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## Cost-benefit Analysis of the Web Hierarchy Caching Model

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**Abstract:** Web proxy caching hierarchy is one of the main solutions used to improve Internet QoS. Focusing on the modeling of Web proxy hierarchy caching, this paper applies cost function to analyze Web caching performance. The experiments evaluate the caching performance of different combinations of replacement policy (LRU, LFU, GDS) across different levels within Web hierarchy caching model. The experimental results demonstrate that when the lower level uses the LFU or LRU replacement policy and the upper level uses the GDS, the two-level hierarchical proxy model achieves higher caching performance.

**Key words:** Web hierarchical caching model, cost function, hit rate, byte hit rate

### INTRODUCTION

Web proxy caching has been proved to be one of the most prevalent approaches to improving user-perceived performance and reducing network traffic (ElAarag and Romano, 2009). In order to avoid single point of fault and improve caching performance, several caches being put at different levels, can cooperate. If the request is not satisfied by the lower level cache, then it will be forwarded to the upper level cache only if the copy of object is found.

In recent years, the research on Web hierarchical caching model has received increasing attention. Some of the most commonly known Web cache placement policies are LFU, LRU, GDS. The representative cache protocols are ICP, HICP, CARP, WCCP and so on (Gupta and Tokekar, 2009). The new algorithm Filter was proposed, nevertheless, Filter incurred additional complexity (Che *et al.*, 2001). The researchers mainly pay close attention to improving the existing replacement policies and caching protocols, very little research has been made on the Web cache performance for the different combinations of replacement policy. This paper keeps an eye on cost function which evaluates Web caching performance via using different combinations of replacement policies in Web hierarchical caching model.

### COST FUNCTION ANALYSIS OF THE WEB HIERARCHICAL CACHING MODEL

In Web caching hierarchical model, if the requested object has been already in cache, the cache is able to satisfy request, resulting in a cache hit. Otherwise, the cache miss occurs. If the request is not found at any

Table 1: Symbol definitions

Notation	Description
$S_t$	The size of object $t$
$Q_t$	$Q_t = 1$ , the cache hit $Q_t = 0$ , the cache miss
$N$	The total number of requests originated at the clients
$B$	The total bytes of $N$ requests
$HR_j$	HR at $j$ -th- level ( $1 \leq j \leq m$ )
$BHR_j$	BHR at $j$ -th- level ( $1 \leq j \leq m$ )

cache level, it will be send to the Web server (Chan *et al.*, 2009). Mostly Web evaluation performance metrics are captured by HR and BHR (Busari and Williamson, 2002; Shi and Zhang, 2008). Besides, the symbols of Eq. 1 and 2 are described in Table 1.

HR (Hit Rate) is the number of requests satisfied by cache divided by the  $N$  cacheable requests seen by the cache.

$$HR = \frac{\sum_{t=1}^N Q_t}{N} \times 100\% \quad (1)$$

BHR (Byte Hit Rate) emphasizes the total bytes saved by caching certain objects.

$$BHR = \frac{\sum_{t=1}^N Q_t \times S_t}{\sum_{t=1}^N S_t} \times 100\% \quad (2)$$

If the request cannot be retrieved from lower level cache, it will be directly sent to the upper level cache. In this case, it will cause data transfer or delay. Here, assume that each cache has the same caching capacity.  $C_1$  indicates the cost which is generated by the request being sent to the first-level cache. In addition to  $C_1$ , define  $C_j$

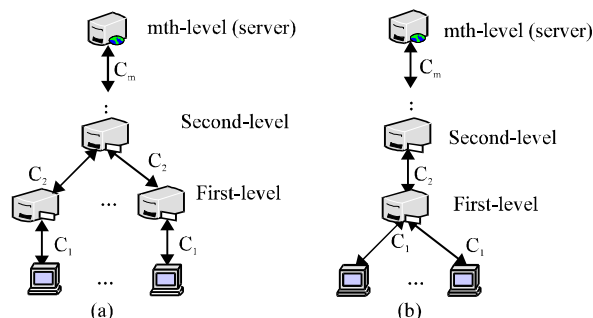


Fig. 1: Cost analysis of m-level hierarchical caching model

( $2 \leq j \leq m$ ) as the cost associated with two adjacent levels. The requests are sent to the first-level cache with the same probability, so the first-level cache can provide similar HR or BHR. In Fig. 1a, the total number of requests  $N_1$  satisfied at the first-level cache is:

$$N_1 = \sum_{i=1}^n (HR_1 \times \frac{N}{n}) = HR_1 \times N$$

Similarly, in Fig. 1b, the total number of requests satisfied at the first-level cache is:  $N_1 = HR_1 \times N$ , we can conclude  $N_1 = N_1$ . It indicates that the Fig. 1b can take place of Fig. 1a for the cost analysis in Web hierarchical caching model.

$N_j$  represents the total number of requests satisfied at the  $j$ th-level cache and  $RC_j$  signifies the cost of satisfied  $N_j$  requests. They can be respectively defined as:

$$N_j = HR_j \times (N - \sum_{i=1}^{j-1} N_i) \quad (3)$$

$$RC_j = (\sum_{i=1}^j C_i) \times N_j \quad (4)$$

$B_j$  represents the total requested bytes at the  $j$ th-level cache.  $BC_j$  means the cost of satisfied  $B_j$  bytes. Both of them can be calculated as Eq. 5 and 6.

$$B_j = BHR_j \times (B - \sum_{i=1}^{j-1} B_i) \quad (5)$$

$$BC_j = (\sum_{i=1}^j C_i) \times B_j \quad (6)$$

The total cost of requests and bytes served from the caches can be expressed as  $RC$  and  $BC$ .

$$RC = RC_1 + RC_2 + \dots + RC_m = \sum_{j=1}^m \{(\sum_{i=1}^j C_i) \times N_j\} \quad (7)$$

$$BC = BC_1 + BC_2 + \dots + BC_m = \sum_{j=1}^m \{(\sum_{i=1}^j C_i) \times B_j\} \quad (8)$$

Supposing all the requests hit at the server, the total cost of requests and bytes can be expressed as  $RC_{worst}$  and  $BC_{worst}$ .

$$RC_{worst} = RC_1 + RC_2 + \dots + RC_m = (\sum_{i=1}^m C_i) \times N \quad (9)$$

$$BC_{worst} = BC_1 + BC_2 + \dots + BC_m = (\sum_{i=1}^m C_i) \times B \quad (10)$$

In general, the requests hit at some cache or server. On this occasion, the cost of total requests and bytes can be expressed as  $RRC$  and  $RBC$ .

$$RRC = \frac{RC}{RC_{worst}} = \frac{\sum_{j=1}^m \{(\sum_{i=1}^j C_i) \times N_j\}}{(\sum_{i=1}^m C_i) \times N} \quad (11)$$

$$RBC = \frac{BC}{BC_{worst}} = \frac{\sum_{j=1}^m \{(\sum_{i=1}^j C_i) \times B_j\}}{(\sum_{i=1}^m C_i) \times B} \quad (12)$$

In order to facilitate the cost analysis, assuming  $C_j = C$  ( $1 \leq j \leq m$ ). According to Eq. 11 and 12, we can deduce Eq. 13 and 14.

$$RRC = \frac{N_1 + 2N_2 + \dots + mN_m}{mN} \quad (13)$$

$$RBC = \frac{B_1 + 2B_2 + \dots + mB_m}{mB} \quad (14)$$

Analyzing the following two cases:

- If all the requests hit at the first-level cache, we can conclude  $RRC = RBC = 1/m$ . In two-level Web hierarchy caching model, we can conclude  $RRC = RBC = 1/3$
- If all the requests are served at the server, then,  $RRC = RBC = 1$ . We can obtain  $RRC = RBC = 1$  for two-level Web hierarchy caching model

In Web hierarchy caching model, the smaller the  $RRC$  or  $RBC$  is, the less the cost of requests is.

### EXPERIMENT AND ANALYSIS

Web hierarchical caching model is an effective way to reduce the user perceived latency as well as resource consumption for network applications. For simplicity, this

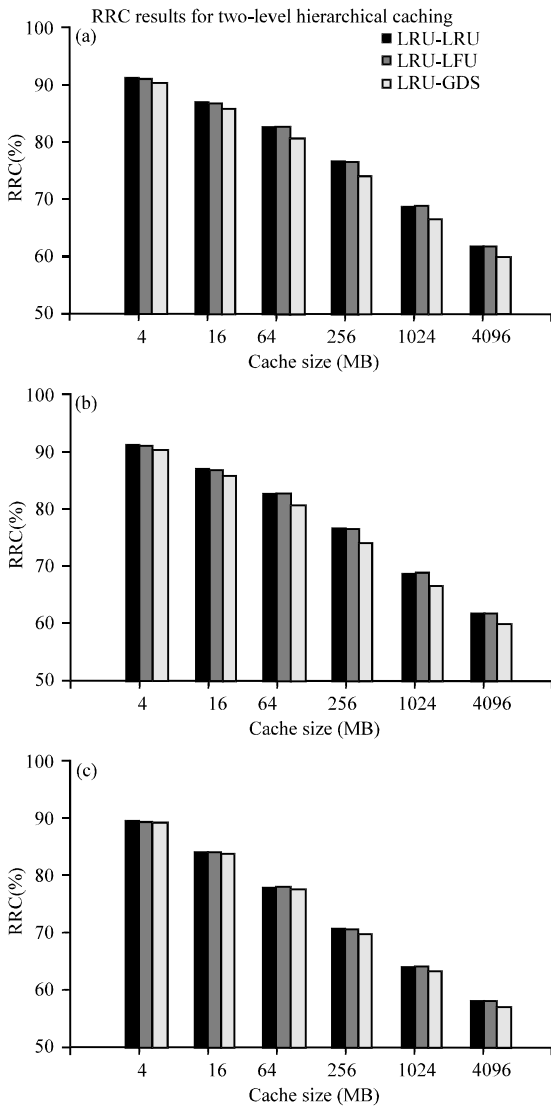


Fig. 2(a-c): The results for RRC

paper focuses on the two-level caching hierarchy and evaluates the caching performance by using the synthetic workloads (Busari and Williamson, 2002). Only consider three different policies which are LRU, LFU and GDS. Suppose lower level cache can not send a request to the upper level cache and the objects are static. There is no exchange information between each cache. LFU-LFU indicates that the former LFU represents lower level cache using LFU, the latter LFU indicates the upper level cache using LFU.

In Fig. 2a, given the same cache size, the combination LRU-GDS can achieve higher performance in terms of RRC, compared with the other two combinations (LRU-LRU and LRU-LFU). Clearly, Fig. 2b shows the combination LFU-GDS has lower RRC than the other two

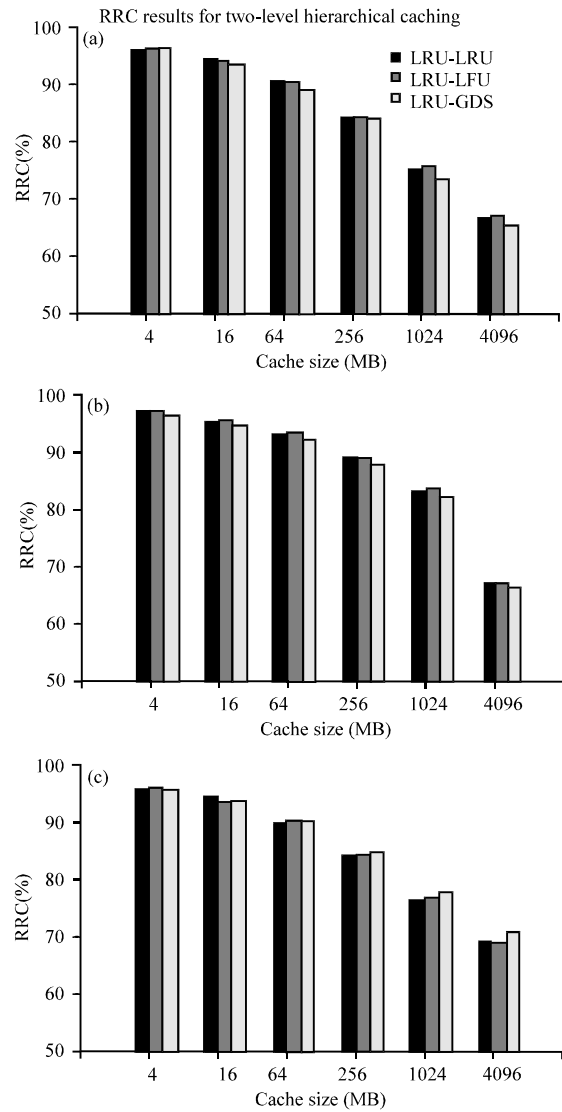


Fig. 3(a-c): The results for RBC

combinations (LFU-LFU and LFU-LRU). It is visible that the combination GDS-GDS can outperform both GDS-LFU and GDS-LRU, as shown in Fig. 2c.

As shown in Fig. 3a, given the same cache size, the combination LRU-GDS can achieve higher performance in terms of RBC, compared with the other two combinations (LRU-LRU and LRU-LFU). It can be drawn from Fig. 3b that the combination LFU-GDS has lower RRC than the other two combinations (LFU-LFU and LFU-LRU). In Fig. 3c, it is obvious that the combination GDS-GDS is the worst among the other two combinations GDS-LFU and GDS-LRU.

### CONCLUSIONS

This paper applies cost function to investigate Web cache performance of combinations of replacement policy

(LRU, LFU, GDS) at different levels of the two-level Web hierarchy model. The results manifest that when the lower level cache uses the LFU or LRU and the upper level cache uses the GDS, the two-level hierarchical cache model obtains higher Web caching performance.

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