

## On the Software Complexity Measures of Bubble Sort Algorithm

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**Abstract:** In this study, different software complexity measures are applied to Bubble sort algorithm. The intention is to study what kind of new information about the algorithm the complexity measures (Halstead's volume and Cyclomatic number) are able to give and to study which software complexity measures are the most useful ones in algorithm comparison. The results explicitly show that Bubble sort has the least Halstead's Volume and Program Difficulty when programmed in Assembly language and the least Program Effort when programmed in Java.

**Key words:** Software complexity, bubble sort, Halstead complexity measure, cyclomatic complexity measure

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### INTRODUCTION

A programmer usually has a choice of data structures and algorithms to use. Choosing the best one for a particular job involves, among other factors, 2 important measures:

- Time complexity: How much time will the program take?
- Space complexity: How much storage will the program need?

A programmer will sometimes seek a tradeoff between space and time complexity. For example, a programmer might choose a data structure that requires a lot of storage in order to reduce the computation time. There is an element of art in making such tradeoff, but the programmer must make the choice from an informed point of view. The programmer must have some verifiable basis on which the selection of a data structure or algorithm. Complexity analysis provides such a basis.

Complexity is a measure of the resources that must be expended in developing, implementing and maintaining an algorithm. Productivity is chiefly a management concern while reliability is a quality factor directly visible to users of software systems. These externally visible attributes of software processes and products are strongly influenced by engineering attributes of software such as complexity. Well-designed software exhibits a minimum of unnecessary complexity, unmanaged

complexity leads to software difficult to use, maintain and modify. It causes increased development costs and overrun schedules.

Algorithms are frequently assessed by the execution time and by the accuracy or optimality of the results. For practical use, an important aspect is the implementation complexity. An algorithm, which is complex to implement, requires skilled developers, longer implementation time and has a higher risk of implementation errors. Moreover, complicated algorithms tend to be highly specialized and they do not necessarily work well when the problem changes (Akkanen and Nurminen, 2000).

Algorithms can be studied theoretically or empirically. Theoretical analysis allows mathematical proofs of the execution times of algorithms but can typically be used for worst-case analysis only. Empirical analysis is often necessary to study how an algorithm behaves with typical input (Sedgewick, 1995).

Ball and Magazine (1981) listed criteria for the comparison of heuristic algorithm that in addition to execution time include ease implementation, flexibility and simplicity. Controlling and measuring complexity is a challenging engineering, management and research problem. Metrics have been created for measuring various aspects of complexity such as sheer size, control flow, data structures and intermodule structure.

Complexity measures can be used to predict critical information about reliability and maintainability of software system from automatic analysis of source code. Complexity measures also provide continuous feedback

during software project to help control the development process. During testing and maintenance they provide detailed information about software modules to help pinpoint areas of potential instability.

### SOFTWARE COMPLEXITY MEASURES

Software complexity is one branch of software metrics that is focused on direct measurement of software attributes, as opposed to indirect software measures such as project milestone status and reported system failures. Current military metrics programs emphasize non-complexity metrics that track project management information about schedules, costs and defects. While such project tracking measures are necessary to any substantial software engineering effort, they lack predictive power and are thus inadequate for risk management. Complexity measures can be used to predict critical information about reliability and maintainability of software systems from automatic analysis of the source code. Complexity measures also provide continuous feedback during a software project to help control the development process. During testing and maintenance, they provide detailed information about software modules to help pinpoint areas of potential instability.

Many of the factors affecting software quality that have been identified by researchers can be seen in part as functions of the complexity and size of the program and the capabilities of the programmers and managers. This will include, but is not limited to, testability, efficiency, legibility and structuredness.

There are a number of ways to quantify complexity in a program. The best-known metrics, which provide such feature, are McCabe's (1976) cyclomatic number and Halstead's (1977) volume. These metrics have been extensively validated and compared (Aggarwal *et al.*, 2002; Ramil and Lehman, 2000; Bezier, 1984; Curtis, 1981; Schneidewind and Hoffman, 1979).

**Halstead's complexity measures:** Halstead argued that algorithms have measurable characteristics analogous to physical laws. His model is based on 4 different parameters: The number of distinct operators (instruction types, keywords, etc.) in a program, called  $n_1$ ; the number of distinct operands (variables and constants),  $n_2$ ; the total number of occurrences of the operators,  $N_1$  and the total number of occurrences of the operands,  $N_2$ . The sum of  $n_1$  and  $n_2$  is denoted as  $n$  while the sum of  $N_1$  and  $N_2$  is called  $N$ . From those four counts, a number of useful measures can be obtained. The number of bits required to

specify the program is called the volume  $V$  of the program and is obtained through the equation.

$$V = N \log_2 n$$

The program level, which is the difficulty of understanding a program, is calculated by

$$L = (2n_2)/(n_1N_2)$$

and the intelligence content of a program is given by

$$I = L \times V$$

In an attempt to include the psychological aspects of complexity in the measures, Halstead studied the cognitive processes related to the perception and retention of simple stimuli. As reported by Olabiyisi (2006) and Olabiyisi *et al.* (2007), the mean number of mental discriminations per second in an average human being, also called the Stroud number, is between 5 and 20. Halstead uses 18 as a reference point for his studies. In his model, the number of discriminations made in the preparation of a program, called effort, is given by

$$E = V/L$$

All of these measures are valid under the assumption that the program is "pure," i.e., free of so-called "poor programming practices." Halstead defines six classes of impurities, among them, synonymous operands, unfactored expressions and common sub expressions. The complete description of these and other impurities is beyond the scope of this study. However, for the programs used for this study, all recognizable impurities were eliminated prior to obtaining the corresponding Halstead measures.

**Cyclomatic complexity measures:** Cyclomatic complexity is the most widely used member of a class of static software metrics. Cyclomatic complexity may be considered a broad measure of soundness and confidence for a program. Introduced by McCabe (1976) it measures the number of linearly independent paths through a program module. This measure provides a single ordinal number that can be compared to the complexity of other programs. Cyclomatic complexity is often referred to simply as program complexity, or as McCabe's complexity. It is often used in concert with other software metrics. As one of the more widely-accepted software metrics, it is

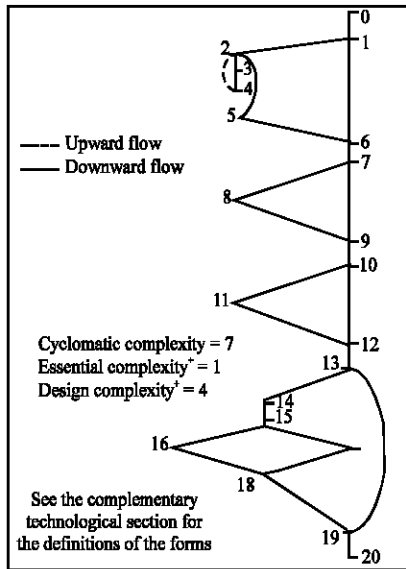


Fig. 1: Connected graph of a simple program

intended to be independent of language and language format. Cyclomatic complexity has also been extended to encompass the design and structural complexity of a system (McCabe *et al.*, 1989; Olabiyisi, 2006; Olabiyisi *et al.*, 2007).

The cyclomatic complexity of a software module is calculated from a connected graph of the module (that shows the topology of control flow within the program):

$$\text{Cyclomatic Complexity (CC)} = E - N + p$$

Where,

- E = The number of edges of the graph.
- N = The number of nodes of the graph.
- p = The number of connected components.

To actually count these elements requires establishing a counting convention (tools to count cyclomatic complexity contain these conventions). The complexity number is generally considered to provide a stronger measure of a program's structural complexity than is provided by counting lines of code. Figure 1 is a connected graph of a simple program with a cyclomatic complexity of seven. Nodes are the numbered locations, which correspond to logic branch points; edges are the lines between the nodes.

**Experiment with bubble sort algorithm:** The bubble sort is the oldest and simplest sort in use. Unfortunately, it's also the slowest. The bubble sort works by comparing

each item in the list with the item next to it and swapping them if required. The algorithm repeats this process until it makes a pass all the way through the list without swapping any items (in other words, all items are in the correct order). This causes larger values to "bubble" to the end of the list while smaller values "sink" towards the beginning of the list.

The bubble sort is generally considered to be the most inefficient sorting algorithm in common usage. Under best-case conditions (the list is already sorted), the bubble sort can approach a constant  $O(n)$  level of complexity. General-case is an abysmal  $O(n^2)$ . While the insertion, selection and shell sorts also have  $O(n^2)$  complexities, they are significantly more efficient than the bubble sort.

For the experiment, we used the complexity finder machine designed by Olabiyisi (2006) to calculate the complexity measures. To do so, the following actions were taken:

- The studied algorithm was coded using Assembly Language, C, Java, Pascal, Visual BASIC resulting in 5 programs. for each algorithm.
- The same programming style (modular programming) was employed in the coding.
- All the programs were run on the same computer.
- Operands, operator, keywords and identifiers were similarly defined for all the programs.

## RESULTS AND DISCUSSION

Table 1 presents complexity measures of different implementation languages for Bubble sort algorithm.

Figure 2 Plots the graph of Halstead's volume for different implementation languages for Bubble sort algorithm.

Figure 3 gives the graph of program difficulty for different implementation language of the algorithm. While, Fig. 4 presents the graph of Program Effort for different implementation languages for the studied algorithm.

There are interesting points to observe about these graphs. Figure 2 shows that Bubble sort has the highest Halstead's Volume when code in C. By implication, the graph shows that Bubble sort is best implemented in Assembly language followed by Pascal, Visual Basic, Java and C in that order.

Figure 3 indicates that if Program Difficulty is to be considered, Bubble sort algorithm implemented in Assembly language is the best while Bubble sort implemented in C is the worst.

Table 1: Bubble sort Complexity Measures by different Implementation Languages

Results of implementation universal machine for complexity					
Algorithm name	Language	Program Vol. (V)	Program difficulty (D)	Program effort (E)	Cyclomatic no. V(G)
Bubble sort	Assembly language	144	37	5328	4
Bubble sort	C	241	265	63865	4
Bubble sort	Java	233	252	58716	4
Bubble sort	Pascal	163	107	17441	4
Bubble sort	Visual basic	179	100	17900	4

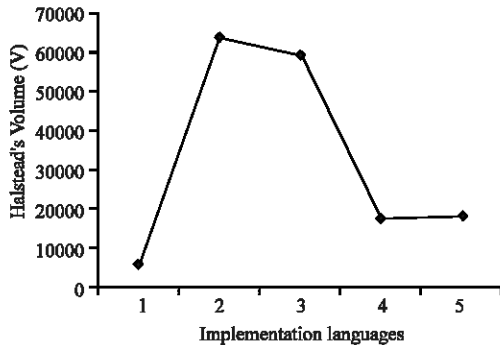


Fig. 2: Graph of different implementation of the bubble sort algorithm

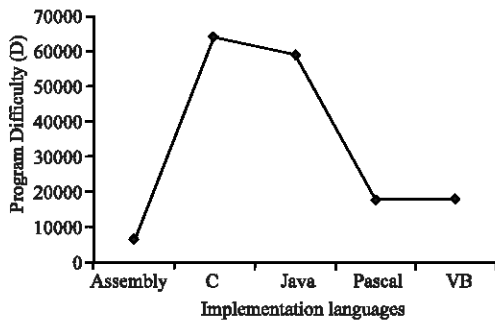


Fig. 3: Graph of program difficulty for different implementation of the bubble sort algorithm

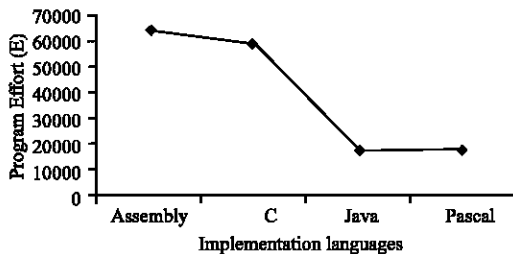


Fig. 4: Graph of program effort for different implementations of the bubble sort algorithm

In Fig. 4, we discover that considering the program effort, Bubble sort algorithm is best implemented in Java followed by Pascal, C and worst implemented in Assembly language.

For all the implementation languages, the cyclomatic number is the same (i.e.4).

### CONCLUSION

This research has considered software complexity measure experiment with Bubble sort algorithm. We study the Bubble sort algorithm by computing the Halstead's Volume (V), the program Effort (E), the program Difficulty (D) and the cyclomatic number V (G) using different implementation languages.

Software complexity measures might help practitioners to choose, out of a large number of alternatives, the algorithms that best match their needs. Understanding the trade-off between implementation and performance would give a firmer basis to decision-making.

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