

## Tank Liquid Level Control using NARMA-L2 and MPC Controllers

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**Abstract:** Liquid level control is highly important in industrial applications such as boilers in nuclear power plants. In this study, a simple liquid level tank is designed based on NARMA-L2 and model predictive control controllers. The simple water level tank has one input, liquid flow inn and one output, liquid level. The proposed controllers is compared in MATLAB and then simulated in simulink to test how the system actual liquid level track the desired liquid level with two input desired signals (step and white noise). The response of the NARMA-L2 controller is then compared with a MPC controller. The results are shown sequentially and the effectiveness of the controller is illustrated.

### INTRODUCTION

In many industrial processes, control of liquid level is required. It was reported that about 25% of emergency shutdowns in the nuclear power plant are caused by poor control of the steam generator water level. Such shutdowns greatly decrease the plant availability and must be minimized. Water level control system is a very complex system because of the nonlinearities and uncertainties of a system. Currently, constant gain PI controllers are used in nuclear organizations for boiler water level control at high power operations. However, at low power operations, PI controllers cannot maintain water level properly. A need for performance improvement in existing water level regulators is therefore needed<sup>[1]</sup>.

### MATERIALS AND METHODS

**Mathematical modeling of the tank:** Consider a tank with cross sectional area  $A$ , liquid level height  $h$  with fluid resistance  $R$ , density  $\rho$ , volume flow in  $q_i$  and volume flow out  $q_o$  as shown in Fig. 1.

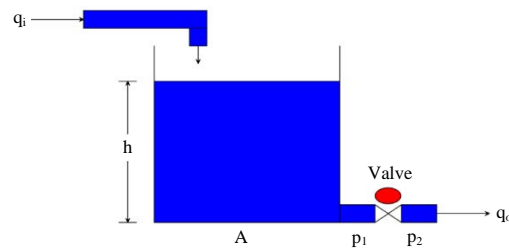


Fig. 1: Water level tank system

Since,  $q_i$  and  $q_o$  are the inflow and outflow, respectively and  $V$  is the volume of the fluid inside the tank, we can write:

$$\frac{dV}{dt} = \frac{d}{dt}(\rho Ah) = \rho q_i - \rho q_o \quad (1)$$

The mass flow out can be expressed in terms of  $h$ . assume a linear model, the exit orifice resistance of the valve will be:

$$\rho q_o = \frac{\Delta p}{R} \quad (2)$$

Table 1: Parameters of the tank

Parameters	Symbols	Values
Area	A	2 (m <sup>2</sup> )
Density	ρ	1 (kg m <sup>-3</sup> )
Gravity	G	10 (m sec <sup>-2</sup> )
Resistance	R	0.05 (s m <sup>-2</sup> )

Table 2: NARMA L-2 parameters

Network architecture			
Variables	Values	Variables	Values
Size of hidden layer	8	Delayed plant input	3
Sample interval(sec)	0.01	Delayed plant output	3
Training data			
Training sample	80	Maximum plant output	1
Maximum Plant input	2	Minimum plant output	2
Minimum Plant input	1	Max interval value (sec)	3
Min interval value (sec)	-	-	1
Training parameters			
Training epochs	-	-	80

$$\rho q_o = \frac{\Delta p}{R} = \frac{p_1 - p_2}{R} = \frac{\rho gh}{R} \quad (3)$$

Assuming constant density, substituting Eq. (3) in to Eq. (1) yields:

$$\rho A \frac{dh}{dt} = \rho q_i - \frac{\rho gh}{R} \quad (4)$$

Taking Laplace transform of Eq. (4), the transfer function becomes:

$$\frac{H(s)}{Q_i(s)} = \frac{A^{-1}}{s + \frac{g}{RA}} \quad (5)$$

The parameters of the tank is shown in Table 1. The numerical value of the system transfer function is:

$$\frac{H(s)}{Q_i(s)} = \frac{0.5}{s + 100}$$

**The proposed controllers**

**NARMA-L2 control:** The neural network controller described in this section is referred to by two different names: feedback linearization control and NARMAL2 control. It is referred to as feedback linearization when the plant model has a particular form (companion form) 24. It is referred to as NARMA-L2 control when the plant model can be approximated by the same form. The central idea of this type of control is to transform nonlinear system dynamics into linear dynamics by canceling the nonlinearities. This section begins by presenting the companion form system model and demonstrating how a neural network can be used to identify this model. Then it describes how the identified neural network model can be used to develop a controller. Table 2 illustrates the network architecture, training data and training parameters<sup>[2]</sup>.

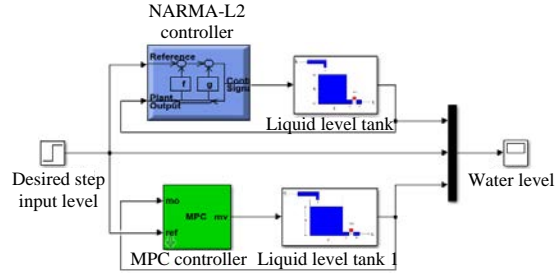


Fig. 2: Simulink model of the tank with the proposed controllers for tracking a desired step input signal

**MPC control:** The MPC Controller block receives the current measured output signal (mo), reference signal (ref) and optional measured disturbance signal (md). The block computes the optimal manipulated variables (mv) by solving a Quadratic Program (QP) (Fig. 2)<sup>[3]</sup>.

**RESULTS AND DISCUSSION**

In this study, the comparison of the tank with the proposed controllers for tracking the desired level of the tank using step and white noise desired input signals in order to analyze which controller shows a better performance for the system with the help of MATLAB/Simulink software<sup>[4]</sup>.

**Comparison of the tank with NARMA-L2 and MPC controllers for tracking a desired step input:** The Simulink model of the tank with the proposed controllers for tracking a desired step input signal is shown in Fig. 2<sup>[5]</sup>.

The simulation result of the tank with the proposed controllers for tracking a desired step input signal is shown in Fig. 3.

The tank system with the proposed controllers Performance specification is shown in Table 3. As we seen from Table 3 that, the tank system with NARMA-L2 controller have better performance in all the criteria chosen.

**Comparison of the tank with NARMA-L2 and MPC controllers for tracking a desired white noise input:** The simulink model of the tank with the proposed controllers for tracking a desired white noise input signal is shown in Fig. 4.

The simulation result of the tank with the proposed controllers for tracking a desired white noise input signal is shown in Fig. 5.

The tank system with the proposed controller's performance specification is shown in Table 4. As we seen from Table 4 that, the tank system with NARMA-L2 controller have almost the same rise time, peak value and low value as the tracked white noise input signal<sup>[6]</sup>.

Table 3: Performance measurement of a step response

Performance measure	NARMA-L2	MPC
Rise time	0.009259 (sec)	0.011269
Percentage overshoot	6.989 (%)	25.949 (%)
Settling time	0.145 (sec)	0.22 (sec)
Peak value	0.5358 (m)	0.6327 (m)

Table 4: Performance measurement of a white noise response

Performance measure	NARMA-L2	MPC	White noise
Rise time	0.057214 (sec)	0.0031578 (sec)	0.049729 (sec)
Percentage overshoot	88.450 (%)	92.113 (%)	105.531 (%)
Peak value	$1.851 \times 10^{-3}$ (m)	$1.589 \times 10^{-3}$ (m)	$1.875 \times 10^{-3}$ (m)
Low value	$2.529 \times 10^{-7}$ (m)	$1.973 \times 10^{-4}$ (m)	$2.524 \times 10^{-7}$ (m)

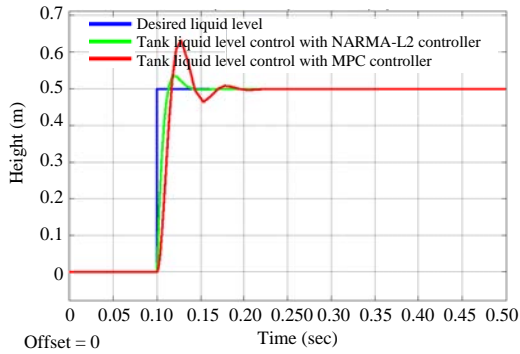


Fig. 3: Simulation result of the tank level for a step input signal

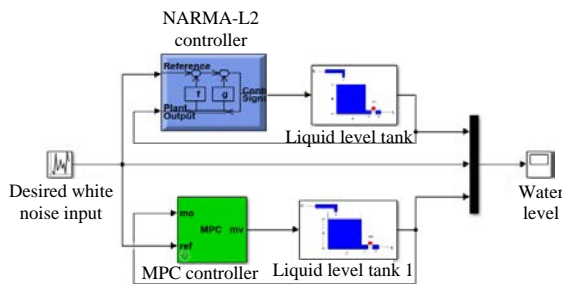


Fig. 4: Simulink model of the tank with the proposed controllers for tracking a desired white noise input signal

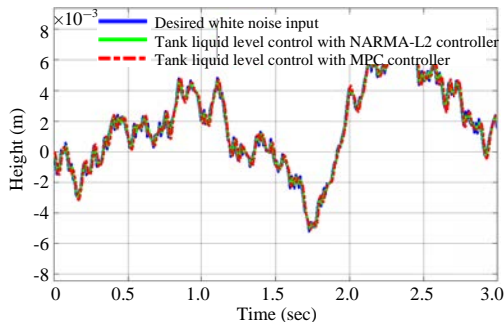


Fig. 5: Simulation result of the tank level for a white noise input signal

## CONCLUSION

The liquid level tank system is designed and tested using MATLAB/Simulink software and the proposed controllers is simulated successfully and the results are promising and satisfactory<sup>[7]</sup>. Comparison of the liquid level tank system with NARMA-L2 and MPC controller is done for the step and white noise desired liquid level signals. The simulation result for the desired step desired liquid level input shows that the liquid level tank system with NARMA-L2 controller have better performance in all the criteria chosen.

The simulation result for the white noise desired liquid level input shows that the liquid level tank system with NARMA-L2 controller have almost the same rise time, peak value and low value as the tracked white noise input signal. Finally, the comparative simulation result prove the effectiveness of the presented liquid level tank system with NARMA L2 controller.

This neural network control approach can be used in boiler water level and also temperature control applications of nuclear/thermal power plants<sup>[8]</sup>.

## RECOMMENDATIONS

As a future scope of this work, the NARMA-L2 controller can be implemented in a microcontroller with modified system parameters for more accurate control and can be used in various applications in industry and household. The controller can also be tested with periodically varying liquid level tracking applications.

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