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Advanced Manufacture Model Based on Cost Control

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Abstract: A model for machining parameter optimization in multi-batch and multi-job is built based on cost analysis. In order to minimize the whole cost, the scheduling rules are employed for the machining parameter optimization during scheduling course with Genetic Algorithm (GA). An example of corporation based on the model and algorithm is developed to validate the rationality of modeling and validity of algorithm. Computational result shows that the new fashion of manufacture model proposed in this paper is advanced for cost control.

Key words: Machining parameter, multi-batch, multi-job, genetic algorithm, cost control

INTRODUCTION

Machining parameter optimization and job scheduling are the most important factors for cost control because the machining parameters can determine the processing time which influences the schedule. The research about machining parameter optimization was in-depth for one job to minimize the cost. For example, Budake *et al.* (1996) educed an approach and Saravanan *et al.* (2001) thought that genetic algorithm was the right approach for machining parameter optimization. Moreover, the model and algorithm of scheduling for minimum cost also emerged endlessly. Rohleder and Scudder (1993) compared both types of economic objectives and built a dynamic job shop model with computer simulation. Shafaei and Brunn (1999) found that the raw material cost and income of jobs were constant so, the formula for operating costs can be found. At present, the problem that how to make the machining parameter optimization of multi-job is still hard to solve. Vickson (1980) studied the scheduling problem in which the processing time can be controlled. Biskup and Cheng (1999) researched the problem that the cost function related to the control of the processing time was generally a linear function taking the form of addition. Chen and Zheng (2001) discussed the kind of single machine scheduling problem with controllable processing times. However, these researches simplified the relation between processing time and processing cost as linearity. In fact, the machining parameters which determine the processing time and influence the schedule, have very complex relation to the cost.

Moreover, In modern manufacture corporation, the jobs usually arrive the shop in the light of batches. When the arriving times of batches are different, the influence

from subsequent batches to anterior batches scheduled also affects the whole cost (Church and Uzsoy, 1992; Jain and Elmaraghy, 1997). Hence, a new model will be proposed in this paper to realize cost control. The model, facing multi-batch and multi-job, can be employed to optimize the machining parameters during the scheduling course and to deal with the relation between rescheduling and cost well.

MODEL CONSTRUCTION

The cost, changed with the variety of processing parameters includes three parts: processing cost, tool cost and logistics cost (Ballfou, 1999). In addition, the penalty cost and the rescheduling cost should be considered on account of the due time and rescheduling.

Coefficient S_i can be synthesized to express the metal removal rate from previous operation to next operation and the assistant time t_{oi} is a constant for each operation. So the processing cost is stated as follow; (Suffix i expresses job i in each batch, herein after the same):

$$C_{1i} = C_m t_{mi} + C_o t_{oi} = C_m \left(\frac{S_i}{f_i \times v_i \times a_{pi}} + \frac{C_o}{C_m} t_{oi} \right) \quad (1)$$

where, C_m is mobile cost per unit time, C_o is assistant cost per unit time. Tool cost is that:

$$C_{2i} = (C_m t_a + C_t) \times \frac{t_{mi}}{T_i} = (C_m t_a + C_t) \times \frac{v_i^{m_1-1} \times f_i^{m_2-1} \times a_{pi}^{m_3-1} \times S_i}{C_T} \quad (2)$$

where, t_a is tool-exchange time, C_t is the cost of one tool, C_T is tool life coefficient and m_1, m_2, m_3 express separately to the influence of v, f, a_p .

Minishing the WIP buffers and shortening the circulation time is propitious to cost control (Faria *et al.*, 2006). Then the WIP cost is that (Pinedo, 1995):

$$C_{3i} = w_i P_i \quad (3)$$

where P_i , complete time of the job, expresses the whole time from ready to complete and w_i is the WIP cost per unit time.

The penalty cost is described as follow (Suffix j expresses batch j , hereinafter the same):

$$C_{4j} = \begin{cases} l_j \times (P_j - Q_j) & \text{if } (P_j > Q_j) \\ 0 & \text{if } (P_j < Q_j) \end{cases} \quad (4)$$

where Q_j is the due time of the batch and l_j is the coefficient of tardiness.

A coefficient r is used to express the increase proportion and rescheduling cost is denoted as follow:

$$C_{5i} = r C_{1i} \quad (5)$$

In the equation, if the job i need not be rescheduling, $r = 0$.

The objective function for m batches, in which there are n jobs, processed on one machine is as follow:

$$C = \sum_{j=1}^m \sum_{i=1}^n C_{1i} + \sum_{j=1}^m \sum_{i=1}^n C_{2i} + \sum_{j=1}^m \sum_{i=1}^n C_{3i} + \sum_{j=1}^m C_{4j} + \sum_{j=1}^m \sum_{i=1}^n C_{5i} \quad (6)$$

When the processing time is known that is to say, the machining parameters are certain and unchangeable, it is a NP-hard question for different batches of jobs arrived at different time (Pinedo, 1995). So a pseudo polynomial algorithm based on the conclusion of Lawler (1977) can be put forward to get the optimal schedule on certain machining parameters. The algorithm is described as follow:

- Step 1:** Observe the processing state of machine if there is new batch arriving. If machine is not working that is to say a job is just complete, transfer to step 2. If machine is working, namely a job is being processing, wait for the completion of the job and transfer to step 2. If all the jobs are complete, transfer to step 8
- Step 2:** Arrange all the unprocessing jobs as a schedule with weighted shortest machining time first (WSPT) rule (Pinedo, 1995) and calculate the whole cost. Remember the cost and its corresponding schedule and transfer to step 3
- Step 3:** Setup the priority of jobs in the sequence in the light of the due time of the batch that jobs belong

to. The priority is from 1 to m . where m denotes the quantity of the batches in the schedule. For example, if the jobs in the schedule belong to 3 batches respectively, m is equal to 3. The less the due time of the batch that jobs belongs to is, the higher priority the job has. The 1 is assigned to variable "flag" and transfer to step 4

- Step 4:** Choose the jobs whose priority are equal to the value of variable "flag". And mark the job which is the last one in these jobs, in the schedule. Transfer to step 5
- Step 5:** Pick up the job whose priority is greater than the value of variable "flag" and which is the nearest one from the marked job to the front. Then insert this job behind the marked job and transfer to step 6
- Step 6:** Calculate the whole cost on current schedule and remember it. If there is no job whose priority is greater than the value of variable "flag" before the marked job, transfer to step 7. Otherwise, transfer to step 5
- Step 7:** Plus 1 to the value of variable "flag" and judge it. If the value of variable "flag" is equal to m , transfer to step 8. Otherwise, transfer to step 4
- Step 8:** Select the least whole cost from all the whole cost remembered as the optimal whole cost and regard its corresponding schedule as the optimal schedule

The algorithm is not only tallying with processing request but easy and feasible.

GENETIC ALGORITHM

Genetic Algorithm is used in this paper to optimize the machining parameters and schedule for minimum cost with different batches.

Usually, a_p is decided by cutting allowance, so the variables for optimization are v and f . There are five kinds of restrictions existing in processing course: restriction of rotate velocity of principal axis, restriction of feed rate, restriction of machine power, restriction of surface roughness and restriction of cutting force (Armarego, 1994). The ranges of variables are determined by these five kinds of restrictions.

The length of one chromosome is $m+k$. where, m and k are determined by precision. In this study, $m = k = 3$. Random selection is employed to generate the initial population and its dimension is 400. The calculation course of fitness of one chromosome is that: first,

translate the chromosome into machining parameters namely f_{ij} , v_{ij} . Second, calculate the processing time of each job with these machining parameters. Third, utilize the model and the algorithm introduced in 1.8 to calculate the whole cost as the fitness of this chromosome.

The selection operator is used by roulette selection and the probability of selection is 0.2. On account of large scope of individual, uniformity crossover can augment search bound with 0.7 probabilities. In order to advance the search efficiency, 0.1 probabilities are adopted to uniformity mutation 15. The genetic algorithm will stop after 1000.

EXAMPLE

The simulation is for the cylindrical finish machining of roller with HT125 lathe in Shanghai Jingzheng mechanical equipment Ltd. The parameters of machine and tool are mentioned in Table 1.

Example: Two batches arrives at workshop orderly and the alternation is 15000 sec. The dimension, single border cutting allowance, surface roughness and value of S ($S = D \times L \times A / 1000$) and other parameters are mentioned in Table 2.

In order to compare each other expediently, the whole cost will be calculated by three approaches:

- **Approach 1:** As the traditional fashion of company, choose the right machining parameters for minimum cost of each operation firstly and then arrange the processing schedule with determinate processing time. The approach introduced by Saravanan *et al.* (2001) will be employed to choose the right machining parameters for minimum cost of each operation. If there is another batch of jobs arriving, the rescheduling will not be

executed. That is to say, the subsequent batches must be processed after the completion of anterior batches

- **Approach 2:** The model built in this paper for machining parameter optimization during the scheduling course are used for minimum cost in one batch of jobs. For different batches, the approach is same as that of approach 1
- **Approach 3:** The model and rule for different batch of jobs put forward in this paper are used

According to these three approaches, the above example are shown in Table 3.

Table 3 shows that the whole cost of approach 3 are minimum. In addition, the fact that approach 2 and approach 3 are both superior to approach 1 shows that the machining parameter optimization during the scheduling course is better for cost control.

When the second batch of jobs arrived after 100 sec, the first batch of jobs was being processed in the light of arranged schedule and parameters. At 15000 sec, the second job of first batch was being processed which caused that the rescheduling occurred at the completion

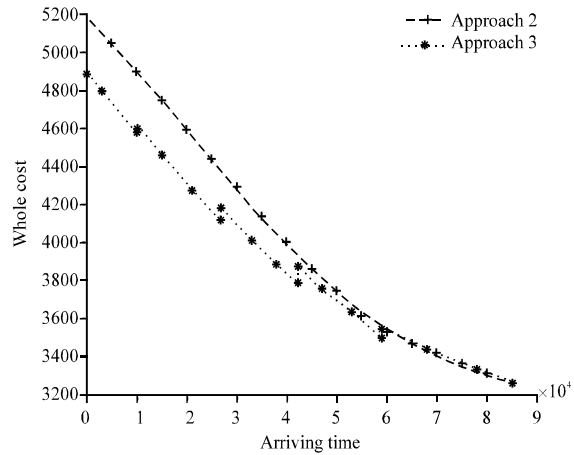


Fig. 1: Relation between the change of whole cost and different arriving time

Table 1: Experimental conditions

Parameter	Values
Tool	
Material	Ceramics
Types	Nip
r_c (mm)	0.8
t_s (sec)	30
C_t (RMB)	600
Machine	
n	2r/min, 140r/min
F_{max} (N)	5000
P_{max} (W)	55000
Transmission coefficient (η)	0.7
f	0.05mm/r, 0.8mm/r
Other	
C_T	75600
m_1	0.3
m_2	0.35
m_3	1.2
C_m (RMB)	0.006

Table 2: Parameters of jobs

Dimension (mm)	Cutting						
	Number	allowance	R_a	S1	t_c	w	a_p
J_1 : 1700×700	4	4	3570	245	0.0024	1.0	
J_2 : 1680×1000	3	5	8400	238	0.003	1.2	
J_3 : 1897×680	3	4	5159.8	233	0.0028	1.0	
J_4 : 1730×500	4	4	3460	240	0.002	1.1	
J_5 : 1150×600	4	5	3450	246	0.0027	1.5	
J_1^* : 746×2032	3	4	6063	240	0.0025	1.2	
J_2^* : 900×2690	3	4	9684	236	0.002	1.4	
J_3^* : 800×2000	4	3	4800	234	0.0032	1.3	
J_4^* : 928×3300	2	5	15312	248	0.0026	1.5	

In addition, $Q = Q' = 1000$, $l = l' = 0.02$, $r = r' = 0.05$, This job belongs to the second batch

of J_2 , so J_2 and J_3 obeyed the former machining parameters and other jobs of first batch obeyed the result of rescheduling.

Influence of different arriving time to whole cost: The curves of Fig. 1 are used to denote the change of whole cost along with different arriving time. In the Fig. 1, the curve of approach 2 is got by 4 times polynomial fitting and each subsection of approach 3 is fit by two time's polynomial.

Figure 2-4 shows, that the whole costs descend along with the arriving time increasing but the trend becomes moderating. The reason for moderating is that the percentage of WIP cost and penalty cost descends. To approach 3, the arriving time affects the number of jobs participating in the rescheduling and affects the machining parameters and schedule of jobs. Therefore, the curve has the shape of subsection and the time of each subsection point is the time for substitutions of the jobs of first batch.

In addition, along with the arriving time increasing, the difference between the whole costs of the two approaches is less. It shows that the more jobs participating in the rescheduling, the better effect for cost control.

Influence of rescheduling cost coefficient r: The curve to denote the change of whole cost along with rescheduling cost coefficient r is as Fig. 2, 3 and 4 with 4 times polynomial fitting.

Figure 2-4 shows that the whole cost increases along with r increasing linearly and to judge by the value of y-axis, the slope of the line will be minished along with the arriving time increase. The reason is that along with the arriving time increasing, the number of jobs participating in rescheduling descends and the influence of rescheduling to the whole cost is weakened.

Table 3: Calculation result

	Approach 1		Approach 2		Approach 3	
	f	v	f	v	f	v
J_1	0.71	0.80	0.62	1.52	0.71	1.52
J_2	0.62	1.14	0.71	1.14	0.52	2.17
J_3	0.71	0.77	0.71	1.48	0.71	1.48
J_4	0.62	1.08	0.71	1.08	0.71	1.60
J_5	0.71	0.68	0.71	1.30	0.71	1.30
J_1'	0.71	0.85	0.71	1.62	0.71	1.62
J_2'	0.62	1.02	0.52	1.95	0.52	1.95
J_3'	0.71	0.91	0.71	1.74	0.71	1.74
J_4'	0.62	1.06	0.52	2.01	0.52	2.01
Whole cost	5152.6		4742.09		4451.67	
Optimal	5-4-2-1-3		5-3-1-4-2-3'		5-3-3'-1'	
Schedule	-3' -1'-4' -2'		-1'-4'-2'		-1-4-2 -4'-2'	

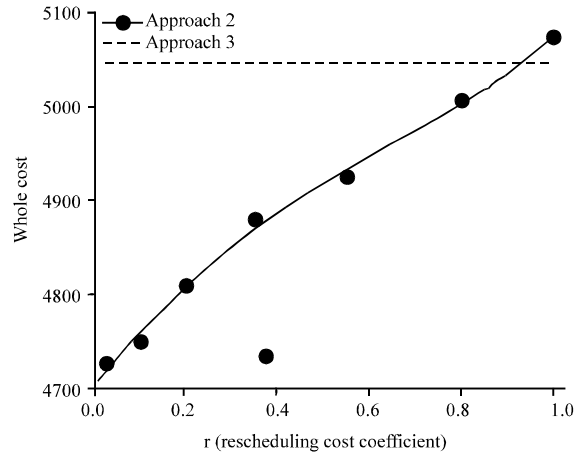


Fig. 2: Relationship between r and whole cost for 5000 sec

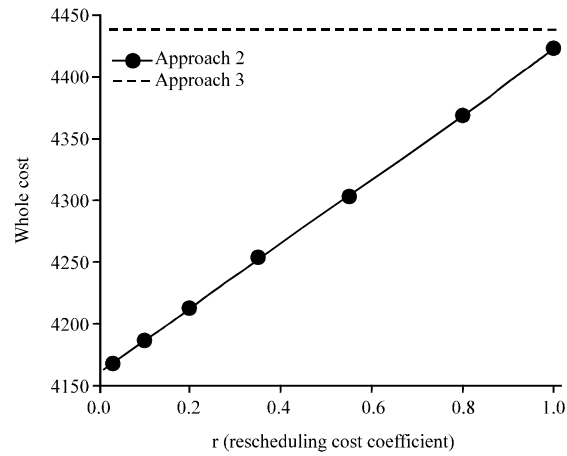


Fig. 3: Relationship between r and whole cost for 25000 sec

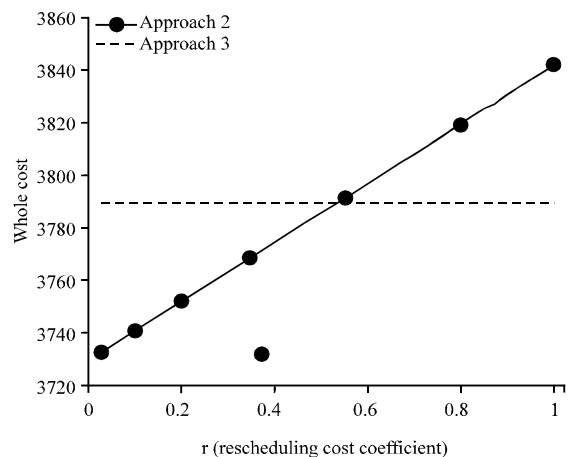


Fig. 4: Relationship between r and whole cost for 48000 sec

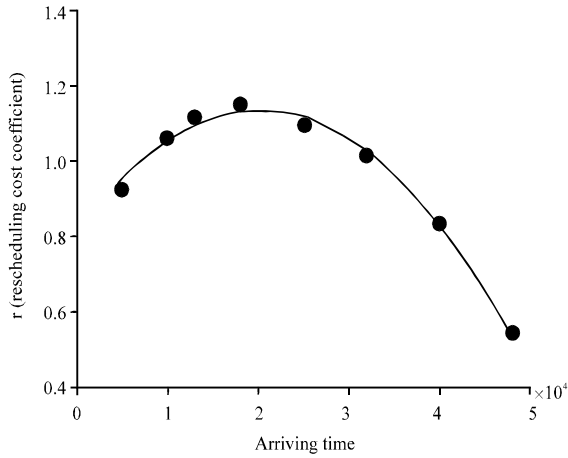


Fig. 5: Change for available range of r along with arriving time

In addition, when r increases to some value, the whole cost with approach 3 will be greater than the cost with approach 2. That is to say, the validity of rescheduling for cost control is limited by the rescheduling cost coefficient. The valid range can be changed with the arriving time of jobs and the changing law can be described by the curve with 2 times polynomial fitting in Fig. 5.

Therefore, we can judge the value of rescheduling according to Fig. 5. If the coordinate is above the curve, then the rescheduling is lost its significance. Contrarily, the farther the coordinate is below the curve, the more significant the rescheduling is. So how to use rescheduling correctly should be considered cautiously in the light of production status.

CONCLUSION

This study built the model for multi-job and multi-batch single machine scheduling to optimize the machining parameters during scheduling. The validity of the model and algorithm are validated by an example. According to the research, the conclusions as follows can be summarized:

- In multi-job and multi-batch single machine scheduling, machining parameters optimization during the scheduling course is more effective for cost control
- The whole costs descend along with the arriving time increasing but the trend is unmonotone and

becomes moderating. The value of the whole cost is discontinuous at the job-substitution time of the last batch

- The whole cost increases linearly and the slope of the line will be diminished along with the arriving time increasing
- The valid range of rescheduling can be changed with the arriving time of jobs as a parabola

REFERENCES

Armarego, E.J.A., 1994. Machining performance prediction for modern manufacturing. Proceedings of the 7th International Conference on Production and Precision Engineering and 4th International Conference on High Technology (4th ICHT), 1994, Chiba, Japan, pp: 215-220.

Ballfou, R.H., 1999. Business Logistics Management: Planning, Organizing and Controlling the Supply Chain. 4th Edn., Prentice Hall International Inc., USA., ISBN-13: 9780130812629, pp: 45-53.

Biskup, D. and T.C.E. Cheng, 1999. Single machine scheduling with controllable processing times and earliness, tardiness and completion time penalties. Eng. Optim., 31: 329-336.

Budake, E., Y. Altintasy and E.J.A. Armarego, 1996. Prediction of milling force coefficients from orthogonal cutting data. J. Manuf. Sci. Eng., 118: 216-224.

Chen, D.W. and F. Zheng, 2001. A new kind of controllable scheduling problems. OR Trans., 5: 27-34.

Church, L.K. and R. Uzsoy, 1992. Analysis of periodic and event-driven rescheduling policies in dynamic shops. Comput. Integr. Manuf., 5: 153-163.

Faria, J., M. Matos and E. Nunes, 2006. Optimal design of work-in-process buffers. Int. J. Prod. Econ., 99: 144-155.

Jain, A.K. and H.A. Elmaraghy, 1997. Production scheduling/rescheduling in flexible manufacturing. Prod. Res., 35: 281-309.

Lawler, E.L., 1977. A pseudopolynomial algorithm for sequencing jobs to minimize total tardiness. Ann. Discrete Math. Elsevier, 1: 331-342.

Pinedo, M., 1995. Scheduling: Theory, Algorithms and System. Prentice Hall, Englewood Cliffs, NJ, USA., ISBN-13: 9780137067572, Pages: 378.

Rohleder, T.R. and G.D. Scudder, 1993. Comparing performance measures in dynamic job shops: Economics vs. time. Int. J. Prod. Econ., 32: 160-183.

- Saravanan, R., P. Asokan and M. Sachithanandam, 2001. Comparative analysis of conventional and non-conventional optimisation techniques for CNC turning process. *Int. J. Adv. Manuf. Technol.*, 17: 471-476.
- Shafaei, R. and P. Brunn, 1999. Workshop scheduling using practical (inaccurate) data Part 1: The performance of heuristic scheduling rules in a dynamic job shop environment using a rolling time horizon approach. *Int. J. Prod. Res.*, 37: 3913-3925.
- Vickson, R.G., 1980. Choosing the job sequence and processing times to minimize total processing plus flow cost on a single machine. *Oper. Res.*, 28: 1155-1167.