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By Using Normal Least Squares Support Vector Regression Model to Carry out Market Forecasting

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Abstract: Forecasting of the market sale is an important part of supply chain management. It is well known that traditional forecasting method for market sale is based on the market demand evaluation of the different departments. In order to derive a more robust least squares support vector regression model, a novel normal least squares support vector regression model is proposed in this study. Compared with least squares support vector regression model, normal least squares support vector regression model incorporates the data information in a global way. It is indicated that the forecasting ability for sales volume of normal least squares support vector regression model is more excellent than those of least squares support vector regression model and traditional support vector regression model.

Key words: Normal direction, regression method, market forecasting

INTRODUCTION

Forecasting of the market sale is an important part of supply chain management (Qu *et al.*, 2012; McCarthy Byrne *et al.*, 2011; Wong and Guo, 2010; Taylor, 2007). Traditional forecasting method for market sale bases on the market demand evaluation of the different departments (Yu *et al.*, 2011; Chang and Wang, 2006).

Support vector regression method is powerful for the regression problems characterized by small samples, nonlinearity and high dimension. Currently, Support vector regression method is an active field in artificial intelligent technology. Artificial neural networks use the empirical risk minimization principle, which is generally employed in the classical methods. Support vector regression method based on the SRM principle (Xie, 2012; Huang, 2012; Kazem *et al.*, 2010; Cho *et al.*, 2009), which seeks to minimize an upper bound of the generalization error. Least squares support vector regression method alters inequality constraints into equal conditions and employs a squared loss function, which can make least squares support vector regression method achieve higher calculation speed and efficiency (Esteki *et al.*, 2010; Patil *et al.*, 2005).

In order to derive a more robust least squares support vector regression model, a novel normal least squares support vector regression model is proposed in this study. Compared with least squares support vector regression model, normal least squares support vector regression model incorporates the data information in a global way. In the experiments, sales volume of Guangbai

Tianhe store from 2004.1 to 2007.6 are used to study the sale forecasting performance of normal least squares support vector regression model compared with other prediction techniques. It is indicated that the forecasting ability for sales volume of normal least squares support vector regression model is more excellent than those of least squares support vector regression model and traditional support vector regression model.

NORMAL LEAST SQUARES SUPPORT VECTOR REGRESSION METHOD

Considering a set of dataset with the input vector and the corresponding output, the form of least squares support vector regression model can be given by:

$$f(x) = w \cdot \phi(x) + b \quad (1)$$

where, w is the weight vector and b is the bias term.

Least squares support vector regression model can be obtained by formulating the regression problem:

$$J_1(w, b, e) = \frac{1}{2} \|w\|^2 + \frac{1}{2} C \sum_{i=1}^n e_i^2 \quad (2)$$

Subject to:

$$y_i = [w' \cdot \phi(x)] + b + e_i$$

where, e_i is the error.

Introduce the Lagrangian as:

$$T_1(w, b, e_i, \alpha_i) = \frac{1}{2} \|w\|^2 + \frac{1}{2} C \sum_{i=1}^n e_i^2 - \sum_{i=1}^n \alpha_i (w' \varphi(x_i) + b - y_i + e_i) \quad (3)$$

where, $\alpha = [\alpha_1, \alpha_2, \dots, \alpha_n]$ refers to the Lagrange multiplier vector.

The conditions for optimality are:

$$\frac{\partial T_1}{\partial w} = 0 \rightarrow w = \sum_{i=1}^n \alpha_i \varphi(x_i) \quad (4)$$

$$\frac{\partial T_1}{\partial b} = 0 \rightarrow \sum_{i=1}^n \alpha_i = 0 \quad (5)$$

$$\frac{\partial T_1}{\partial e_i} = 0 \rightarrow \alpha_i = C e_i \quad (6)$$

$$\frac{\partial T_1}{\partial \alpha_i} = 0 \rightarrow w' \varphi(x_i) + b + e_i = y_i \quad (7)$$

Then, the optimal solution will be calculated according to the linear equation:

$$\begin{bmatrix} 0 & I' \\ I & P \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} 0 \\ y \end{bmatrix} \quad (8)$$

where, $y = [y_1, \dots, y_n]$, $I = [1, 1, \dots, 1]$ and $P = K + V$:

$$K = (k(x_i, x_j))_{n \times n} \quad (9)$$

$$V = \text{diag} \left\{ \frac{1}{C}, \frac{1}{C}, \dots, \frac{1}{C} \right\} \quad (10)$$

Hence, the regression function of least squares support vector regression model becomes:

$$f(x) = \sum_{i=1}^n \alpha_i k(x, x_i) + b \quad (11)$$

In order to derive a more robust least squares support vector regression model, a novel normal least squares support vector regression model is proposed in this study. Then, we modify the constraints in traditional least squares support vector regression model as follows:

$$\frac{y_i - (w' \varphi(x_i) + b)}{\sqrt{1 + \|w\|^2}} = e_i \quad (12)$$

Combining with the same objective function, we derive the following least squares support vector regression model:

$$J_2(w, b, e) = \frac{1}{2} \|w\|^2 + \frac{1}{2} C \sum_{i=1}^n e_i^2 \quad (13)$$

Subject to:

$$\frac{y_i - (w' \varphi(x_i) + b)}{\sqrt{1 + \|w\|^2}} = e_i$$

Compared with least squares support vector regression model, normal least squares support vector regression model incorporates the data information in a global way.

Then, we have the following Lagrangian:

$$T_2(w, b, e, \alpha_i) = \frac{1}{2} \|w\|^2 + \frac{1}{2} C \sum_{i=1}^n e_i^2 - \sum_{i=1}^n \alpha_i \left(\frac{y_i - (w' \varphi(x_i) + b)}{\sqrt{1 + \|w\|^2}} - e_i \right) \quad (14)$$

Finally, we can obtain the solution of Eq. 14 using the same method as least squares support vector regression model.

EXPERIMENTAL RESULTS

As shown in Fig. 1, sales volume of Guangbai Tianhe store from 2004.1 to 2007.6 are used to study the sale forecasting performance of normal least squares support vector regression model compared with other prediction techniques. The sales volume of Guangbai Tianhe store from 2006.11 to 2007.6 are used to test the sale forecasting performance of normal least squares support vector regression model.

The experimental data must be normalized to improve the smoothness of the prediction techniques:

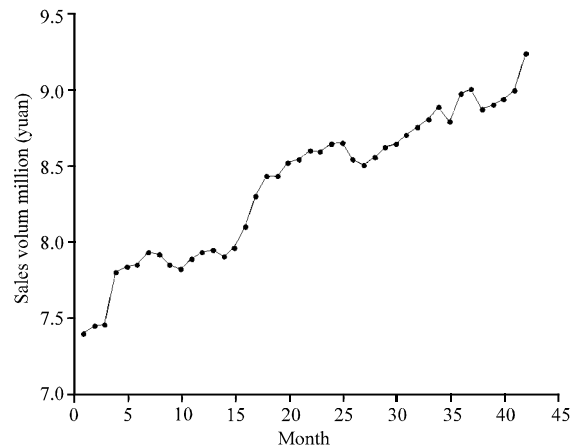


Fig. 1: Sales volume of Guangbai Tianhe store from 2004.1 to 2007.6

$$d'_i = \frac{d_i - d_{\min}}{d_{\max} - d_{\min}} \quad (15)$$

where, d_{\min} , d_{\max} are the minimum and maximum value, respectively.

Figure 2 gives the comparison between actual curve and sale forecasting curve of normal least squares support vector regression model and the sale forecasting error of normal least squares support vector regression model is given in Fig. 3. As shown in Fig. 2 and 3, the maximum sale forecasting error of normal least squares support vector regression model is less than 1.4%. Then, Fig. 4 gives the comparison between actual curve and sale forecasting curve of least squares support vector regression model and the sale forecasting error of

least squares support vector regression model is given in Fig. 5. As shown in Fig. 4 and 5, the maximum sale forecasting error of least squares support vector regression model is less than 4%.

Finally, Fig. 6 gives the comparison between actual curve and sale forecasting curve of support vector regression model, and the sale forecasting error of support vector regression model is given in Fig. 7. As shown in Fig. 6 and 7, the maximum sale forecasting error of support vector regression model is less than 9%.

The testing results show that the forecasting error for sales volume of normal least squares support vector regression model is smaller than that of least squares support vector regression model and the forecasting error for sales volume of least squares support vector

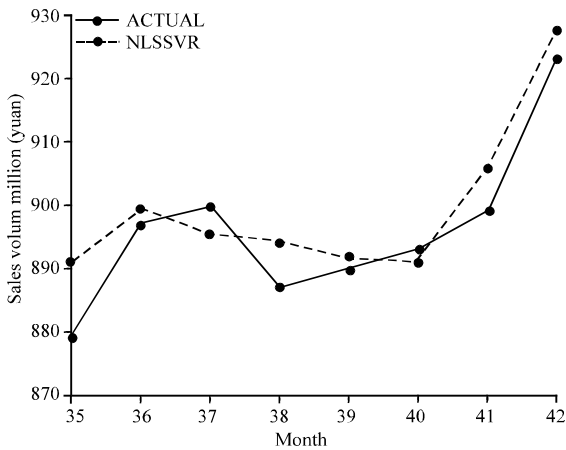


Fig. 2: Comparison between actual curve and sale forecasting curve of normal least squares support vector regression model

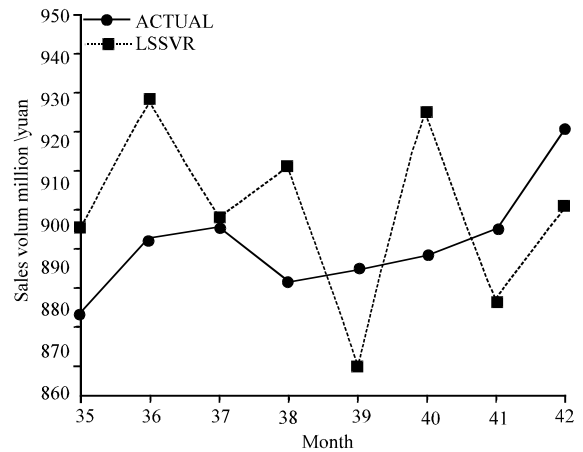


Fig. 4: Comparison between actual curve and sale forecasting curve of least squares support vector regression model

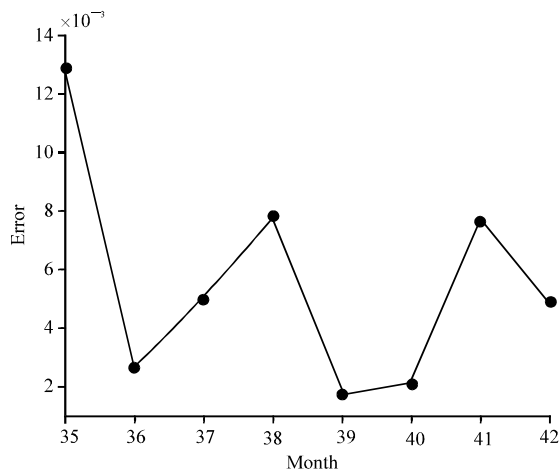


Fig 3: Sale forecasting error of normal least squares support vector regression model

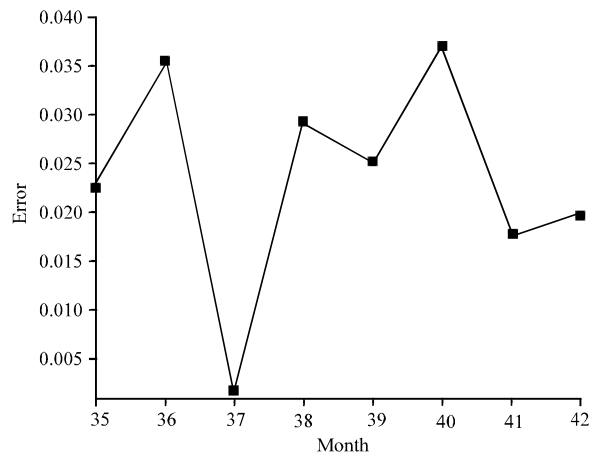


Fig. 5: Sale forecasting error of least squares support vector regression model

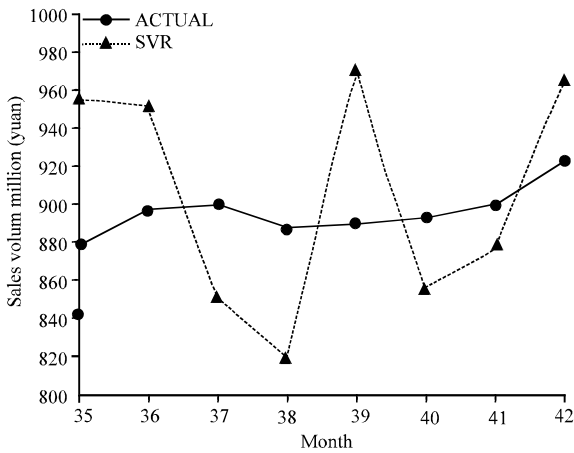


Fig. 6: Comparison between actual curve and sale forecasting curve of support vector regression model

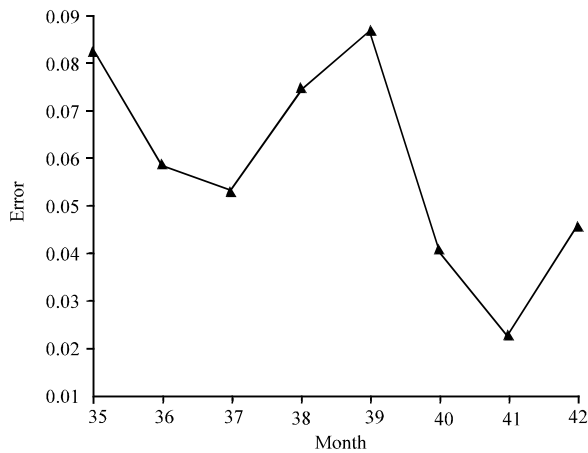


Fig. 7: Sale forecasting error of support vector regression model

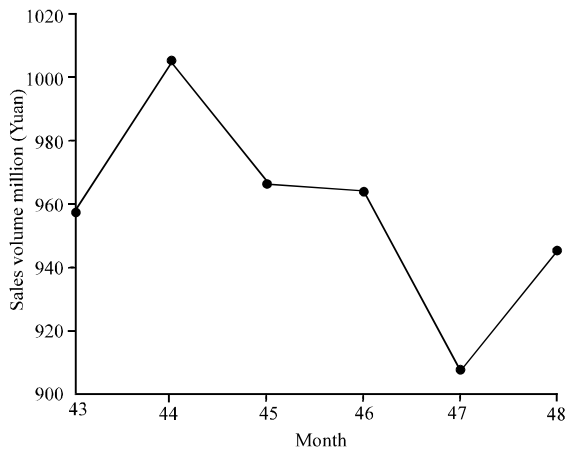


Fig. 8: Sales volume prediction results of normal least squares support vector regression model

regression model is smaller than that of traditional support vector regression model. Therefore, we can conclude that the forecasting ability for sales volume of normal least squares support vector regression model is more excellent than those of least squares support vector regression model and traditional support vector regression model.

Then, we employ normal least squares support vector regression model to predict sales volume of Guangbai Tianhe store from 2007.7 to 2007.12 and 2007.7~2007.12 are denoted as 43~48. The sales volume prediction results of normal least squares support vector regression model are given in Fig. 8.

CONCLUSION

A novel normal least squares support vector regression model is proposed in this study. Compared with least squares support vector regression model, normal least squares support vector regression model incorporates the data information in a global way. It can be seen that the forecasting ability for sales volume of normal least squares support vector regression model is more excellent than those of least squares support vector regression model and traditional support vector regression model.

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