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## Unsteady State Modeling and Analysis of a Passive Liquid-feed DMFC

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**Abstract:** A one-dimensional, unsteady state, two phase model has been developed for a liquid-feed DMFC delivery system including the fuel cell itself. The model considers the mass and heat transport in the feed delivery system attached to the anode and cathode of the fuel cell. The effects of feed methanol concentration in the reservoir and current density on mass transport of catalyst layer revealed. It is further revealed that the optimum performance with 4 M methanol concentrations in term of methanol crossover with consideration of time

**Key words:** Unsteady state, passive liquid-feed DMFC

### INTRODUCTION

Passive direct methanol fuel cells are promising high current density compare to battery and have the advantages of high efficiency, reliability, flexibility, durability and easy in maintenance. However, two predominant issues that hinder the application of Direct Methanol Fuel Cell (DMFC) technology are low kinetics of methanol electro-oxidation on the anode catalyst and crossover of un-reacted methanol from the anode to the cathode. Water and thermal management is one of the key factors which ensure its highly efficient steady operation and extend its life-span (Shi *et al.*, 2007). There have already been quite a few investigations on water (Shi *et al.*, 2007; Scharfer *et al.*, 2008; Liu and Wang, 2008) and thermal management (Dohle *et al.*, 2002) for a DMFC. Based on experiment, an increase in temperature primarily has a positive impact on the DMFC performance at the same time increase the methanol crossover (Oedegaard and Hentschel, 2006). Some afford must be done to improve and solve the challenging on fabrication of DMFC.

Majority of the modeling on DMFC are focusing on active system and steady state condition. Thus, we have an unsteady state analytical model for a passive DMFC by taking these two factors into account. Moreover, this model could separate the anodic and the cathodic performances individually with a clear crossover effect. Major voltage losses of the DMFC can then be identified from its power delivery curve. In this work, we selected an in-house passive DMFC constructed with known and estimated parameters as a base cell to validate to our

model. Modeling work then started with various parameters such as catalyst loadings, thickness and methanol concentrations. The impacts of these parameters individually or in combination on the efficiency of the passive DMFC were analyzed and discussed.

### MODEL DEVELOPMENT

The model considers a passive-feed DMFC for 1 dimension system which consists of anode flow channel AFC, anode backing layer ABL, anode catalyst layer ACL, membrane, cathode catalyst layer CCL, cathode diffusion layer CDL and cathode flow channel CFC. Figure 1 represents the layer consideration in the single cell of DMFC. On the anode, methanol from solution tank diffused in anode backing layer to anode catalyst layer.

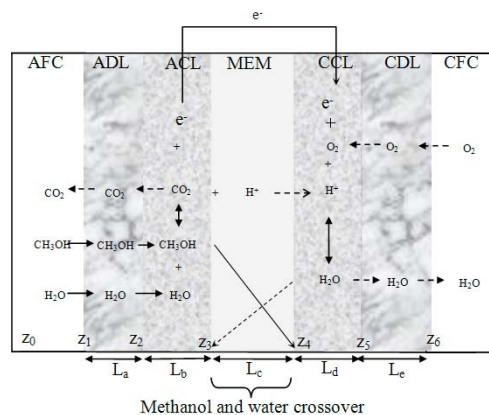


Fig. 1: A schematic diagram of a passive liquid-feed DMFC

Table 1: Mass balance

Layer	Heat
Anode diffusion layer	$N_M = D_a^{eff} \frac{\partial C_M}{\partial z} = \sqrt{D_a^{eff} / \pi t} e^{-z^2 / 4 D_a^{eff} t} (C_b - C_{M})$ (1)
Anode catalyst layer	$\frac{\partial C_M}{\partial t} = D_a^{eff} \frac{\partial^2 C_M}{\partial z^2} - k C_M$ (2)
Mem-brane	$N_M = \sqrt{D_c^{eff} / \pi t} e^{-z^2 / 4 D_c^{eff} t} C_M + \xi_M C_M \frac{I_{a,CL}}{F} + k_p C_M \frac{\Delta P}{L_c}$ (3)
Cathode catalyst layer	$\frac{\partial C_{O_2}}{\partial t} = D_c^{eff} \frac{\partial^2 C_{O_2}}{\partial z^2} - k C_{O_2}$ (4)
Cathode diffusion layer	$N_{O_2} = D_c^{eff} \frac{\partial C_{O_2}}{\partial z} = \sqrt{D_c^{eff} / \pi t} e^{-z^2 / 4 D_c^{eff} t} (C_{O_2} - C_{O_2})$ (5)

**Heat transport:**

Table 2: Heat balance

Layer	Heat
Anode diffusion layer	$\frac{\partial T}{\partial x} = \alpha \frac{(T_{ACL} - T_{ADL})}{z_2 - z_1}$ (6)
Anode catalyst layer	$\frac{\partial T}{\partial t} = \alpha \frac{\partial^2 T}{\partial z^2} + q$ (7)
Membrane	$\frac{T - T_m}{T_0 - T_m} = e^{-\left(\frac{h x c}{c_p \rho V}\right)}$ (8)
Cathode catalyst layer	$\rho c_p \frac{\partial T}{\partial t} = \lambda \frac{\partial^2 T}{\partial z^2} + q$ (9)

**Mass transport:** A passive liquid feed Direct Methanol Fuel Cell (DMFC) injected the fuel to the tank called Anode Flow Channel (AFC). The system neither external liquid pump nor gas blower. Methanol tank is considered as batch reactor at varying in volume which the principle same as Plug Flow Reactor (PFR). We assume the reaction occur completely and carbon dioxide produced with. There are three major components coexisting in AFC side, porous media and fluid channel, such as H<sub>2</sub>O, CH<sub>3</sub>OH and CO<sub>2</sub>. If carbon dioxide is considered in the system, means 2-phase system are consider. Other intermediate are neglected, OH, HO, CO, etc. in the system. The equation related to mass balance and heat transport are shown in Table 1 and 2.

**Voltage balance:**

$$\frac{\Gamma_M}{M_M} = \left( a_a i_{0M,ref} \frac{k C_M}{C_M + \lambda e^{\alpha_A \eta_A F / RT}} e^{\alpha_A \eta_A F / RT} \right) \quad (10)$$

where, M<sub>M</sub> is the molecular weight of methanol, n<sub>M</sub> is the number of electrons transferred during methanol oxidation (where consumption of 1 mol of methanol can produce n<sub>M</sub> = 6 mol electrons), a<sub>a</sub> is the specific surface area of the anode, I<sub>0M,ref</sub> is the reference methanol oxidation exchange current density, λ is constant in the rate expression and α<sub>A</sub> is the anodic transfer coefficient.

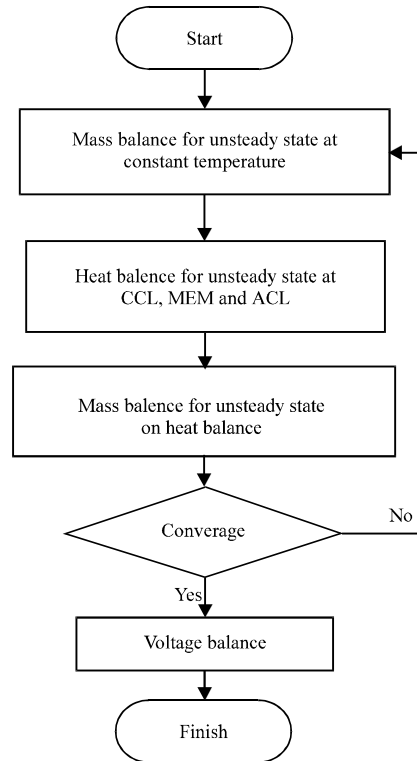


Fig. 2: Schematic diagram analytical solution for unsteady state

**Analytical solution:** Solution for the mathematical problem made based on Fig. 2.

**RESULTS AND DISCUSSION**

These results consist of three components which are mass balance, heat balance and voltage balance.

Figure 3a-d show the methanol and oxygen distribution through the layer at difference time. Methanol concentration at the first 15 h abruptly drops because the platinum as catalyst works effectively at ACL. Oxygen can diffuse into the cathode from the ambient due to the air breathing action of the cell. Air from surrounding will pass through CFC then diffused at CDL. Diffusion process is very slow with time and z direction because oxygen concentration at CDL increases slowly as shown in Fig. 3c and d.

Fig. 4a and b show the temperature distribution for each layer ACL and ADL. For ACL layer, temperature increase abruptly then start to decrease after 2 h. This shows the activity of reaction between methanol and water to produce proton and electron. Heat is transfer

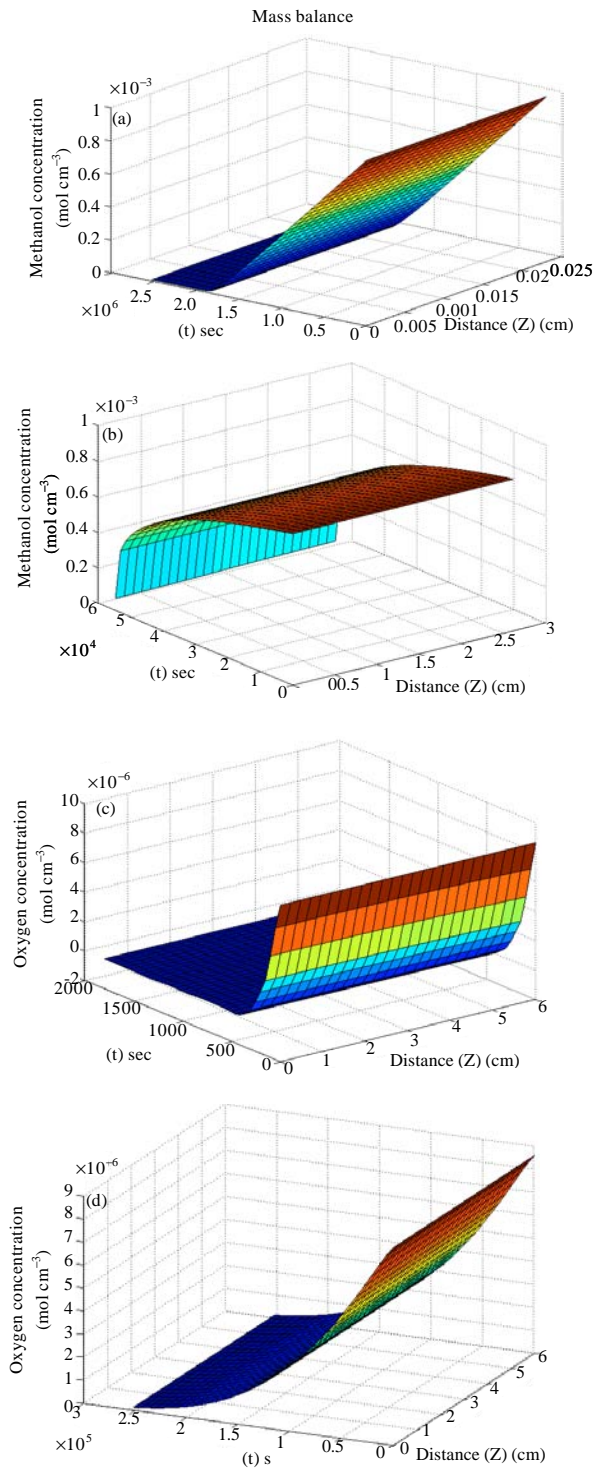


Fig. 3: (a) Methanol Concentration at ABL, (b) Methanol Concentration at ACL, (c) Oxygen Concentration at CCL and (d) Oxygen Concentration at CDL

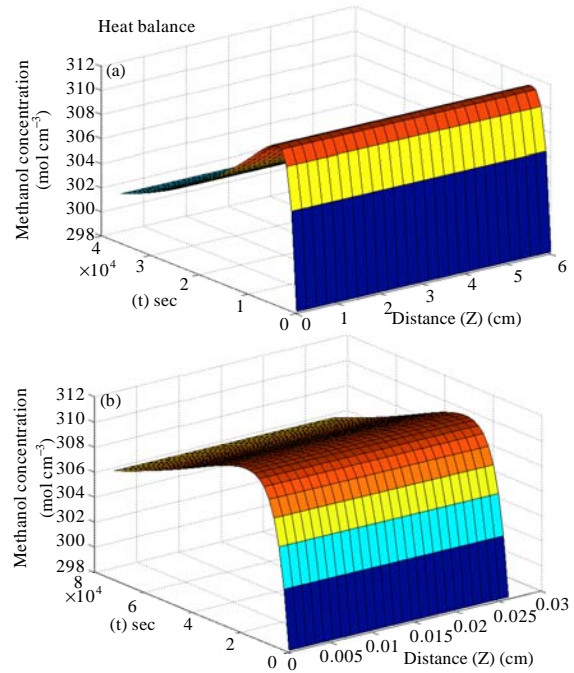


Fig. 4: (a) Temperature distribution at ACL for 10 h after methanol injected to the reservoir and (b) Temperature distribution at ACL for 10 h after methanol injected to the reservoir

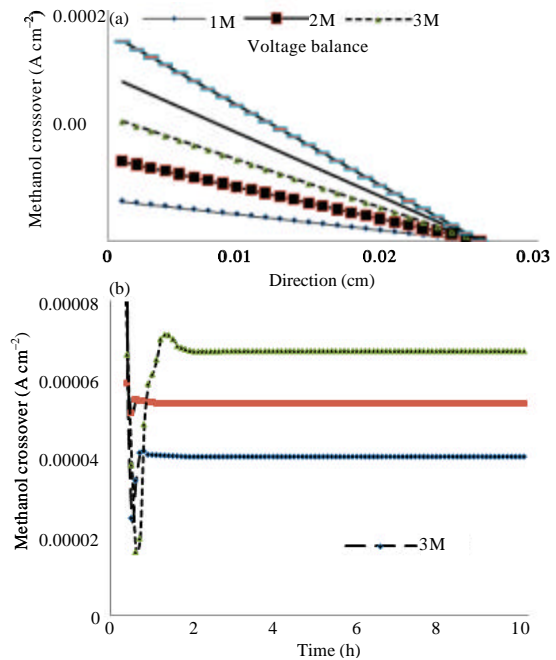


Fig. 5: Methanol crossover through (a) z-direction and (b) time

from the ACL to the ADL. Here, temperature at ADL is depends on the ACL. Form the figure, temperature also increase at ADL then decrease slowly after 6 h.

In this study, current density set as constant of 20 mA cm<sup>-2</sup> and then run the simulation at various methanol concentrations from 1 M to 5 M which is optimum methanol concentration. The results in Fig. 5a shows the effect of methanol crossover have increase proportionally to the bulk methanol concentration. Figure 5b shows the trend of methanol crossover through the membrane along the experiment for 10 h. 5 Molar concentrations show the highest effect of methanol crossover to current density.

### CONCLUSION

A unsteady state of direct methanol fuel cell with mass and heat transport for both anode and cathode are take into consideration. The model takes into account mass transfer from the anode flow and fragment heat due to the electrochemical reaction in the anode and cathode side.

### ACKNOWLEDGMENT

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### NOMENCLATURES

$a_o$  = Active area per unit volume in anode catalyst layer (cm<sup>-1</sup>)  
 $a_i$  = Integrated constant (cm<sup>-1</sup>)  
 $A_a$  = Active area per unit mass of PtRu catalyst (cm<sup>2</sup> g<sup>-1</sup>)  
 $A_c$  = Active area per unit mass of Pt catalyst (cm<sup>2</sup> g<sup>-1</sup>)  
 $A_r$  = Active area (cm<sup>2</sup>)  
 $C_b$  = Anode channel concentration of methanol (mol cm<sup>-3</sup>)  
 $C_c$  = Carbon dioxide concentration (mol cm<sup>-3</sup>)  
 $C_M$  = Methanol Concentration (mol cm<sup>-3</sup>)  
 $C_{1M}$  = Methanol concentration at  $z_2$  (mol cm<sup>-3</sup>)  
 $C_{2M}$  = Methanol concentration at  $z_3$  (mol cm<sup>-3</sup>)  
 $C_{M,ref}$  = Reference methanol concentration (mol cm<sup>-3</sup>)  
 $C_o$  = Oxygen concentration (mol cm<sup>-3</sup>)  
 $C_{Og}$  = Oxygen concentration at cathode catalystlayer/ gas diffusion (mol cm<sup>-3</sup>)

$C_{O,ref}$  = Reference oxygen concentration (mol cm<sup>-3</sup>)  
 $C_w$  = Water concentration (mol cm<sup>-3</sup>)  
 $D_a$  = Methanol diffusivity in anode catalyst layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_a^{eff}$  = Effective diffusivity of methanol in anode catalyst layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_b$  = Methanol diffusivity in anode backing layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_b^{eff}$  = Effective diffusivity of methanol in anode backing layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_c$  = Oxygen diffusivity in cathode catalyst layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_c^{eff}$  = Effective oxygen diffusivity in cathode catalyst layer (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_d$  = Oxygen gas diffusivity in cathode gas diffusion (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_d^{eff}$  = effective oxygen gas diffusivity in cathode gas diffusion (cm<sup>2</sup> sec<sup>-1</sup>)  
 $D_m$  = Methanol diffusivity in membrane (cm<sup>2</sup> sec<sup>-1</sup>)  
 $F$  = Faraday constant (C mol<sup>-1</sup>)  
 $i_{oM,ref}$  = Reference methanol oxidation exchange current density (A cm<sup>-2</sup>)  
 $i_{oO,ref}$  = Reference oxygen reduction exchange current density (A cm<sup>-2</sup>)  
 $I_{cell}$  = Cell discharge current density (A cm<sup>-2</sup>)  
 $I_{leak}$  = Cross-over current density (A cm<sup>-2</sup>)  
 $j$  = local transfer current density within catalyst layer (A cm<sup>-3</sup>)  
 $k$  = Potential dependent rate constant of methanol oxidation (sec<sup>-1</sup>)  
 $k_c$  = Potential dependent rate constant of oxygen reduction (sec<sup>-1</sup>)  
 $k_p$  = Permeation constant of pressure induced convection (cm<sup>2</sup>/sec/atm)  
 $L_a$  = Anode catalyst layer thickness (cm)  
 $L_b$  = Anode backing layer thickness (cm)  
 $L_c$  = Cathode catalyst layer thickness (cm)  
 $L_d$  = Cathode gas diffusion thickness (cm)  
 $L_m$  = Membrane thickness (cm)  
 $n_M$  = Electrons transferred of methanol oxidation  
 $n_O$  = NO electrons transferred of oxygen reduction  
 $N_m$  = Methanol flux at membrane (mol/cm<sup>2</sup>/sec)  
 $N_m$  = Oxygen flux at membrane (mol/cm<sup>2</sup>/sec)  
 $R$  = Universal gas constant (J/mol/K)  
 $R_g$  = Rg universal gas constant (atm/cm<sup>3</sup>/mol/K)

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