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A Novel Satellite Selection Method for Satellite Navigation System Based on Genetic Algorithm

Huo Hangyu, Zhang Xiaolin, Chen Canhui and Cao Xiangrong
School of Electronics and Information Engineering,
Beijing University of Aeronautics and Astronautics, Beijing, 100191, China

Abstract: In order to achieve real-time selection of navigation satellites in multi-constellations navigation system, a novel satellite selection method named Genetic Satellite Selection Method (GSSM) is proposed. Combined with the basic idea of genetic algorithm and the feature of multi-constellations navigation system, a fast crossover operator and mutation operation is described. The experiment results show that, in the satellites selection process, the GSSM can effectively reduce 98.9% computation comparing to the traditional optimal Geometric Dilution of Precision (GDOP) method. From the view of the overall navigation system, it can also reduce almost 73% computation.

Key words: Satellite navigation, genetic algorithm, geometric dilution of precision, satellite selection

INTRODUCTION

In recent years, satellite navigation system has been playing an increasing role in various areas of the society. From now on, more than 100 navigation satellites work in the space, coming from GPS, GLONASS, Galileo and COMPASS. For the better positioning accuracy and system reliability, the multi-constellations navigation has become a hot issue. But on the other hand, the computation of navigation system will sharply increased with more satellites. In most case, the traditional satellites selection method can't meet the real-time requirement in the multi-constellations navigation system, especially for the high dynamic environment (Zhang *et al.*, 2000; Li *et al.*, 2007; Zhang *et al.*, 2007; Jin *et al.*, 2009).

This study propose a novel satellite selection method based on genetic algorithm, including the visible satellites selection method, a fast crossover and mutation design which will effectively reduce the computation of navigation system to meet the real-time requirement in the multi-constellations environment.

GENETIC SATELLITE SELECTION METHOD

Mathematical description of satellite selection: In satellite navigation system, the purpose of satellite selection is to select the optimum subset of satellites which can provide the best navigation result. The mathematical description is under below:

- $n \in \mathbb{N}, m \in \mathbb{N}$ and $n > m$
- $\exists X_k = [x_n, x_{n-1}, \dots, x_1], x_j = 1$ or $0, j = 1, \dots, n$: meeting

$$\sum_{j=1}^n x_j = m$$

- to find $X_0 \in \{X_k\}$, meeting $GDOP(X_0) = \min\{GDOP(X_k) \leq GDOP_T\}$

where, n is the number of visible satellites; m is the number of selected satellites; k is the number of m -satellite subset; X_k is the selected satellites scenario; $GDOP(X_k)$ is $GDOP$ of X_k ; X_0 is the selected satellite solution $GDOP_T$; is the $GDOP$ threshold which meets positioning accuracy requirement.

Coding scheme: Satellite selection scenario uses binary encoding. Each visible satellite is treated as a gene and is assigned a binary value '1' or '0'. '1' of $X_k = [x_n, \dots, x_j, \dots, x_1]$ indicates that the corresponding satellite is selected.

Fitness function: The objective function of satellite selection (Eq. 1):

$$f_0(X) = GDOP(X) \quad (1)$$

where, X represents the scheme of satellite selection.

The fitness function in GSSM is as follows (Eq. 2):

$$f(X) = \frac{GDOP_{max} - f_0(X) + \epsilon}{GDOP_{max} - GDOP_{min} + \epsilon} \quad (2)$$

where, $GDOP_{max}$ and $GDOP_{min}$ denote the maximum and minimum of GDOP of current population, respectively, ϵ is a constant, $\epsilon \in (0,1)$.

Crossover operators: According to the characteristics of satellite selection, the number of selected satellites should be the constant. A new crossover operator named One Matched Crossover (OMX) is proposed. Under the constraint, it will ensure that all of the crossover offspring will not out of the range of parent and it can also guarantee that the satellites with better GDOP will not be eliminated.

We suppose m is the numbers of selected satellites. The steps of OMX can be described as follows:

- Step 1:** Two individuals (parents) are randomly selected with a probability p_c , called the crossover probability. And then randomly generating an integer of $1 \sim (m-1)$, the integer represents the numbers which will be used to cross those selected satellites. That means the selected satellites whose serial number is lower will be utilized in crossover operator
- Step 2:** Produce original offspring by interchanging the badge of selected satellites of parents
- Step 3:** Ascertain the mapping relationship of interchanged satellites
- Step 4:** Legalize offspring based on the mapping relationship

A specific example of OMX is demonstrated below. Assuming there are 16 visible satellites and 8 satellites need to be selected.

- Select two individuals randomly

Parent 1: 0111100101110000, the serial number of selected satellites is: 15, 14, 13, 12, 9, 7, 6, 5

Parent 2: 0001100101011110, the serial number of selected satellites is: 13, 12, 9, 7, 5, 4, 3, 2

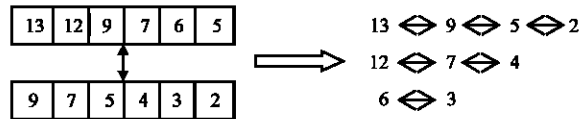
The integer 6 has been generated randomly.

- Produce original offspring by interchanging the latter 6 selected satellites

Child 1: 0110000101011110, the serial number of selected satellites is: 15, 14, 9, 7, 5, 4, 3, 2

Child 2: 0001100101110000, the serial number of selected satellites is: 13, 12, 9, 7, 6, 5

- Ascertain the mapping relationship:



- Legalize the offspring based on the mapping relationship

From the above, we can know the satellite 13 and 12 of Parent 2 should be replaced with satellite 2 and 4, respectively and the exchanged satellites will be maintained. Then two legal offspring (feasible solutions) are reconstructed as follows:

Child 1: 0110000101011110, the serial number of selected satellites is: 15, 14, 9, 7, 5, 4, 3, 2

Child 2: 000110010111010, the serial number of selected satellites is: 13, 12, 9, 7, 6, 5, 4, 2

Mutation operator: Simile to the crossover operator, mutation operator also has to guarantee that the number of selected satellites of individual has exactly the same quantity in satellite selection. According to the requirement, a kind of new mode, dual genes '01' relative mutation, is proposed in GSSM.

Assuming the number of visible satellites is n , the detailed operating steps of this mutation operator are as follows:

- Step 1:** An individual C_p is selected randomly with a certain probability p_m known as the mutation probability
- Step 2:** A random integer g_1 is generated with $1 \sim n$ interval
- Step 3:** Judge the type of the g_1 th gene of individual C_p . If the g_1 th gene is 0, another integer g_2 ($g_2 \neq g_1$) is generated randomly with $1 \sim n$ interval and it ought to ensure that the g_2 th gene of individual C_p is 1. Otherwise, if the g_1 th gene is 1, the corresponding gene of integer g_2 should be 0
- Step 4:** Change the g_1 th and g_2 th genes of individual C_p (a 0 is converted to 1 and vice versa)

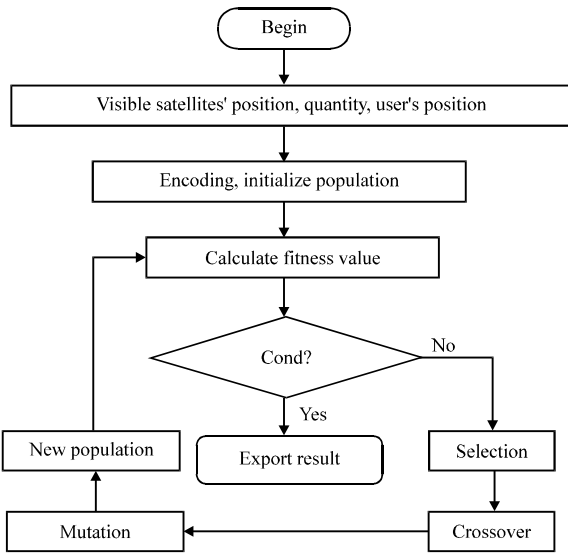


Fig. 1: Flowchart of GSSM

Selection strategy: The population size in satellite selection is smaller and the preferable constellations ought not to be eliminated. So, a larger sample space is employed in GSSM. It can ensure that parents and offspring have the same competition chance. The roulette wheel selection is utilized to obtain the new crossover and mutation population. The selection strategy can improve the performance of genetic algorithm by increasing crossover probability and mutation probability and selection will not cause too much random variation by high crossover probability and mutation probability.

Termination principle of GSSM: The computational process will be terminated when the GDOP of the individual meets the constraint $\min \text{GDOP}(X_k) \leq \text{GDOP}_T$. Furthermore, in order to ensure the efficiency of iterative operation, a maximum evolutionary generation is also defined.

Figure 1 shows the flowchart of GSSM.

EXPERIMENT RESULTS

Basing on the compatible GPS/COMPASS receiver platform, we implement the semi-physical simulation of the method proposed in this paper. The satellite data is generated from the navigation signal source which contains 32 GPS satellites and 12 COMPASS satellites. The navigation receiver is implemented on the FPGA and DSP.

Performance analysis of GSSM under different GDOP_T : GDOP_T decides the accuracy of navigation system. In

order to meet the availability requirement of the satellite navigation system, Position Dilution of Precision (PDOP) should not be more than 6 (Kaplan and Hegarty, 2007). We analyze the performance of GSSM under different GDOP_T (2.5, 3, 3.5, 4, 4.5, 5, 5.5 and 6). The number of selected satellites is taken as 8 to meet the system fault detection.

According to RTCA D0-2229D standard, the mask angle is assumed to be 5° . Simulation time is 24 h. The sampling interval is 5s. Based on twenty-seven stations of Crustal Moment Observation Network of China, we do the simulation of OMX under the GPS and COMPASS dual-constellation navigation system.

Analysis of validity: Figure 2-5 shows the temporal variation of GDOP and GDOP_T within 24 h in SUIY, TASH, YONG and XIAA station after satellite selection under GDOP_T 2.5, 3, 4 and 6. Table 1 is a statistical analysis of GDOP

From Fig. 2-5 and Table 1, the following conclusions can be drawn:

- The $\overline{\text{GDOP}}$ after satellite selection were less than GDOP_T for the four observatories station
- The temporal variation of GDOP after satellite selection is smooth for the four observatories station
- The probability of GDOP after satellite selection less than GDOP_T increased with the increase of GDOP_T . When GDOP_T is between 2.5 and 4, almost all case (96.99%) is meet GDOP requirement. When GDOP_T is between 4 and 6, no case is failed

Analysis of computation complexity of satellite selection:

Figure 6-9 shows the temporal variation of evolution algebra N_g for satellite selection within 24 h in SUIY, TASH, YONG and XIAA station with different GDOP_T . Table 2 is a statistical analysis of N_g .

From Fig. 6-9 and Table 2, the following conclusions can be drawn:

- The N_g of satellite selection decreases with the increase of GDOP_T
- When $\text{GDOP}_T = 6$, only one evolution is needed to finish satellite selection
- When $\text{GDOP}_T = 4$, 98% satellite selection can be finished within 3 evolutions at most
- When $\text{GDOP}_T = 3$, 98% satellite selection can be finished within 6 evolutions and 95% satellite selection can be finish within 2 evolutions
- When $\text{GDOP}_T = 2.5$, most satellite selection needs much more evolutions

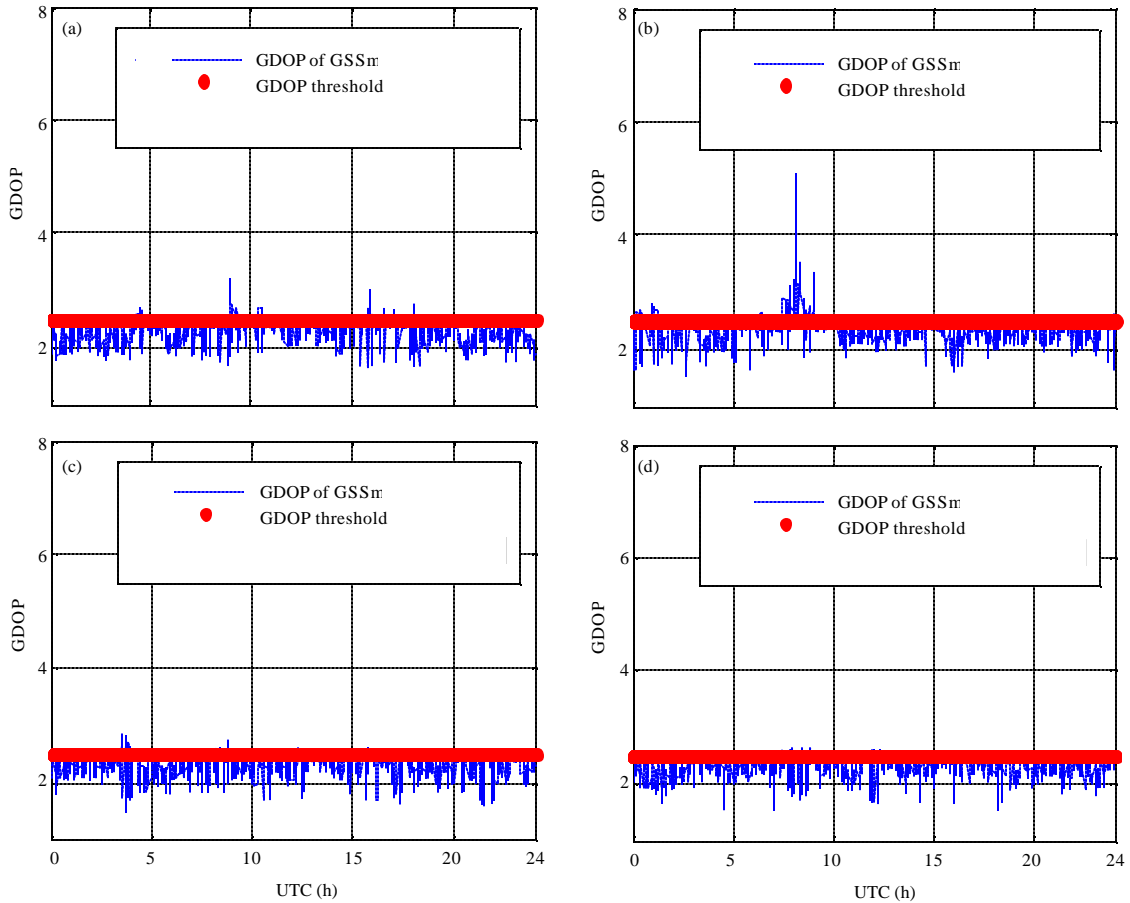


Fig. 2(a-d): GDOP and GDOP_T after satellite selection (GDOP_T = 2.5). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

Table 1: GDOP Statistics after satellite selection under different GDOP_T

Station	GDOP _T	GDOP _{min}	GDOP _{max}	$\overline{\text{GDOP}}$	GDOP _{var}	P(GDOP >> GDOP _T) (%)
SUIY	2.5	1.534	4.259	2.275	0.040	97.56
	3.0	1.510	3.921	2.373	0.080	99.99
	4.0	1.521	4.000	2.394	0.105	100.00
	6.0	1.529	4.027	2.395	0.105	100.00
TASH	2.5	1.301	5.116	2.333	0.050	96.99
	3.0	1.552	5.287	2.446	0.080	99.87
	4.0	1.479	3.991	2.469	0.110	100.00
	6.0	1.543	4.223	2.468	0.111	100.00
XIAA	2.5	1.413	3.018	2.305	0.030	98.16
	3.0	1.583	3.000	2.420	0.066	100.00
	4.0	1.639	3.837	2.439	0.081	100.00
	6.0	1.589	3.967	2.437	0.081	100.00
YONG	2.5	1.453	2.820	2.291	0.030	98.54
	3.0	1.517	3.000	2.388	0.061	100.00
	4.0	1.481	3.518	2.393	0.065	100.00
	6.0	1.509	3.533	2.394	0.067	100.00

Analysis of computation complexity of overall navigation:

In satellite navigation system, the observation equation is (Eq. 3):

$$y = Hx + \epsilon \tag{3}$$

where, $H \in \mathbb{R}^{n \times l_{sys}}$ is the measurement matrix; $x \in \mathbb{R}^{l_{sys}}$ is the state vector; $\epsilon \in \mathbb{R}^{l_{sys}}$ is the measurement error; $y \in \mathbb{R}^n$ is the measurement vector; n is the number of visible satellites; l_{sys} is the state variable dimension:

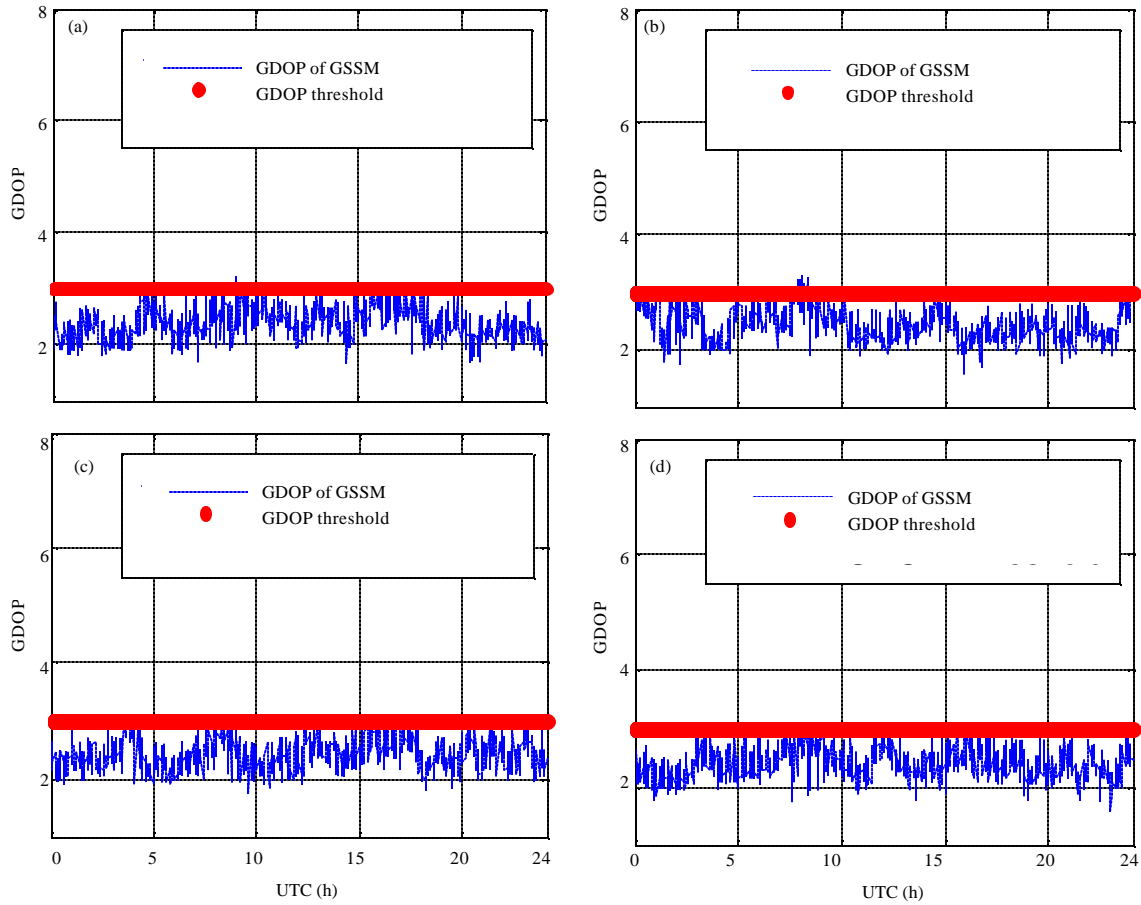


Fig. 3(a-d): GDOP and GDOP_T after satellite selection (GDOP_T = 3). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

Table 2: Ng Statistics of satellite selection under different GDOP_T

Station	GDOP _T	Ng _{min}	Ng _{max}	Ng	Ng _{var}	Ng _{0.95}	Ng _{0.98}
SUIY	2.5	1	59	3.081	28.751	14	23
	3.0	1	36	1.127	0.980	1	3
	4.0	1	3	1.000	0.001	1	1
	6.0	1	1	1.000	0.000	1	1
TASH	2.5	1	65	4.115	41.411	19	26
	3.0	1	38	1.386	5.264	2	6
	4.0	1	2	1.000	0.000	1	1
	6.0	1	1	1.000	0.000	1	1
XIAA	2.5	1	53	3.149	25.552	14	21
	3.0	1	14	1.082	0.254	1	2
	4.0	1	1	1.000	0.000	1	1
	6.0	1	1	1.000	0.000	1	1
YONG	2.5	1	52	2.659	18.816	11	19
	3.0	1	7	1.019	0.037	1	1
	4.0	1	1	1.000	0.000	1	1
	6.0	1	1	1.000	0.000	1	1

Remark: Ng_{0.95} is a minimum evolution algebra which meeting p(GDOP ≤ GDOP_T) ≥ 0.95 Ng_{0.98} is a minimum evolution algebra which meeting p(GDOP ≥ GDOP_T) ≥ 0.98

Table 3: Amount of computation to position statistics

	Amount of computation		
	Before satellite selection	After satellite selection	Difference
Addition	188700	52300	136400
Multiplication	190450	54450	136000

Equation 4 is the least squares method. There is five-dimensional state variables, for dual constellation integrated navigation system, I_{sys} = 5. The average number of visible satellites approximately equal to 19. The number of selected satellites is taken as 8. Table 3 give the amount of calculation of the least square estimation algorithm (number of iterations is assumed for 50 times). We can conclude that the amount of addition decreases 72.3% and the amount of multiplication decreases 71.4%.

Performance compared with GSSM and optimal GDOP method: The purpose of the optimal GDOP method of satellite selection is to find the subset with minimal GDOP

$$\hat{x} = (H^T H)^{-1} H^T y \tag{4}$$

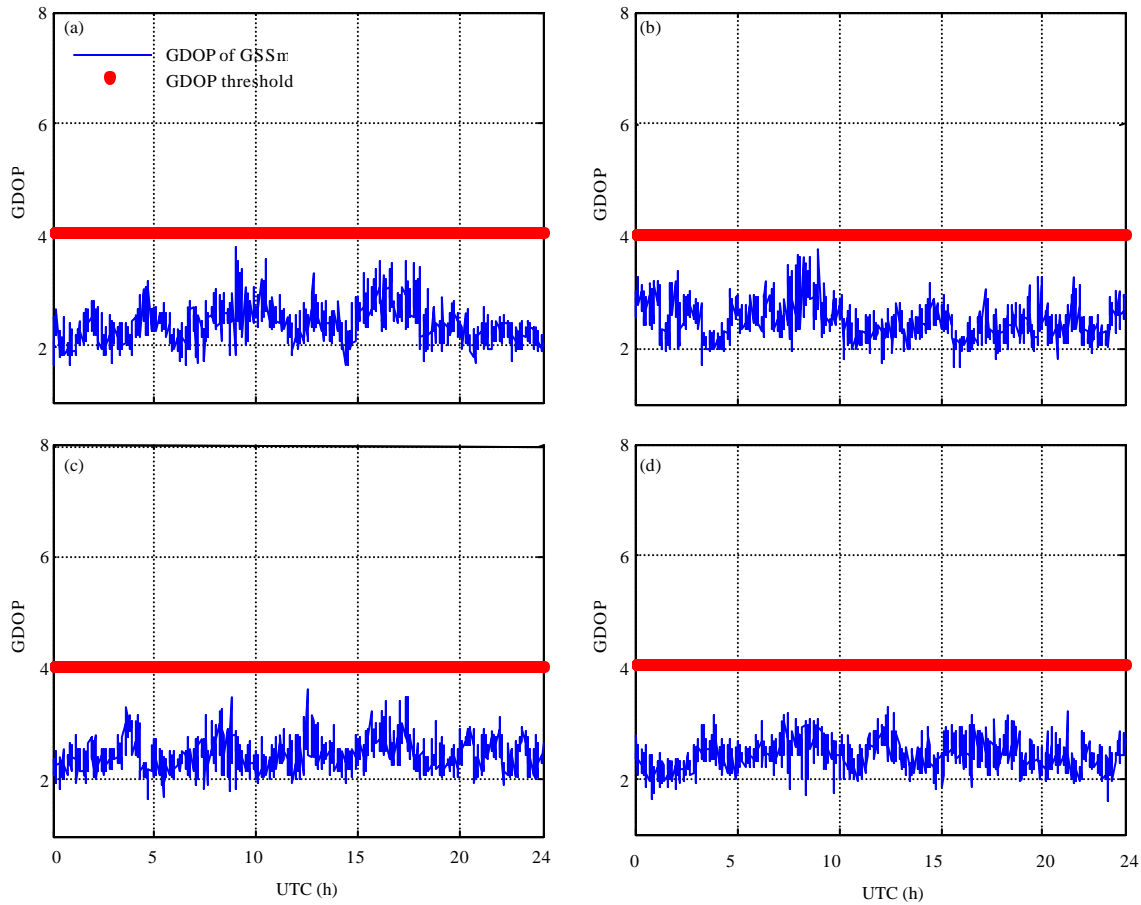


Fig. 4(a-d): GDOP and $GDOP_T$ after satellite selection ($GDOP_T = 4$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

Table 4: GDOP Statistics after satellite selection

Station	$GDOP_{min}$	$GDOP_{max}$	\overline{GDOP}	$GDOP_{var}$	$P(GDOP_{GSSM} \leq GDOP_{Optimal})$
SUIY	2.182	3.689	2.631	0.073	0.806
TASH	2.179	3.872	2.695	0.070	0.785
XIAA	2.243	3.676	2.692	0.073	0.841
YONG	2.159	3.317	2.587	0.052	0.774

in all satellite subsets. GSSM cares about the final positioning accuracy instead of the GDOP which will reduce the complexity of computation. Therefore, when comparing these two methods, we should focus on the complexity under the same discrepancy of GDOP after satellite selection. In the comparative analysis, the number of selected satellites is taken as 5. And $GDOP_T$ is taken as 6; the number of selected satellites is taken as 8.

Comparison of GDOP after satellite selection: Figure 10 shows the temporal variation of GDOP after satellite selection in GSSM and GDOP with the optimal GDOP method. Table 4 is a statistical analysis of GDOP. The following conclusions can be drawn:

- The \overline{GDOP} after satellite selection with GSSM were less than the optimal GDOP method 9.9, 9.2, 10.5 and 8.1%, respectively for the four observatories station
- The GDOP after satellite selection with the GSSM were less than the optimal GDOP method which probability not less than 77.4%

Comparison of Computation for satellite selection: Table 5 shows the statistical analysis of N_{GDOP} which is the number of calculations of GDOP for satellite selection. The following conclusions can be drawn:

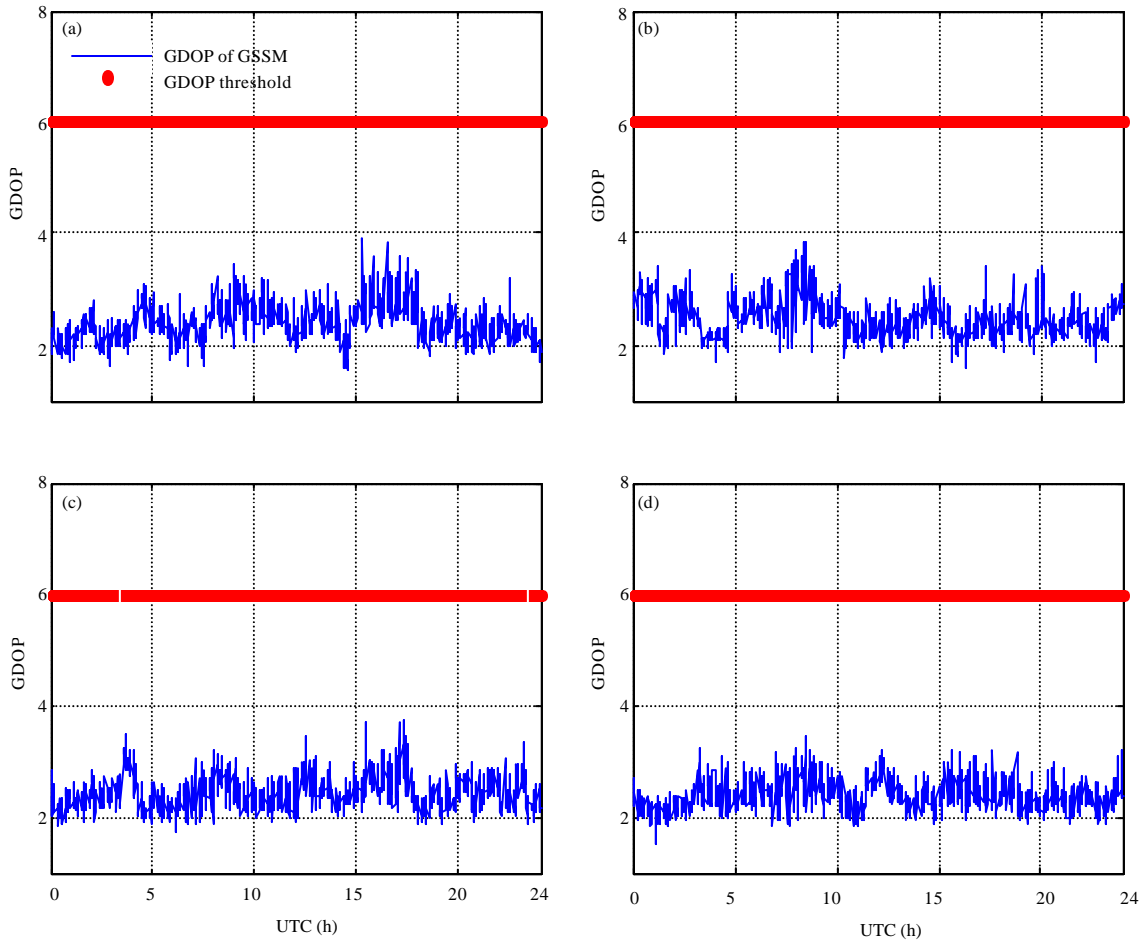


Fig. 5(a-d): GDOP and $GDOP_T$ after satellite selection ($GDOP_T = 6$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

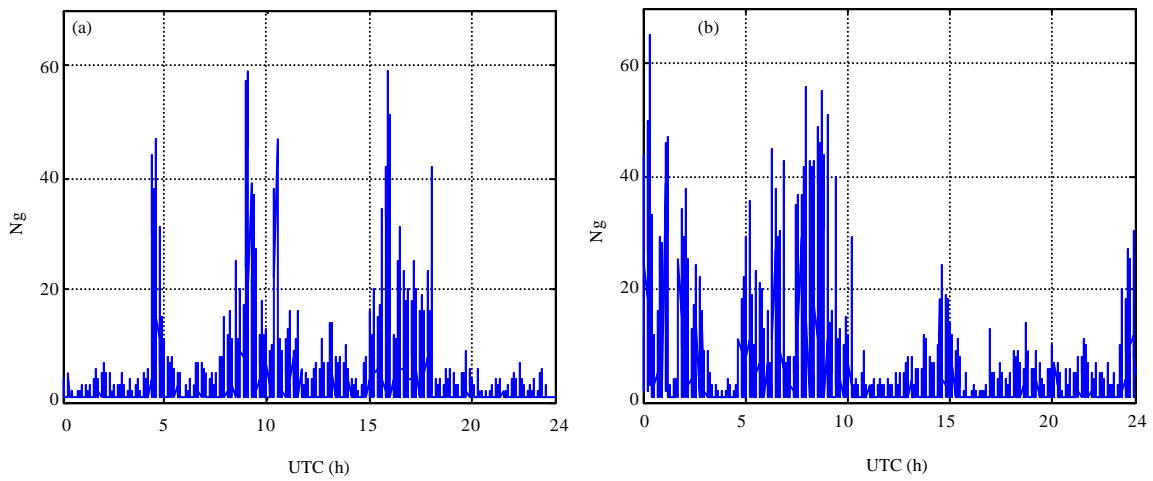


Fig. 6(a-d): Continue

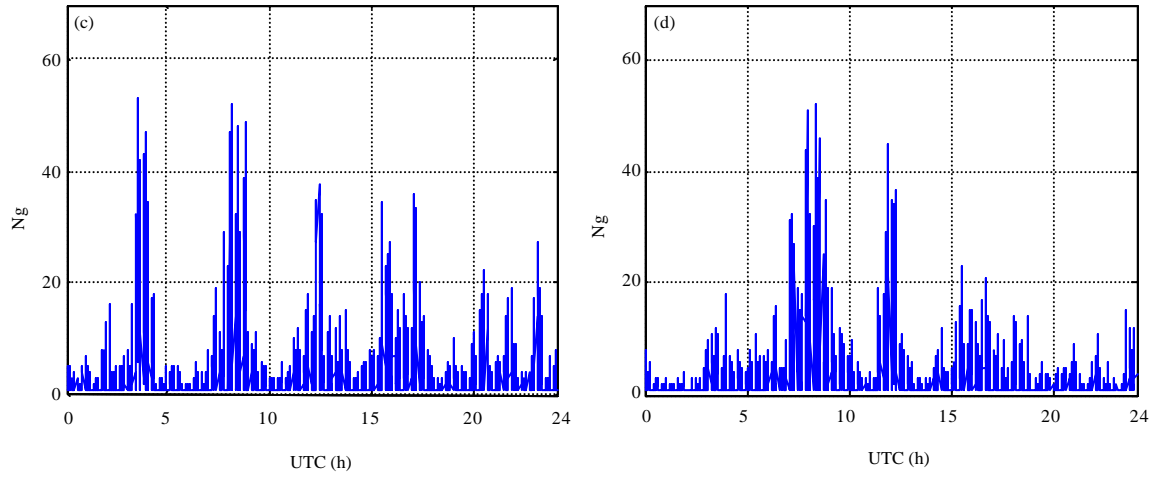


Fig. 6(a-d): N_g after satellite selection ($GDOP_T = 2.5$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

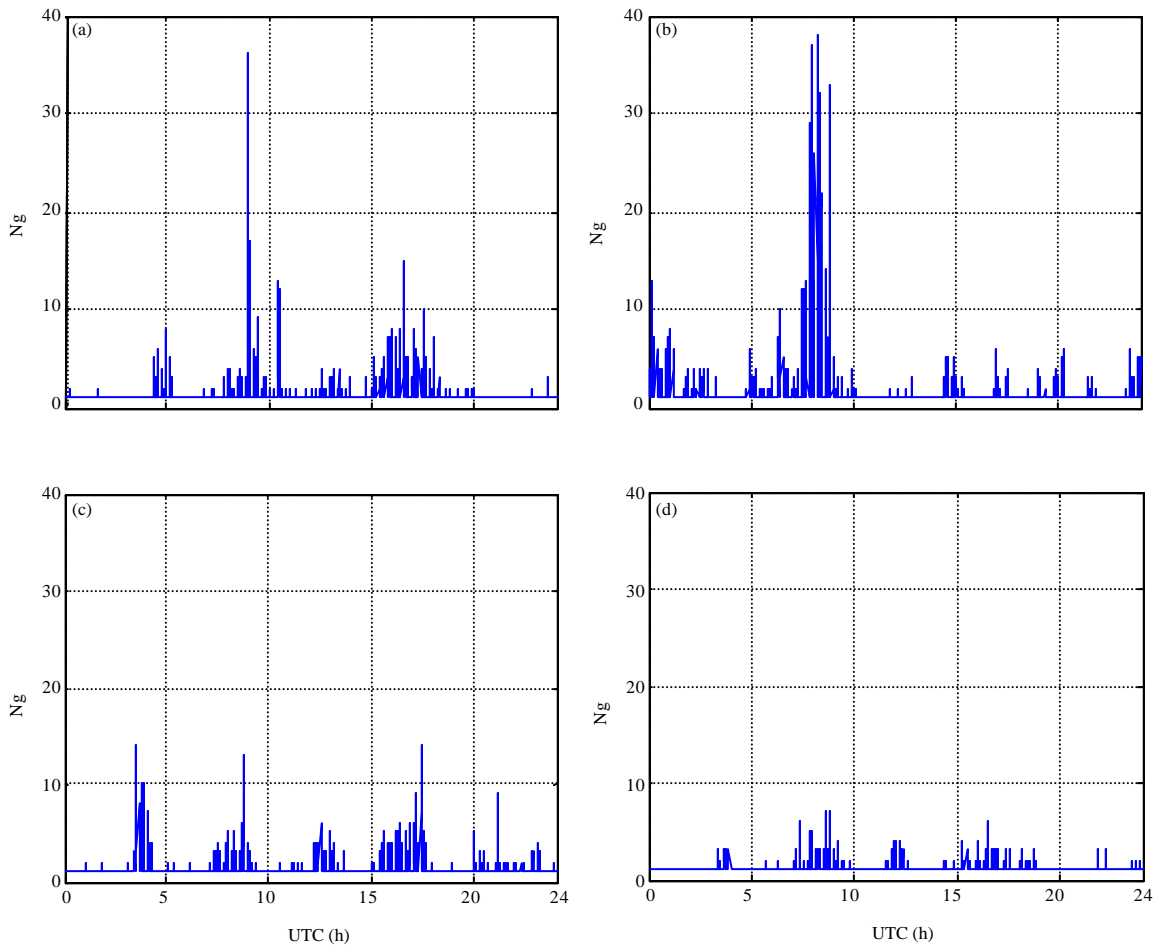


Fig. 7(a-d): N_g after satellite selection ($GDOP_T = 3$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

Table 5: Statistics of N_{GDOP} in the two kinds of method

Station	N_{GDOP} of Optimal				N_{GDOP} of GSSM			
	Minimum	Maximum	Mean	Var	Minimum	Maximum	Mean	Var
SUIY	2002	33649	9204	2.803e+007	22	22	22	0
TASH	2002	20349	7649	1.382e+007	22	22	22	0
XIAA	2002	33649	12314	3.362e+007	22	22	22	0
YONG	3003	42504	17688	9.030e+007	22	22	22	0

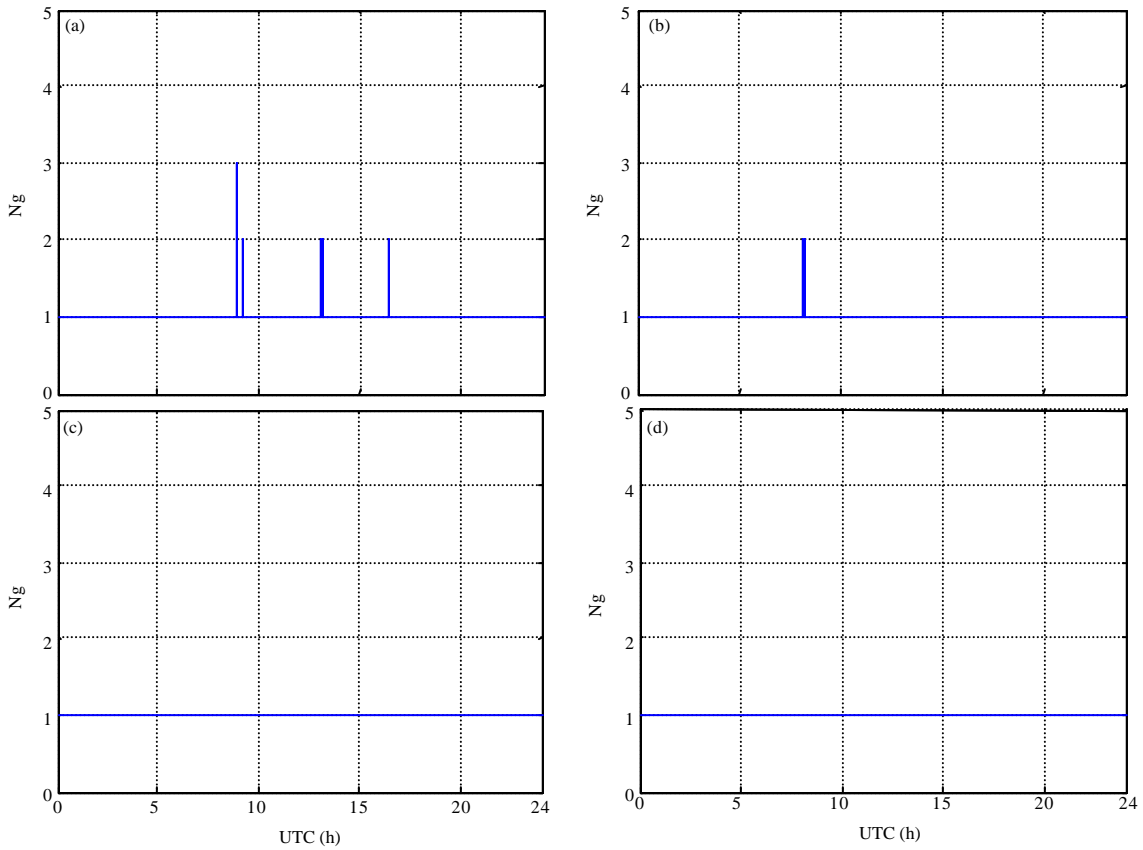


Fig. 8(a-d): N_g after satellite selection ($GDOP_{\tau} = 4$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

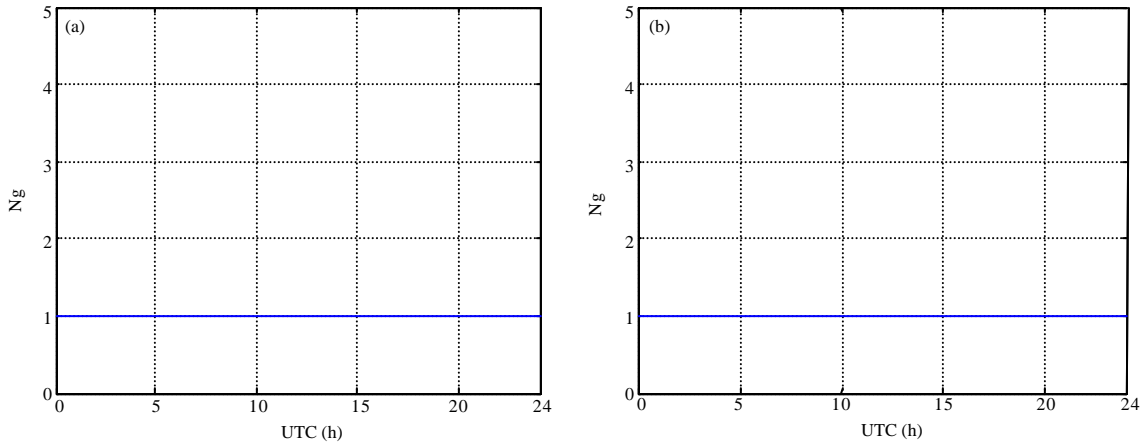


Fig. 9(a-d): Continue

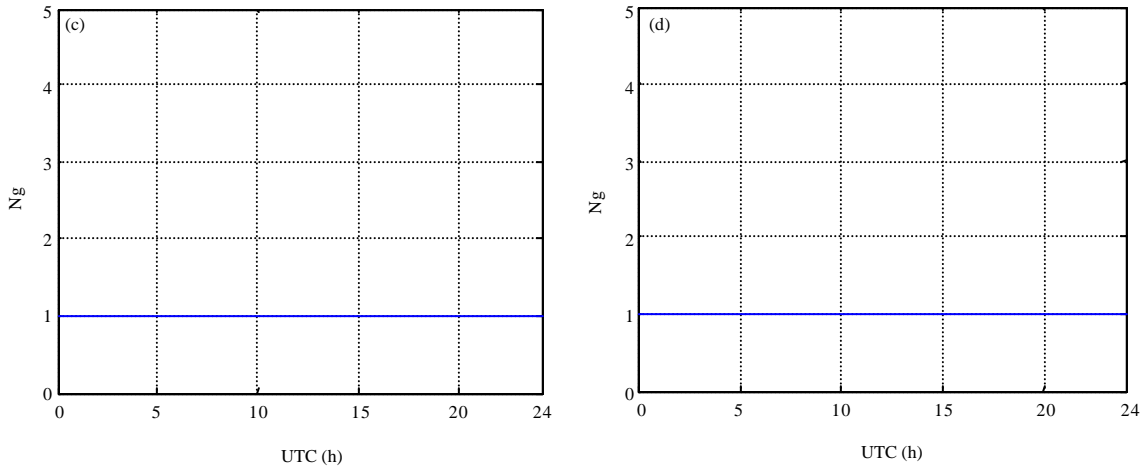


Fig. 9(a-d): N_g after satellite selection ($GDOP = 6$). (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

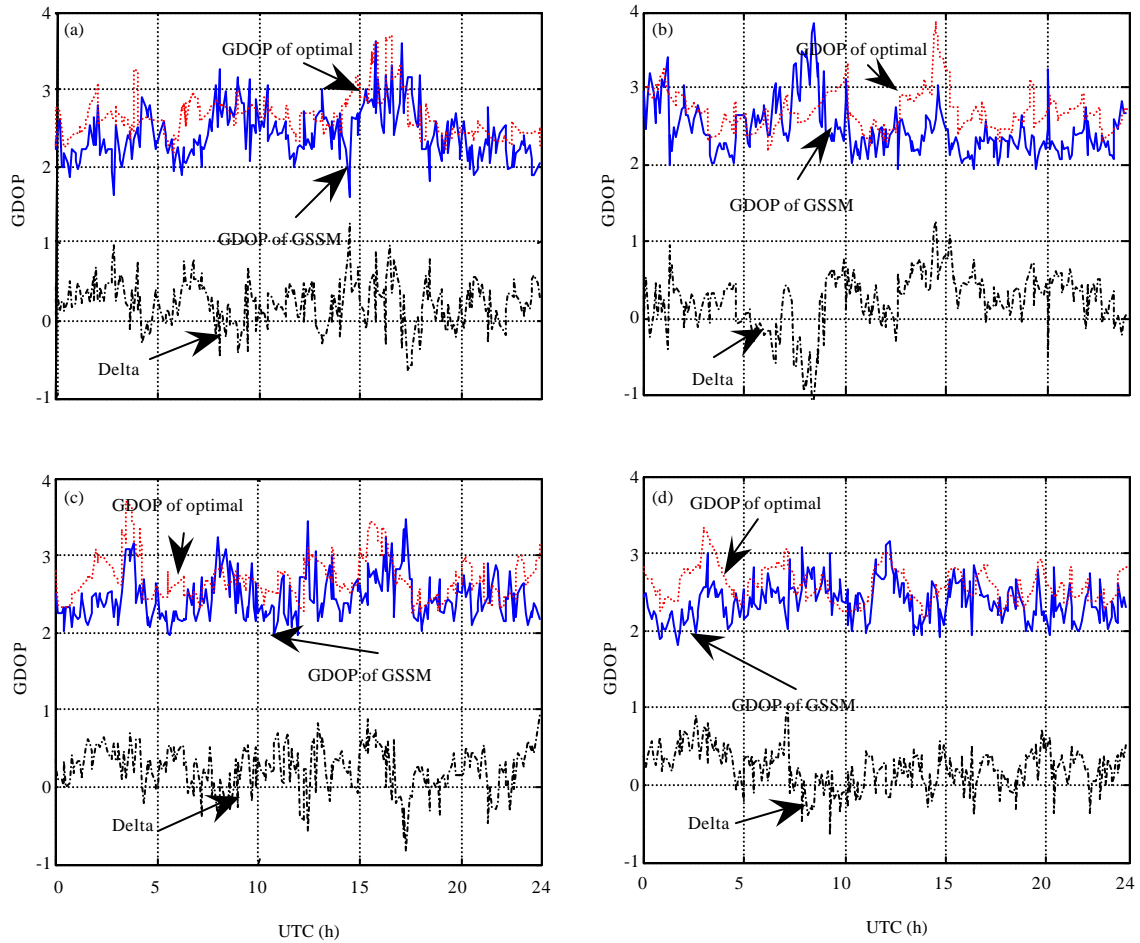


Fig. 10(a-d): GDOP after satellite selection by utilizing two kinds of method and their difference. (a) SUIY, (b) TASH, (c) XIAA and (d) YONG

- The N_{GDOP} for satellite selection with the GSSM were less than the minimum N_{GDOP} for satellite selection with the optimal GDOP method 98.90, 98.90, 98.90 and 99.27%, respectively for the four observatories station
- The average value of N_{GDOP} for satellite selection with the GSSM were less than the optimal GDOP method 99.93, 99.89, 99.93 and 99.95%, respectively for the four observatories station

CONCLUSION

To reduce the computation of satellites selection, a novel satellite selection method, named Genetic Satellite Selection Method, is proposed based on genetic algorithm in the paper. With the help of the fast coding scheme and fitness function process, it can effectively accelerate the satellite selection under the GPS/COMPASS multi constellation navigation system. Our experiment result shows the GSSM is not only improving the real-time performance of

navigation system, but also still meeting the accuracy of locating requirement.

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