

Simulation 3-DOF RRR Robotic Manipulator under PID Controller

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Abstract: A robotics manipulator system is a multi-link mechanical system each link is driven by an electrical actuator individually. Most industry application uses robotics system, this system needs to be controlled efficiently. In this study, 3-DOF serial robotic manipulator is simulated with a PID controller by using MATLAB\Simulink. The PID controller is proposed for every single manipulator where each manipulator is controlled independently. The performance of the 3-DOF robotic arm for trajectory tracking studies under this controller with different trajectory and without/with external disturbance torque.

Key words: Robot arm, robotics manipulator, 3-DOF, PID, MIMO PID controller, torque

INTRODUCTION

Robotics manipulator can be classified in many categories such as application, type of link connection, number of Degree of Freedom (DOF), type of link motion and shape of the workspace and so on.

The 3-DOF serial (RRR) robotics manipulator can be used in many industry process like pick and place and painting. Various kind of robotic arms are designed according to the type of movement but the controller design is very important as mechanical part design. Many researches are available in the related literature to design controllers like PD or PID (Yamacli and Canbolat, 2008), neural network (Horowitz *et al.*, 1991), fuzzy logic algorithm (Lewis *et al.*, 1993) and artificial intelligence (Golnazarian, 1995; Jungbeck and Madrid, 2001).

In this study, a 3-DOF serial RRR robotics arm under its controller is simulated by using MATLAB/Simulink then the performance of controlled robot with adaptive PID controller will be discussed.

MATERIALS AND METHODS

Configuration of 3-DOF robotics arm: The configuration of the serial 3-DOF robotics manipulator is shown in Fig. 1.

To find the kinematic equation of the manipulator, the Denavit Hartenberg (DH) notation (Craig, 2005; Corke, 2007; Wang *et al.*, 2014) will be used. The parameters of 3R robotics arm is shown in the Table 1. The transformation matrix for each link will be (Guo *et al.*, 2015; Lloyd and Hayward, 1988):

$$T_1^0 = \begin{bmatrix} C_1 & -S_1 & 0 & 0 \\ S_1 & C_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (1)$$

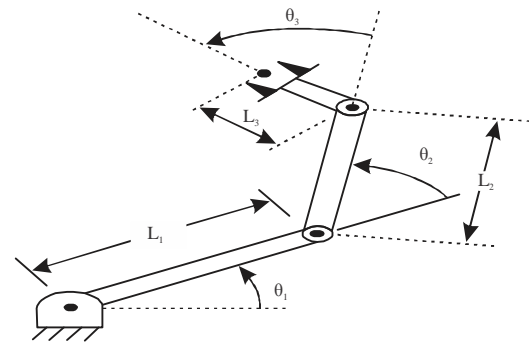


Fig. 1: 3-DOF RRR robotics arm

Table 1: DH parameters for 3R robotics arm

i	α_{i-1}	a_{i-1}	d_i	θ_i
1	0	0	0	θ_1
2	0	L_1	0	θ_2
3	0	L_2	0	θ_3
4	0	L_3	0	0

$$T_2^1 = \begin{bmatrix} C_2 & -S_2 & 0 & L_1 \\ S_2 & C_2 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (2)$$

$$T_3^2 = \begin{bmatrix} C_3 & -S_3 & 0 & L_2 \\ S_3 & C_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (3)$$

$$T_4^3 = \begin{bmatrix} 1 & 0 & 0 & L_3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (4)$$

The transformation matrix of the end effector relative to the base will be (Liu *et al.*, 2017; Cui *et al.*, 2010):

$$T_0^4 = \begin{bmatrix} C_{123} & -S_{123} & 0 & L_3C_{123}+L_2C_{12}+L_1C_1 \\ S_{123} & C_{123} & 0 & L_3S_{123}+L_2S_{12}+L_1S_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (5)$$

The Lagrangian dynamic formulation (White *et al.*, 1989; Yu *et al.*, 2015) provides a means of deriving the equations of motion from a scalar function called the Lagrangian which is defined as the difference between the kinetic and potential energy of a mechanical system. The Lagrangian of a manipulator is:

$$E(\theta, \dot{\theta}) = k(\theta, \dot{\theta}) - u(\theta) \quad (6)$$

$$k(\theta, \dot{\theta}) = \frac{1}{2} m^* v_c^2(\theta, \dot{\theta}) \quad (7)$$

The equations of motion for the manipulator are then given by:

$$\tau_i = \frac{\partial E}{\partial \dot{\theta}_i} - \frac{\partial E}{\partial \theta_i} \quad (8)$$

where, τ is the $n \times 1$ vector of actuator torques:

$$\tau_i = \frac{d}{dt} \left(\frac{\partial k}{\partial \dot{\theta}_i} \right) - \frac{\partial k}{\partial \theta_i} + \frac{\partial u}{\partial \theta_i} \quad (9)$$

$$\tau = M(\theta)\ddot{\theta} + V(\theta, \dot{\theta}) + G(\theta) \quad (10)$$

Where:

- $M(\theta)$: Then 3×3 mass matrix of the manipulator
- $V(\theta, \dot{\theta})$: 3×1 vector of centrifugal and Coriolis terms
- $G(\theta)$: 3×1 vector of gravity terms

The term state-space equation will be used because the term $V(\theta, \dot{\theta})$ appearing in Eq. 10 has both position and velocity dependence (Guo *et al.*, 2015).

Each element of $M(\theta)$ and $G(\theta)$ is a complex function that depends on θ , the position of all the joints of the manipulator. Each element of $V(\theta, \dot{\theta})$ is a complex function of both θ and $\dot{\theta}$. Table 2 present the simulation parameters of the robot manipulator.

PID controller: Generally, a PID controller of each joint controlled independently is given with the formula (Goldman, 1983; Astrom and Hagglund, 1995; Han *et al.*, 2014). The PID controller is most used in

Table 2: Robot parameters

Parameters	Link 1	Link 2	Link 3
Mass (kg)	0.30	0.25	0.15
Length (m)	0.25	0.20	0.15
Moment of inertia (kgm ²)	0.02	0.02	0.02

Table 3: Parameters of PID controllers

Variables	Link 1	Link 2	Link 3
K_p	18.00	18.5	19.50
K_i	49.00	50.0	49.88
K_d	2.51	2.0	2.70

control system. The main and important advantage of PID controller is its feasibility and easy to be implemented. The main equation of PID controller is (Ang *et al.*, 2005; Bingul, 2004; Allaoua *et al.*, 2010; Wang *et al.*, 2006):

$$\tau_i(t) = K_{Pi} e_i(t) + K_d \frac{de_i(t)}{dt} + \frac{1}{K_i} \int e_i(t) dt \quad (11)$$

Where:

- $e(t)$: The error function
- K_p : The proportional control coefficient which providing control proportional to the error
- K_d : The derivative control coefficient which used to improve transient response
- K_i : The integral control coefficient used to reduce the steady state errors

The PID parameters are given as shown in Table 3.

RESULTS AND DISCUSSION

Simulation models of 3-DOF robotics manipulator with PID controller and results: Dynamic of the 3-DOF robotics arm with PID controller simulated by MATLAB\Simulink Fig. 2. The response will be under PID controller with different desired angles and without/with disturbance.

Trajectory performance, torque performance and position error are discussed in PID controllers. Figure 3 and 4 shows the link angles and the link angle errors with PID controller, respectively for step trajectories and without disturbance.

Assume the external disturbance torques as shown in Fig. 5. Figure 6 shows the response of the all links when the external disturbance is applied.

So, the error in the position of all links of the robotics manipulator will be as Fig. 7. When the desired angle of the three links of the robotics arm is sine wave, the response of these links will be as Fig. 8.

The error of the trajectory when the desired angles sine waves assume there is no disturbance torque shown in Fig. 9.

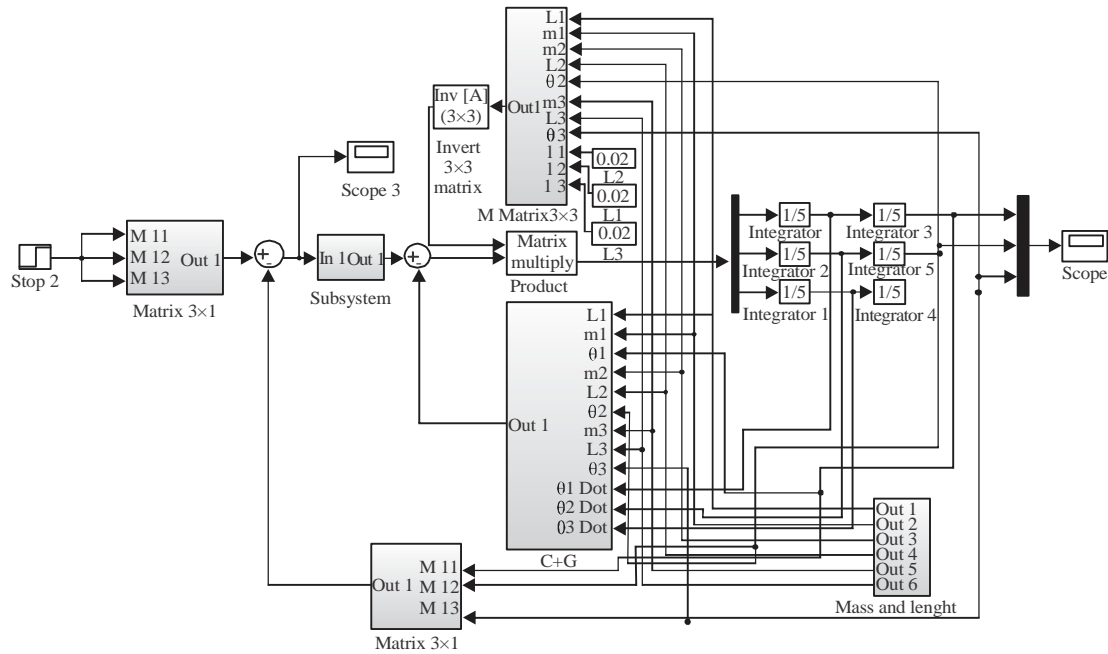


Fig. 2 Simulink model of 3-DOF robotics arm

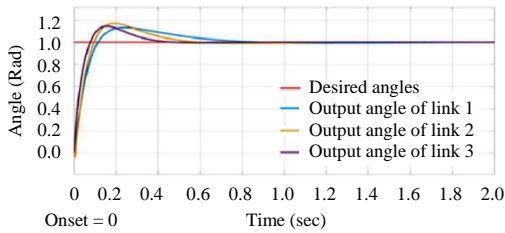


Fig. 3: Link angles of 3-DOF robotics arm

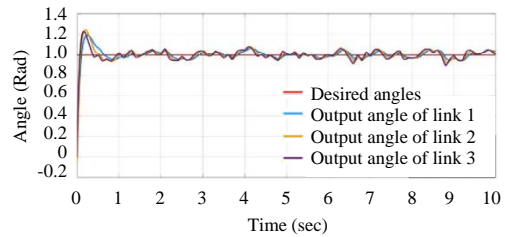


Fig. 6: Response of the all links when the external disturbance is applied

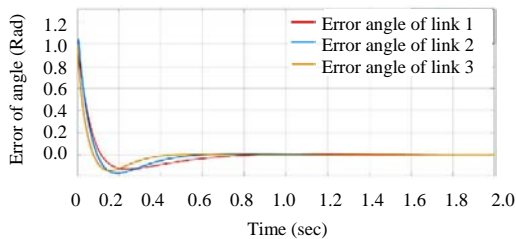


Fig. 4: Link angles error of 3-DOF robotics arm

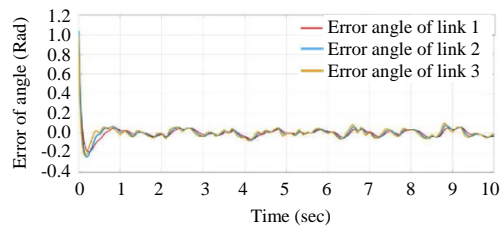


Fig. 7: Error in the position

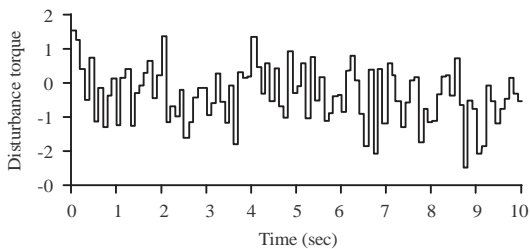


Fig. 5: External disturbance torques

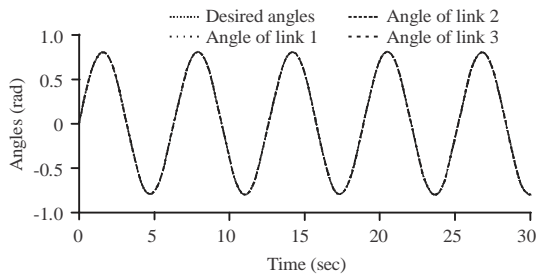


Fig. 8: Response of all links for desired sine angles

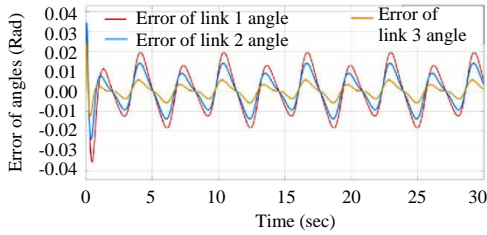


Fig. 9: Error of the trajectory

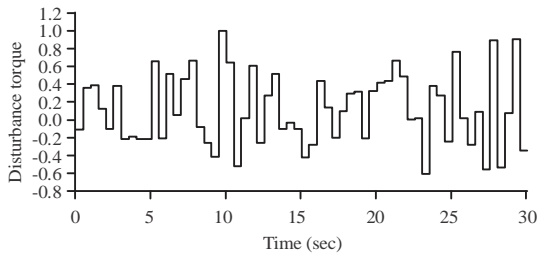


Fig. 10: External disturbance torques

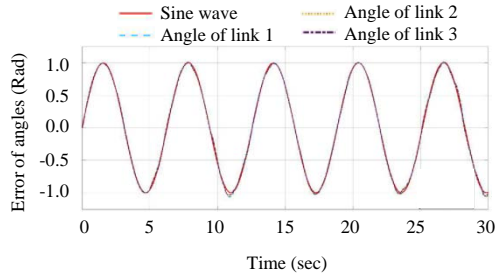


Fig. 11: The response for sine wave desired angles with external disturbance

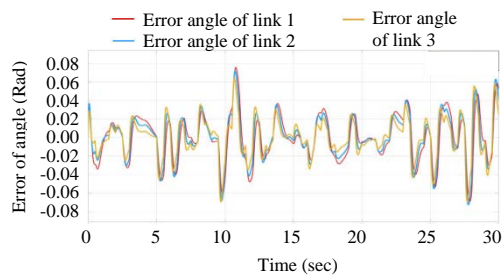


Fig. 12: Error of all links position with external disturbance

If the disturbance as Fig. 10 will be applied, the response of all three links will be as Fig. 11 and the error in angles of links will be as Fig. 12.

Figure 11 shows the response of these links when the desired angle of the three links of the robotics arm is sine wave. The error of all links position of the robotics manipulator after the external disturbance applied will be as Fig. 7.

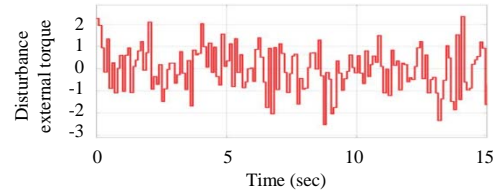


Fig. 13: External disturbance torque with different desired angle

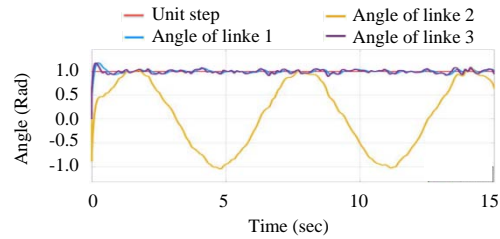


Fig. 14: Link angles with different desired angle and with external disturbance

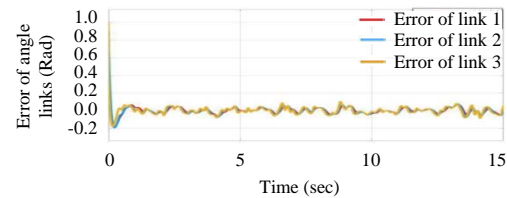


Fig. 15: Error of link angles with different desired angle

Table 4: Maximum error response

Desired angle	Max. disturbance	Link 1	Link 2	Link 3
Unit step	0.150	0.180	0.175
Unit step	-2 to 2	0.19	0.220	0.210
Sinusoidal	0.035	0.025	0.013
Sinusoidal	-0.75 to 1.1	0.075	0.075	0.075
Unit step+sinusoidal	0.120	0.140	0.130
Unit step+sinusoidal	-2.5 to 2.5	0.170	0.190	0.170

Figure 13 shows the external disturbance when the desired angle of the first and third link as a unit step and the desired angle of the second link as sine wave angle, the response will be as shown in Fig. 14.

The error of the angle of links when the desired angles are different and with external disturbance will be as shown in Fig. 15.

The response for desired angles (unit step, sinusoidal, unit step and sinusoidal) represented with/without external disturbance torque. The maximum error of each link in each case is shown in Table 4.

CONCLUSION

The robotics manipulators became very important and used widely in industry, thus, the study and control of the joints is very vital. In this study, the

analysis of 3-DOF robotic arm has done and the dynamic equations has been represented by using Lagrangian dynamic formulation. Beside the dynamic model has been simulated by using MATLAB/Simulink and controlled by PID controller. The response of all links of 3-DOF robotics manipulator under the PID controller is represented when the desired angles be: unit step, sinusoidal and unit step and sinusoidal.

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