

<http://ansinet.com/itj>

ITJ

ISSN 1812-5638

# INFORMATION TECHNOLOGY JOURNAL

**ANSI***net*

Asian Network for Scientific Information  
308 Lasani Town, Sargodha Road, Faisalabad - Pakistan

## Multicast Capacity of UWB Wireless *Ad hoc* Networks with Power Constraint

<sup>1</sup>Yongfa Hong, <sup>2</sup>Xinzhen Bai and <sup>1</sup>Binguo Wang

<sup>1</sup>College of Information Science and Engineering,

<sup>2</sup>College of Information and Electrical Engineering, Shandong University of Science and Technology,  
 Qingdao, 266590, Shandong, People's Republic of China

**Abstract:** This study discusses the multicast capacity of a large-scale random Ultra Wideband (UWB) wireless ad hoc network with power constraint. For different number of multicast destination, two different upper bounds of multicast capacity are given. When the number of multicast destination is  $O\left(\frac{n}{\log n}\right)$ , an upper bound of multicast capacity is  $O\left(\frac{(n \log n)^{\frac{\alpha-1}{2}}}{\sqrt{k}}\right)$  when the number of multicast destination is  $\Omega\left(\frac{n}{\log n}\right)$ , an upper bound of multicast capacity is  $O\left(\frac{(\log n)^{\frac{\alpha-1}{2}}}{k^{\frac{1-\alpha}{2}}}\right)$ . A strategy of MAC and routing which can achieve the lower bound of multicast capacity of power-constrained UWB wireless *ad hoc* networks is designed and the lower bound of multicast capacity is  $\Omega\left(\frac{1}{\sqrt{k}}\left(\frac{n}{\log n}\right)^{\frac{\alpha-1}{2}}\right)$ . These results extend the foregoing work on unicast capacity for UWB wireless *ad hoc* networks.

**Key words:** Multicast capacity, UWB, wireless *ad hoc* network, routing, MAC

### INTRODUCTION

Wireless *ad hoc* networks are a type of communication networks composed of a set of nodes with dynamical networking ability and without any infrastructure support. Each node has the double function for routers and hosts. The communication and cooperation between nodes are by virtue of wireless links. The characteristics of distributed structure, limited bandwidth, instability of link, dynamical topological structure make wireless *ad hoc* networks different to other communication networks. So, the research on capacity of wireless *ad hoc* networks is becoming more challenge. Gupta and Kumar (2000) initiated the research of asymptotic capacity of static wireless *ad hoc* networks. For wireless random networks whose nodes are randomly and uniformly deployed in a disc with unit area, they showed that the asymptotic capacity is:

$$\Theta\left(\frac{W\sqrt{n}}{\sqrt{\log n}}\right)$$

under the protocol model and the upper bound and lower bound are  $O(\sqrt{n})$  and:

$$\Omega\left(\sqrt{\frac{n}{\log n}}\right)$$

under physical model. Grossglauser and Tse (2002) and Diggavi *et al.* (2005) showed that the mobility of nodes, even one-dimensional mobility, can improve the asymptotic capacity of wireless random networks to  $O(n)$ . Haddad *et al.* (2006) showed that the broadcast capacity of wireless random networks is:

$$\Theta\left(\frac{W}{\max(1, \Delta^d)}\right)$$

where,  $\Delta$ , are the reference parameter and the dimension of space. For more general occasion, Shakkottai *et al.* (2007) derived an upper bound of multicast capacity of wireless random network and designed a multicast routing mechanism based "comb" structure which can make wireless random network attain

the multicast capacity in the same order with the upper bound. Li *et al.* (2007) showed that the total multicast capacity is:

$$\Theta\left(\sqrt{\frac{n}{\log n}} \frac{W}{\sqrt{k}}\right)$$

when the number of destination of each multicast source is:

$$k = O\left(\frac{n}{\log n}\right)$$

and is  $\Theta(W)$  when the number of destination of each multicast source is:

$$k = \Omega\left(\frac{n}{\log n}\right)$$

UWB (Ultra Wideband) is a technology for transmitting information spread over a large bandwidth (>500 MHz). UWB has many advantages such as strong anti-interference performance, high transmission rate, very wide bandwidth, low energy consumption, small sending power etc. UWB technology has many applications such as indoor communication, high rate wireless LAN, home network, precision locating and tracking applications etc. Negi *et al.* study the asymptotic capacity of power-restricted UWB wireless ad hoc networks. Negi and Rajeswaran (2007) showed an upper bound of capacity for single node of above networks is:

$$O\left((n \log n)^{\frac{\alpha-1}{2}}\right)$$

and an feasible lower bound of capacity for single node is:

$$\Omega\left(\frac{n^{\frac{\alpha-1}{2}}}{(\log n)^{\frac{\alpha+1}{2}}}\right)$$

With the theory of percolation, Zhang and Hou (2005) improve the above-mentioned lower bound to:

$$\Omega\left((n \log n)^{\frac{\alpha-1}{2}}\right)$$

which is the same order with the upper bound. Otherwise, this study is confined to uni-cast capacity of networks. The object of the present study is to study the multicast capacity of power-restricted UWB wireless *ad hoc* networks.

## NETWORK MODEL

Suppose that  $n$  nodes are randomly and uniformly deployed in a square with unit area, the set of all nodes is denoted as  $V = \{v_1, v_2, \dots, v_n\}$ . Each node is a source of a multicast flow and each source randomly choose  $k-1$  ( $2 \leq k \leq n$ ) different nodes as destinations of multicast flow from the remainder  $n-1$  nodes. Each source  $v_i$  will send data to its all destinations with rate  $r_k(n)$ . Since the restriction of transmission capability of wireless nodes, the data maybe by virtue of multi-hops and storage-and-forward to reach to all destinations. If there is a spatio-temporal scheduling strategy so that the data send by source with rate  $r_k(n)$  can be received by corresponding destinations with high probability, then the rate  $r_k(n)$  is called feasible multicast throughput.

Suppose all physical links are point-to-point links which use UWB impulse wireless transmission technology and support the rate of Shannon capacity. Each node adopt binary PPM modulation with additive white Gaussian noise, the power spectrum density of noise is  $N_0$ . The signal attenuation is in proportion to the  $\alpha$  power of the distance between the sending and receiving nodes, where  $\alpha \geq 2$  is the path loss index. So, the power loss  $h_{ij}$  between node  $v_i$  and node  $v_j$  can be expressed as  $h_{ij} = |v_i - v_j|^{-\alpha}$ , where  $|v_i - v_j|$  is the Euclidean distance between node  $v_i$  and node  $v_j$ . So, the SINR (signal-to-interference and noise ratio) at the receiving node can be expressed as:

$$\text{SINR} = \frac{P_{ij} h_{ij}}{N_0 W + \sum_{k=1}^M a_k P_k h_{kj}}$$

where,  $P_{ij}$  is the sending power of node  $v_i$  on the link  $v_i \rightarrow v_j$ ,  $P_k$  is the total transmit power of node  $v_k$ ,  $W$  is signal bandwidth,  $M$  is the number of collided packets since there are  $M$  nodes simultaneously send data,  $a_k$  is orthogonal factor. For homogenous networks,  $a_k = a$ ,  $\forall k \in \{1, 2, \dots, n\}$ . The first term  $\eta W$  of denominator in the SINR is the Gaussian noise power and the second term is Multi-user Interference (MUI). If AWGN noise power is far larger than MUI, then MUI can be ignored with respect to AWGN noise. So, the SINR can be simplified as  $\text{SINR} = P_{ij} h_{ij} / (N_0 W)$ . By the formula of Shannon capacity, the Shannon capacity  $C_{ij}$  of each link can be expressed as:

$$C_{ij} = \lim_{W \rightarrow \infty} W \log \left(1 + \frac{P_{ij} h_{ij}}{N_0 W}\right) = \frac{P_{ij} h_{ij}}{N_0}$$

When node  $v_i$  use power  $P_{ij}$  to send data on the link  $v_i \rightarrow v_j$ , the transmission rate on the link  $v_i \rightarrow v_j$  is:

$$r_{ij} = C_{ij} = \frac{P_{ij} h_{ij}}{N_0}$$

which means:

$$P_{ij} = \frac{r_{ij} N_0}{h_{ij}} = r_{ij} N_0 |v_i - v_j|^\alpha$$

## AN UPPER BOUND OF MULTICAST CAPACITY

This section will derive an upper bound of Power-constraint UWB wireless *ad hoc* networks. Firstly, a square with unit area is divided into smaller square with area  $\frac{100 \log n}{n}$  by use of straight line paralleling to the side of square. Thus the length of side of smaller square is:

$$\rho(n) = \sqrt{\frac{100 \log n}{n}}$$

The set of all smaller squares is denoted as  $V(n, \rho(n))$ . The number of nodes inside region  $s$  is denoted as  $N(S)$ . The following Vapnik-Chervonenkis theorem will be used in the next discussion:

**Vapnik-Chervonenkis theorem (Vapnik and Chervonenkis, 1971):** Suppose  $\mathfrak{Z}$  is a set with finite VC-dimension  $VC-d(\mathfrak{Z})$ ,  $\{X_i\}$  is a sequence of independently random variables with a common distribution  $P$ , then for any  $\varepsilon, \delta > 0$ , when:

$$N > \max \left\{ \frac{8VC-d(\mathfrak{Z})}{\varepsilon}, \log \frac{16e}{\varepsilon}, \frac{4}{\varepsilon} \log \frac{2}{\delta} \right\}$$

$$\Pr \left( \sup_{F \in \mathfrak{Z}} \left| \frac{1}{N} \sum_{i=1}^N I(X_i \in F) - P(F) \right| \leq \varepsilon \right) > 1 - \delta$$

is valid.

By use of the above-mentioned Vapnik-Chervonenkis theorem, the following lemma can be proved:

**Lemma 1:** For a smaller square  $S$  ( $S \in V(n, \rho(n))$ ), the number  $N(S)$  of nodes which lie inside  $S$  satisfies  $50 \log n \leq N(S) \leq 150 \log n$  with high probability.

**Proof:** It is easy to verify that the VC-dimension  $VC-d(v(n, \rho(n)))$  of set  $V(n, \rho(n))$  is 3. Let:

$$\varepsilon = \delta = \frac{50 \log n}{n}$$

when  $n$  is large enough, by Vapnik-Chervonenkis theorem:

$$\Pr \left( \sup_{S \in V(n, \rho(n))} \left| \frac{N(S)}{n} - \frac{100 \log n}{n} \right| \leq \frac{50 \log n}{n} \right) > 1 - \frac{50 \log n}{n}$$

That is:

$$\Pr \left( \sup_{S \in V(n, \rho(n))} |N(S) - 100 \log n| \leq 50 \log n \right) > 1 - \frac{50 \log n}{n}$$

Thus:

$$\lim_{n \rightarrow \infty} \Pr \left( \inf_{S \in V(n, \rho(n))} N(S) \geq 50 \log n \right) = 1$$

$$\lim_{n \rightarrow \infty} \Pr \left( \sup_{S \in V(n, \rho(n))} N(S) \leq 150 \log n \right) = 1$$

This means that the number  $N(S)$  of nodes which lie inside  $S$  satisfies  $50 \log n \leq N(S) \leq 150 \log n$  with high probability.

For the set  $T_i$  of all multicast trees which connect the multicast source  $v_i$  and corresponding  $k-1$  multicast destinations, if  $\|t_i\|$  denotes the sum of side of multicast tree  $t_i \in T_i$ , Li *et al.* (2007) prove the following lemma.

**Lemma 2 (Li *et al.*, 2007):** For any  $t_i \in T_i$ , when  $k \rightarrow \infty$ , then  $\|t_i\|$  satisfies  $\|t_i\| \geq \tau \sqrt{k}$ , a.s., where,  $\tau$  is a constant.

For two multicast trees  $t_i$  and  $t_i^*$  in  $T_i$ , if  $r_i(k)$  and  $r_i^*(k)$  denote the multicast rate of multicast source,  $\|t_i\|^\alpha$ ,  $\|t_i^*\|^\alpha$  denote the sum of  $\alpha$  power of each side's Euclidean length for multicast trees  $t_i$  and  $t_i^*$ , where  $t_i^*$  is the multicast tree with minimum sum of  $\alpha$  power of each side's Euclidean length, that is  $t_i^* \in \arg \min_{t_i \in T_i} \|t_i\|^\alpha$ .  $t_i^*$  is called the minimum power multicast tree. The total power used by two multicast trees are  $P(t_i) = r_i(k) N_0 \|t_i\|^\alpha$  and  $P(t_i^*) = r_i(k) N_0 \|t_i^*\|^\alpha$ , respectively. In order to derive the upper bound of multicast capacity, an upper bound of the number of the smaller squares which intersect with minimum power multicast tree  $t_i^*$  is needed.

**Lemma 3:** The number  $N_{\max}$  of the smaller squares which intersect with minimum power multicast tree  $t_i^*$  satisfies:

$$N_{\max} \leq \pi k + \frac{\sqrt{2}}{5} \sqrt{\frac{n}{\log n}} \|t_i^*\|$$

**Proof:** With a similar method used by Li *et al.* (2007), a region  $C(t_i^*)$  in the plane is defined as:

$$Y \in C(t_i^*) \text{ if and only if } \exists Z \in t_i^* \text{ such that } |Z - Y| \leq \sqrt{2} \rho(n)$$

where,  $Z, Y$  are the points lie in square with unit area. If  $|C(t_i^*)|$  denotes the total area of the region  $|C(t_i^*)|$ , then  $|C(t_i^*)|$  satisfies:

$$|C(t_i^*)| \leq \frac{100 \log n}{n} \pi k + \sqrt{\frac{800 \log n}{n}} \|t_i^*\|$$

Since the area of each smaller square is  $\frac{100 \log n}{n}$ , so, the number  $N_{\max}$  of the smaller squares which intersect with minimum power multicast tree  $t_i^*$  satisfies:

$$N_{\max} \leq \frac{|C(t_i^*)|}{\frac{100 \log n}{n}} \leq \pi k + \frac{\sqrt{2}}{5} \sqrt{\frac{n}{\log n}} \|t_i^*\|$$

Since each smaller square contain at most  $150 \log n$  nodes with high probability, so  $N_{\max}$  satisfies:

$$\begin{aligned} N_{\max}^{\text{nodes}} &\leq 150 \log n \times N_{\max} \\ &\leq 150 \log n \times \left( \pi k + \frac{\sqrt{2}}{5} \sqrt{\frac{n}{\log n}} \|t_i^*\| \right) \\ &= 150 \pi \log n k + 30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \end{aligned}$$

with high probability. Since the total consumed power of each multicast tree depend on the rate of multicast source and the length of multicast tree, then:

$$\begin{aligned} P(t_i^*) &= r_i^*(k) N_0 \|t_i^*\|^\alpha \\ &\geq N_{\max}^{\text{nodes}} r_i^*(k) N_0 \left( \frac{\|t_i^*\|}{N_{\max}^{\text{nodes}}} \right)^\alpha \\ &\geq r_i^*(k) N_0 \frac{\|t_i^*\|^\alpha}{\left( 150 \pi \log n k + 30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \right)^{\alpha-1}} \end{aligned}$$

Because the total power can be availed by all nodes is  $nP_0$  and there are  $n$  minimum power multicast trees in the network. By the symmetry of deployment of nodes, the expectation of the consumed power for each minimum power multicast tree  $t_i^*$  must be less or equal to  $P_0$  this means:

$$P_0 \geq E(P(t_i^*)) = r_i^*(k) N_0 E \left( \frac{\|t_i^*\|^\alpha}{\left( 150 \pi \log n k + 30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \right)^{\alpha-1}} \right)$$

The following two kinds of situations are discussed:

- When:

$$k = O \left( \frac{n}{\log n} \right)$$

since  $\|t_i^*\| \geq \tau \sqrt{k}$ , a.s., as  $n$  is large enough, then  $30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \geq 150 \pi \log n k$ .

Thus there are constants  $c, c_1 > 0$  such that:

$$P_0 \geq E(P(t_i^*)) = r_i^*(k) N_0 c_1 \frac{E(\|t_i^*\|)}{(n \log n)^{\frac{\alpha-1}{2}}} \geq r_i^*(k) N_0 c \frac{\sqrt{k}}{(n \log n)^{\frac{\alpha-1}{2}}}$$

So:

$$r_i^*(k) \leq c P_0 \frac{(n \log n)^{\frac{\alpha-1}{2}}}{\sqrt{k}}$$

That means that:

$$\lim_{n \rightarrow \infty} \Pr \left( r(n, k) = c P_0 \frac{(n \log n)^{\frac{\alpha-1}{2}}}{\sqrt{k}} \text{ is feasible} \right) = 0$$

- When:

$$k = \Omega \left( \frac{n}{\log n} \right)$$

Since:

$$f(\|t_i^*\|) = \frac{\|t_i^*\|^\alpha}{\left( 150 \pi \log n k + 30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \right)^{\alpha-1}}$$

is a monotonic increasing function with respect to  $\|t_i^*\|$  and  $\|t_i^*\| \geq \tau \sqrt{k}$ , a.s. so:

$$\frac{\|t_i^*\|^\alpha}{\left( 150 \pi \log n k + 30 \sqrt{2} \|t_i^*\| \sqrt{n \log n} \right)^{\alpha-1}} \geq \frac{(\tau \sqrt{k})^\alpha}{\left( 150 \pi \log n k + 30 \sqrt{2} \tau \sqrt{k} \sqrt{n \log n} \right)^{\alpha-1}}$$

Since:

$$k = \Omega \left( \frac{n}{\log n} \right)$$

then as  $n$  is large enough  $150 \pi \log n k \geq 30 \sqrt{2} \tau \sqrt{k} \sqrt{n \log n}$ .

Thus there are constants  $c_3, c_4 > 0$  such that:

$$P_0 \geq E(P(t_i^*)) \geq r_i^*(k) N_0 c_3 \frac{(\sqrt{k})^\alpha}{(\log n k)^{\alpha-1}} = r_i^*(k) c_4 \frac{k^{1-\frac{\alpha}{2}}}{(\log n)^{\alpha-1}}.$$

It is:

$$r_i^*(k) \leq c_4 P_0 \frac{(\log n)^{\alpha-1}}{k^{1-\frac{\alpha}{2}}}$$

So:

$$\lim_{n \rightarrow \infty} \Pr \left( r(n, k) = c_4 P_0 \frac{(\log n)^{\alpha-1}}{k^{1-\frac{\alpha}{2}}} \text{ is feasible} \right) = 0$$

from what has been discussed above, the following theorem is true.

**Theorem 1:** The multicast capacity of the above-mentioned power-constraint wireless *ad hoc* networks satisfies:

When:

$$k = O\left(\frac{n}{\log n}\right)$$

Then:

$$\lim_{n \rightarrow \infty} \Pr\left(r(n, k) = cP_0 \frac{(n \log n)^{\frac{\alpha-1}{2}}}{\sqrt{k}} \text{ is feasible}\right) = 0$$

When:

$$k = \Omega\left(\frac{n}{\log n}\right)$$

Then:

$$\lim_{n \rightarrow \infty} \Pr\left(r(n, k) = cP_0 \frac{(\log n)^{\frac{\alpha-1}{2}}}{k^{1-\frac{\alpha}{2}}}\right) = 0$$

Especially, when  $k = 2$  which is the situation of unicast, then by the above theorem 1:

$$\lim_{n \rightarrow \infty} \Pr\left(r(n, k) = cP_0 (n \log n)^{\frac{\alpha-1}{2}} \text{ is feasible}\right) = 0$$

That is the same order with the upper bound of pernode unicast throughput of Power-constraint UWB wireless *ad hoc* networks which is derived by Negi and Rajeswaran (2007).

## A LOWER BOUND OF MULTICAST CAPACITY

In this section, a lower bound of multicast capacity is derived by virtue of the constructive method. Since each multicast source can randomly choose different  $k-1$  ( $2 \leq k \leq n$ ) nodes from  $n-1$  nodes, so, a node maybe the destination for multiple multicast flows. According to Li *et al.* (2007), a node is the destination for at most:

$$\Theta\left(\frac{\log n}{\log \log n}\right)$$

multicast flows with high probability. With a Similar method of Li *et al.* (2007), a square with unit area is divided into smaller square with area  $\frac{100 \log n}{n}$  by use of

straight line paralleling to the side of square, thus there are  $1/a(n)$  smaller square in the square with unit area. For this partition, Li *et al.* (2007) prove the following lemma.

**Lemma 4 (Li *et al.*, 2007):** If:

$$a(n) \geq \frac{50 \log n}{n}$$

then each smaller square contain  $\Theta(na(n))$  nodes with high probability.

Since:

$$a(n) = \frac{100 \log n}{n}$$

satisfies the condition of the above lemma, so each smaller square will contain  $\Theta(na(n)) = \Theta(\log n)$  nodes with high probability. Next, a multicast tree which connects multicast source and all multicast destinations is constructed based on the Manhattan multicast routing algorithm by Li *et al.* (2007). Such construction make the number of multicast flow through a smaller square be  $O(\sqrt{kn \log n})$  with high probability. As discussed earlier, each smaller square contain  $\Theta(\log n)$  nodes with high probability. In order to balance the number of multicast flows in each smaller square. The following multicast flow allocation mechanism is adopted:

- For any multicast flow began in a smaller square, then the multicast source is assigned to this multicast flow
- For any multicast flow terminated in a smaller square, then the multicast destinations are assigned to this multicast flow
- For any multicast flow relayed in a smaller square, then the node with minimum assigned multicast flow is assigned this multicast flow

Since each smaller square contain  $\Theta(\log n)$  nodes with high probability and the number of multicast flows through a smaller square is at most  $O(\sqrt{kn \log n})$ . By the above-mentioned multicast flow allocation mechanism, the number of multicast flows relayed in a smaller square is at most:

$$O\left(\sqrt{k} \frac{\sqrt{n}}{\sqrt{\log n}}\right)$$

with high probability, so the number of assigned multicast flows for a node in a smaller square is at most:

$$1 + \Theta\left(\frac{\log n}{\log \log n}\right) + O\left(\sqrt{k} \frac{\sqrt{n}}{\sqrt{\log n}}\right) = O\left(\sqrt{k} \frac{\sqrt{n}}{\sqrt{\log n}}\right)$$

with high probability.

Since, the transmission of node is limited to the adjacent smaller squares, the rate  $d(n)$  which is transmitted by a node in a smaller square satisfies:

$$d(n) \geq \frac{cP_0}{N_0} \left( \frac{n}{\log n} \right)^{\frac{\alpha}{2}}$$

and the number of assigned multicast flows for a node in a smaller square is at most:

$$O\left(\sqrt{k} \frac{\sqrt{n}}{\sqrt{\log n}}\right)$$

with high probability. So if chosen multicast rate  $r(n)$  satisfies:

$$r(n)\sqrt{k} \frac{\sqrt{n}}{\sqrt{\log n}} \leq \frac{c_4 P_0}{N_0} \left( \frac{n}{\log n} \right)^{\frac{\alpha}{2}} \Rightarrow r(n) \leq c_5 P_0 \frac{1}{\sqrt{k}} \left( \frac{n}{\log n} \right)^{\frac{\alpha-1}{2}}$$

Then it is ensured that  $r(n)$  is a feasible multicast rate. Thus multicast rate of Power-constraint UWB wireless *ad hoc* networks satisfies:

$$\lim_{n \rightarrow \infty} \Pr \left( r(n) = cP_0 \frac{1}{\sqrt{k}} \left( \frac{n}{\log n} \right)^{\frac{\alpha-1}{2}} \text{ is feasible} \right) = 1$$

Above all, the following conclusion is attained:

**Theorem 2:** A feasible lower bound of multicast capacity for Power-constraint UWB wireless *ad hoc* networks is:

$$\lim_{n \rightarrow \infty} \Pr \left( r(n) = cP_0 \frac{1}{\sqrt{k}} \left( \frac{n}{\log n} \right)^{\frac{\alpha-1}{2}} \text{ is feasible} \right) = 1$$

Especially, when  $k = 2$  which is the situation of unicast, then the result of the above theorem 2 is reduced to:

$$\lim_{n \rightarrow \infty} \Pr \left( r(n) = cP_0 \left( \frac{n}{\log n} \right)^{\frac{\alpha-1}{2}} \text{ is feasible} \right) = 1$$

The above feasible lower bound is higher on order than the feasible lower bound:

$$\Omega \left( \frac{n^{\frac{\alpha-1}{2}}}{(\log n)^{\frac{\alpha+1}{2}}} \right)$$

which is given by Negi and Rajeswaran (2007).

## CONCLUSION

The present study discusses the multicast capacity of power-constraint large scale random UWB wireless *ad hoc* networks. According to the number of the multicast destinations, two different upper bound of multicast capacity are derived. When the number of multicast destinations satisfies:

$$O\left(\frac{n}{\log n}\right)$$

an upper bound of multicast capacity for Power-constraint large scale random UWB wireless *ad hoc* networks is:

$$O\left(\frac{(n \log n)^{\frac{\alpha-1}{2}}}{\sqrt{k}}\right)$$

When the number of multicast destinations satisfies:

$$\Omega\left(\frac{n}{\log n}\right)$$

an upper bound of multicast capacity:

$$O\left(\frac{(\log n)^{\alpha-1}}{k^{\frac{1-\alpha}{2}}}\right)$$

where,  $\alpha \geq 2$  is path loss index,  $n$  is the number of network nodes,  $k$  is the number of multicast destinations. On the other hand, a strategy of MAC and routing which can attain feasible throughput:

$$\Omega\left(\frac{1}{\sqrt{k}} \left( \frac{n}{\log n} \right)^{\frac{\alpha-1}{2}}\right)$$

is designed, at the same time, a feasible lower bound of multicast capacity for power-constraint UWB wireless *ad hoc* networks is obtained.

## REFERENCES

- Diggavi, S.N., M. Grossglauser and D.N.C. Tse, 2005. Even one-dimensional mobility increases the capacity of wireless networks. IEEE Trans. Inform. Theory, 51: 3947-3954.
- Grossglauser, M. and D. Tse, 2002. Mobility increases the capacity of Ad-hoc wireless networks. IEEE/ACM Trans. Network., 10: 477-485.

- Gupta, P. and P.R. Kumar, 2000. The capacity of wireless networks. *IEEE Trans. Inform. Theory*, 46: 388-404.
- Haddad, A.K., V. Ribeiro and R. Riedi, 2006. Broadcast capacity in multi-hop wireless networks. *Proceedings of The Annual International Conference on Mobile Computing and Networking*. September 23-29, 2006, Los Angeles, CA., USA., pp: 239-250.
- Li, X.Y., S.J. Tang and O. Frieder, 2007. Multicast capacity for large scale wireless *ad hoc* networks. *Proceedings of the 13th Annual ACM International Conference on Mobile Computing and Networking*, September 9-14, 2007, Montreal, Quebec, Canada, pp: 266-277.
- Negi, R. and A. Rajeswaran, 2007. Capacity of ultra wide band wireless *ad hoc* networks. *Trans. Wireless Commun.*, 6: 3816-3824.
- Shakkottai, S., L. Xin and R. Srikant, 2007. The multicast capacity of large multihop wireless networks. *Proceedings of the 13th Annual ACM International Conference on Mobile Computing and Networking*, September 9-14, 2007, Montreal, Quebec, Canada, pp: 247-255.
- Vapnik, V.N. and A.Y. Chervonenkis, 1971. On the uniform convergence of relative frequencies of events to their probabilities. *Theo. Probab. Applic.*, 16: 264-264.
- Zhang, H. and J.C. Hou, 2005. Capacity of wireless *ad hoc* networks under ultra wide band with power constraint. *Proceedings of the International Conference on Computer Communications*, March 13-17, 2005, Miami, FL, USA., pp: 455-465.