed and El-Mohandes, 2012; Lal et al., 2015).

Figure 1 displays the flowchart of the complete methodology used in this study. On the left side it displays the watermark infusion and on the right side watermark abstraction after employing the intrusion adjacent to the watermarked image.

## Algorithm

Algorithm 1: The proposed algorithm for the introduction of watermark has been displayed in the Fig. 1 with the comprehensive explanation as follows: Step 1: DWT is utilized to partition the grey scale cover image into four orthogonal multi- determined sub bands: LL1, HL1, LH1 and HH1. LH1 is selected for the later step. DWT isolates an image into under determined matching image (LL) and horizontal (HL), vertical (LH) and diagonal ( HH ) categories.
Step 2: DWT is once again utilized to partition the sub bad LH1 and acquire minor four sub bands at lower stage and by selecting LH2 sub band. It is vital to observe that another sub band can be selected advancing to various outcomes.
Step 3: LH2 is partitioned into $4 \times 4$ regions.
Step 4: Considering DWT-DCT algorithm, DCT is utilized at each region in the appointed sub band. Step 5: Watermark is constructed into units and zeros. Step 6: Pair of distinct un-correlated series are produced. The initial series has been utilized to introduce the watermark bit 0 ( $\mathrm{PN} \_0$ ) and the other series has been utilized to introduce the watermark bit 1 (PN_1). Total components in every paired pseudorandom series must be identical to the total mid band components of the DCT altered partitions.
Step 7: Pair produced un-correlated pseudorandom series, PN_0 and PN_1 are joined with the support of progressed determinant k , in the DCT altered $4 \times 4$ regions that has been the applicants from the DWT subbands of the grey scale cover image. Introduction mechanism is observed in the centre of the DCT coefficients. If it is considered that $D$ is the matrix in the centre of DCT coefficients, then the concealed action can be displayed as:
If watermark bit is 0 then:

$$
\begin{equation*}
\mathrm{D}^{\prime}=\mathrm{D}+\mathrm{k} \text { *PN_0 } \tag{3}
\end{equation*}
$$

where k is a key
Else,
If watermark bit is 1 then:
$\mathrm{D}^{\prime}=\mathrm{D}+\mathrm{k}$ *PN_1
Step 8: By employing converse DCT and DWT, the watermarked image is re-organized

Watermark extraction: The ownership can be identified from the actual image when some power demands the abstraction of the watermark image and search the real


Fig. 1: Methodology flowcharts
owner of the image. In this condition we demand the utilization of the wavelet transform mechanism for instance, DWT and DWT-DCT. The mechanism can be utilized to abstract the watermark as:

## Algorithm 2:

Step 1: The assaulted image is further disintegrated into four orthogonal multi determinant sub bands that is LL1, HL1, LH1 and HH1 by employing DWT.
Step 2: After employing DWT one more time to LH1 so as to collect limited four sub bands than the initial one and select the sub band LH2.
Step 3: LH2 is further partitioned into 4 x 4 regions.
Step 4: DCT alteration is executed in every region in the sub-band LH2 and abstracting the centred band coefficients of each region.
Step 5: Un-identical paired uncorrelated pseudorandom series are produced one more time. Total number of components in every paired pseudorandom series must be same to the number of mid-band components of the DCT altered DWT sub bands. Reproducing the paired pseudorandom series, PN_0 and PN_1 are utilized using the same source that was utilized in the introduction of the watermark mechanism initially.
Step 6: For every region in sub band LH2, the correlation in the middle of the centred-band coefficients and the pair produced pseudorandom series, PN_1 and PN_0 is determined. If the correlation with the PN_0 is advanced than the correlation with PN_1 then the
abstracted watermark bit is regarded as 0 else 1.
Step 7: Retrieving the watermark by the utilization of the abstracted bits and calculating the strength of the algorithm by evaluating the
correlation amid actual watermark and the abstracted one.

## RESULTS AND DISCUSSION

The imperceptibility and robustness watermarking: The proposed algorithm has been employed on $512 \times 512$ cover image. After that it has been employed on $50 \times 20$ grey scale image with the 'copyright' watermark written inside. It will be displayed that the algorithm is powerful against intrusions such as Gaussian sound, circulation, abridgement which are not very often utilized in real life but are classic and typical. Some of the intrusions such as Gaussian sound are disgraceful while others such as cropping are biased numerical intrusions. Still some others are watermark elimination which aids to measure the
correlation between the actual grey scale watermark and the abstracted grey scale watermark from the invaded grey scale cover image. Using the operation, PSNR can be measured as:

$$
\begin{gather*}
\mathrm{PSNR}=10 \cdot \log _{10}\left(\frac{\mathrm{MAX}^{2}}{\mathrm{MSE}}\right)  \tag{5}\\
\text { PSNR }=20 \cdot \log _{10}\left(\frac{\mathrm{MAX}_{\mathrm{I}} \text { pixel value }}{\sqrt{\mathrm{MSE}}}\right)
\end{gather*}
$$

Where the Mean Square Error (MSE) is the aggregate squared error amid the altered and the actual image. PSNR is a measure of the peak error whereas MAX is the value of highest pixel. Correlation $\rho$ can be acquired as:

$$
\begin{equation*}
P(\hat{W})=\frac{\sum_{i=1}^{N} i \hat{w} i}{\sqrt{\sum_{i=1}^{N}{ }^{2}} \sqrt{\sum_{i=1}^{N} \hat{w}_{i}^{2}}} \tag{6}
\end{equation*}
$$

Where $\rho$ is the correlation of the introduced watermark w and abstracted watermark w and N is the measure of the watermark image. By using DWT- DCT transform, the algorithm recorded a better value of PSNR comparing with DWT only. The capability of an algorithm of storing the cover image non-fuzzy is acknowledged as imperceptibility of the algorithm measured by the utilization of peak signal to noise ratio (PSNR). Figure 2 displays the actual image, watermark and the original image plus watermark using DWT-DCT.

After frequent repetitions, the algorithm displays efficient strength across this type of intrusion. Attack factor signifies the extent to which the attack occurs or else it indicates the extent to which the attack affects the watermark image. Correlation signifies the correlation of the watermark initialli, in the very beginning when the outbreak is launched and afterwards thus, analyzing the strength of the algorithm. Correlation operation measures the correlation value in comparison with the threshold value. Utilizing the threshold value, image is regarded watermarked if the correlation value transcends threshold value. From Table 1 and the analysis for the result in Fig. 2 show the results, correlation values of embeded and extracted watermark show clearly that the performance of DWT_DCT is better than DWT against Gaussian noise. On the other hand, correlation values of the rotation attack shows great degradation. This degradation is not due to the lack of capability of the
J. Eng. Applied Sci., 11 (Special Issue 2): 3227-3232, 2016


Fig. 2: The imperceptibility images for original image + watermark by using DWT-DCT

Table 1: Displays the outcome for robustness analysis of DWT-DCT algorithm

| Type of attacks | Attacks factor | Correlation (Leena) | Correlation (Papper) | $\begin{gathered} \text { Correlation } \\ \text { (Man) } \\ \hline \end{gathered}$ | Extracted watermark using DWT-DCT |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Gaussian filter | 1.0 | 0.7300 | 0.730 | 1.000 | Copyright |
|  | 2.0 | 0.7100 | 0.707 | 0.990 | odryight |
|  | 3.0 | 0.7090 | 0.700 | 0.980 | oripright |
|  | 5.0 | 0.7060 | 0.690 | 0.580 | Bonjright: |
| Gaussian noise | 0.1 | 0.7300 | 0.700 | 0.100 |  |
|  | 0.3 | 0.6500 | 0.690 | 0.920 |  |
|  | 0.5 | 0.6400 | 0.450 | 0.570 |  |
|  | 0.7 | 0.3500 | 0.400 | 0.410 | yxatian |
| Rotation | 35.0 | -0.0140 | 0.026 | 0.045 |  |
|  | 60.0 | -0.0200 | 0.011 | 0.036 |  |


| Type of attacks | Attacks factor | Correlation (Leena) | Correlation (Papper) | Correlation (Man) | Extracted watermark using DWT-DCT |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 90.0 | -0.0200 | 0.006 | -0.090 | arong |
|  | 180.0 | -0.0200 | -0.024 | -0.030 |  |
| Median filtter | 1.0 | 0.7300 | 0.730 | 0.980 |  |
|  | 2.0 | 0.2900 | 0.260 | 0.520 | $\%$ |
|  | 3.0 | 0.2200 | 0.210 | 0.490 |  |
|  | 5.0 | 0.0160 | 0.070 | 0.170 |  |
| Gaussian noise | 0.1 | 0.7000 | 0.600 | 0.900 |  |
|  | 0.2 | 0.7000 | 0.510 | 0.720 |  |
|  | 0.3 | 0.6400 | 0.310 | 0.490 |  |
|  | 0.5 | 0.5200 | 0.150 | 0.270 |  |
| Rotation | 1.0 | 0.0100 | 0.030 | 0.020 |  |
|  | 2.0 | 0.0060 | 0.026 | 0.025 |  |
|  | 3.0 | -0.0060 | -0.040 | -0.090 |  |
|  | 5.0 | -0.0200 | -0.034 | -0.017 |  |

algorithm but comes from the fact that the watermark values has been moved due to the change of the values position through rotation nature. DWT-DCT algorithm breakdown the frequencies into high and low frequency and considers the medium image frequency. DWT-DCT encompasses the criterion that frequency transform is used on a large scale in image compression. Table 1 displays the outcome for powerful analysis of DWT-DCT algorithm counter to Gaussian sound intrusion. Delivered outcome displays better advancement correlation of abstracted and introduced watermarks in comparison with DWT.

## CONCLUSION

Through the utilization of DWT and DWT-DCT the powerful digital image watermark technique has been
employed with the huge capability of watermark information of actual image. The constructed algorithm is associated with the watermark and by the utilization of DWT and DWT-DCT to maintain ownership privilege by concealing ownership image in another image and safeguard it. Introduction and the abstraction by the utilization of DWT-DCT is efficient than introducing by the utilization of DWT because DWT-DCT breakdown borderline densities. Medium densities of images are considered and DWT-DCT incorporate the reality that the altered frequency is utilized on a large scale in image compression. Watermark image can be abstracted when employing various types of intrusions. Hence, the application of the wavelet classification and execution of Haar transform are effective in sightless and invisible watermark. Assessment of the proposed algorithm, correlation values of the introduced and the abstracted watermark apparently display the efficiency of digital wavelet transform adjacent to dithering. In comparison, correlation values of circulation intrusion display distinct detereoration which does not take place due to the deficiency of the ability of the algorithm bu due to the modifying atitude of the watermark values. The future work, Harmony search and Bat algorithm are examples of Nature Inspired Algorithm that at the moment have not been applied to the optimization of digital image watermarking techniques.

## ACKNOWLEDGEMENTS

The researchers wish to thank Universiti Kebangsaan Malaysia (UKM) and Ministry of Higher Education, Malaysia for supporting this work by research grants DIP-2014-018 andFRGS/1/2014/ICT07/UKM/02/2.

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