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Research ZVS Synchronous Rectification of Resonant Converter

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Abstract: In order to expand the application of synchronous rectification, the technology using ZVS synchronous rectifier is studied which is based on the IPT resonant converter. By using its own resonant characteristic, a novel control method that AC-DC section of the resonant converter works in ZVS SR state is proposed in this study. First of all, the ZVS working operation of SR is analyzed and equivalent circuits for each operation mode are also given. On that basis, the novel control method is proposed. Then, according to the differential equations of equivalent circuit, the state space model is established. In order to make full-bridge SR network of the secondary circuit work in ZVS state, the ZVS operating point can be obtained by solving the fixed point function which is based on the state space model and stroboscopic mapping method. Moreover, operating principle of control circuit for ZVS SR is also presented. Finally, experimental results verify the effectiveness of control method proposed in this study.

Key words: Synchronous rectification, ZVS, resonant converter, stroboscopic mapping

INTRODUCTION

Synchronous Rectifier (SR) has been widely adopted in the low output voltage applications to reduce the conduction loss of the output rectifier (Lim *et al.*, 2010). Therefore, SR has become a research hotspot associated with the AC-DC converter of all kinds of switching power supply.

At present, researches on synchronous rectification are mainly concentrated in buck converter (Stankovic *et al.*, 2012), forward converter (Coban and Cadirci, 2011), flyback converter (Kim *et al.*, 2014), half-bridge converter (Jeong, 2008), push-pull converter. However, the application of SR in a resonant converter has been rarely studied.

Analyzing the existing synchronous rectifier converters, their rectifier section generally work in hard switching state. Therefore, when the switching frequency of SR is high, large switching losses are caused and the system efficiency is reduced. At the same time, it is easy to influence the main circuit operation of converter and reduce the system performance because synchronous rectification of the existing converters usually is adopted self-driving mode.

However, compared with other converters, resonant converter has the advantages of small volume, high transmission efficiency. In particular, capacitor voltage and inductor current in the resonant tank are sine wave, so that a wide range of switching network worked in Zero Voltage Switching (ZVS) or Zero Current Switching (ZCS) can be easy to achieve. Further analysis shows

that, due to the existence of resonant tank, the traditional self-driving cannot be adopted to achieve the SR output for resonant converter.

In this study, the resonant converter circuit based on Inductive Power Transfer (IPT) (Li *et al.*, 2012) is as a research object. By using its own resonant characteristic, a novel control method that AC-DC section of the resonant converter works in ZVS SR state is proposed.

This study is organized as follows. ZVS operation principle of SR for the IPT resonant converter is presented. Then, the state space model of the resonant converter is established. In order to quickly and accurately calculate the ZVS-operating cycle of SR, the fixed point function about it is established by using a stroboscopic mapping method which is based on the state space model. Moreover, operating principle of control circuit for ZVS SR is also presented. Finally, experimental results are conducted to verify that control method proposed in this study is effective for the resonant converter circuit based on IPT.

ZVS OPERATION PRINCIPLE OF SR

In this study, the IPT resonant converter circuit used synchronous rectifier is showed in Fig. 1 which consists of a primary and a secondary circuit. In the primary circuit, the switching network (S_1 , S_4 and S_2 , S_3) convert the dc voltage source E_{dc} to high frequency ac that drives an LCL resonant tank consisting of L_1 , C_p and L_p . Therefore, a high-frequency ac can be generated in the primary coil L_p .

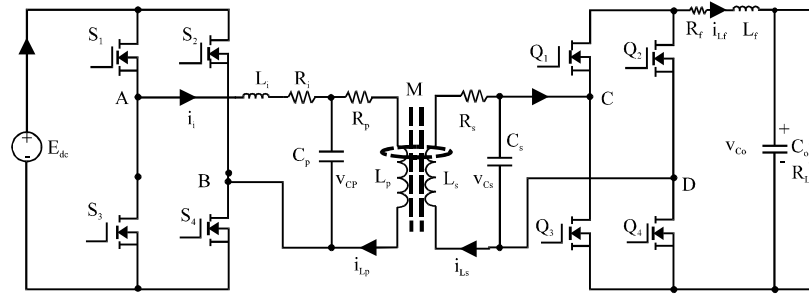


Fig. 1: Circuit diagram of the IPT resonant converter used SR

Due to the magnetic field coupling, a high-frequency ac voltage is induced in the secondary coil L_s which is then completely tuned by the parallel capacitor C_s . In the secondary circuit, the two switching pairs (Q_1, Q_4 and Q_2, Q_3) constitute a full-bridge SR network. L_f and C_o constitute a filter link, R_L is the load resistance and M is the mutual inductance coupling value between primary coil and secondary.

In order to simplify the analysis, following assumptions are made for the analyses of operating modes:

- All MOSFETs are considered to be ideal
- The input voltage source E_{dc} is ideal
- The filter inductor L_f current is continuous

Critical operation waveforms of the system are given in Fig. 2, for steady-state operation. v_{AB} is the input voltage of the primary full-bridge converter. i_i is the flowing current of inductor L_i . v_{Cs} is the voltage across capacitor C_s . v_{Qi} ($i = 1, 2, 3, 4$) is the drain-source voltage of switch Q_i in the secondary SR network. G_i ($i = 1, 2, 3, 4$) is the drive voltage of switch Q_i in the secondary SR network.

Meanwhile, so as to clearly analyze operation modes of the circuit shown in Fig. 1, time t_0 is assumed to be the starting point of one operational cycle and stipulate positive direction of the dc energy E_{dc} injected is that switches S_1 and S_4 are turned on. When Switches Q_1 and Q_4 are turned on, this is SR output positive direction of the AC voltage v_{Cs} . So, effective circuits for each mode in one operational cycle are given in Fig. 3.

Mode 1 (t_0-t_1): The state of primary circuit is that dc energy is injected from negative direction. Switches S_2 and S_3 are turned on when S_1 and S_4 are turned off. The state of secondary circuit is that the AC voltage v_{Cs} is

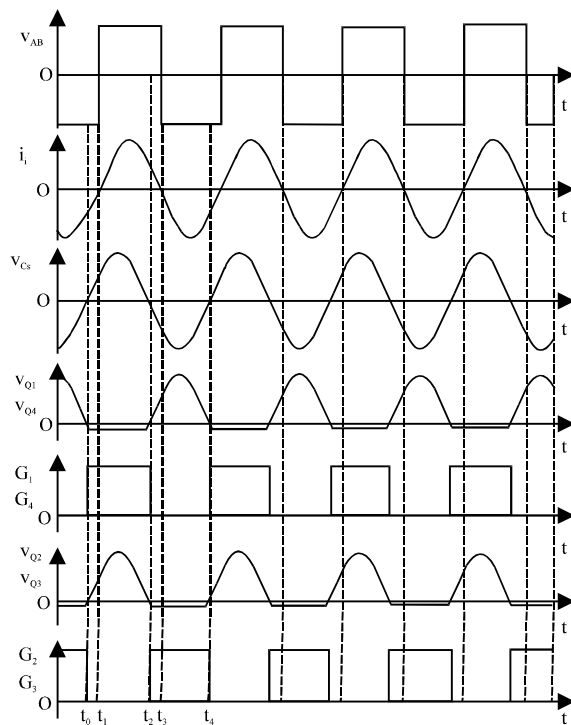


Fig. 2: Critical steady-state operation waveforms

output from positive direction of the synchronous rectifier. Switches Q_1 and Q_4 are reversely turned on when Q_2 and Q_3 are turned off. In this mode, its equivalent circuit is shown in Fig. 3a.

Mode 2 (t_1-t_2): The state of primary circuit is that energy is injected from positive direction. Switches S_1 and S_4 are turned on when S_2 and S_3 are turned off. The state of secondary circuit is that the AC voltage v_{Cs} is output from positive direction of the synchronous rectifier. Switches Q_1 and Q_4 are reversely turned on when Q_2 and Q_3 are turned off. In this mode, its equivalent circuit is shown in Fig. 3b.

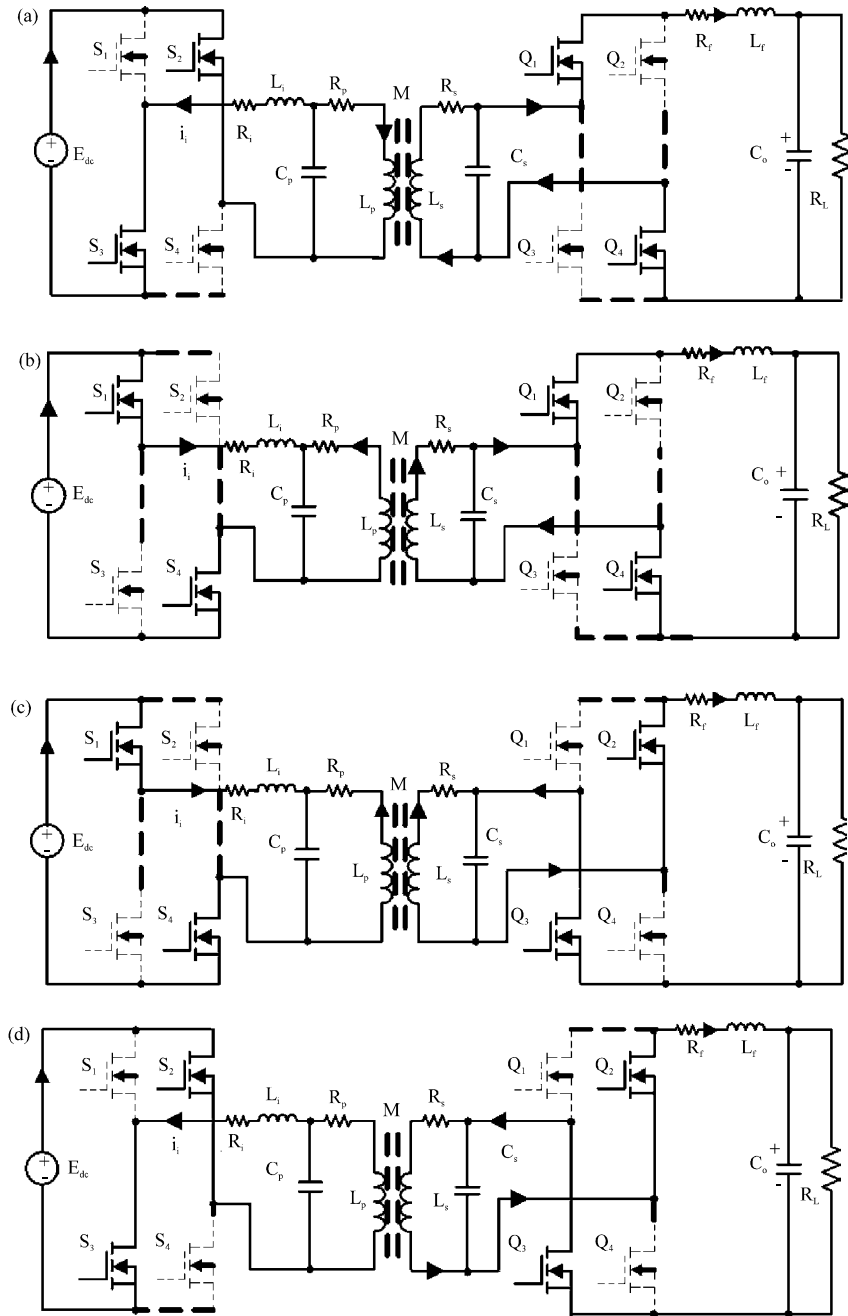


Fig. 3(a-d): Equivalent circuits for each operation mode (a) Mode 1, (b) Mode 2, (c) Mode 3 and (d) Mode 4

Mode 3 (t_2-t_3): The state of primary circuit is that energy is injected from positive direction. Switches S_1 and S_4 are turned on when S_2 and S_3 are turned off. The state of secondary circuit is that the AC voltage v_{C_s} is output from negative direction of the synchronous rectifier. Switches Q_2 and Q_3 are reversely turned on when Q_1 and Q_4 are turned off. In this mode, its equivalent circuit is shown in Fig. 3c.

Mode 4 (t_3-t_4): The state of primary circuit is that energy is injected from negative direction. Switches S_2 and S_3 are turned on when S_1 and S_4 are turned off. The state of secondary circuit is that the AC voltage v_{C_s} is output from negative direction of the synchronous rectifier. Switches Q_2 and Q_3 are reversely turned on when Q_1 and Q_4 are turned off. In this mode, its equivalent circuit is shown in Fig. 3d.

Through the above analysis, the switching states of two primary switching pairs (S_1, S_4 and S_2, S_3) are changed, when the current of inductance L_i is zero. This time that their switching states are changed between turned on and off, the current flowing through them are zero. Hence, the primary switching inverter works in zero current soft switching state.

In the secondary circuit, the voltage v_{C_s} of the capacitor C_s is a sinusoidal voltage. It is obvious to know that when v_{C_s} is equal to zero, the drain to source voltage v_{Q_i} of the four switches (Q_1, Q_2, Q_3 and Q_4) are also equal to zero. Therefore, ZVS SR output of the AC voltage v_{C_s} can be achieved by controlling the switching pairs (Q_1, Q_4 and Q_2, Q_3) turned on or off when v_{C_s} is equal to zero.

In summary, the primary full-bridge converter working in zero current soft switching state and the secondary full-bridge SR network working in zero voltage soft switching state can be achieved in the IPT resonant converter.

STEADY STATE MODELING

In order to carry out the numerical analysis of the circuit shown in Fig. 1, a steady state mathematical model of the system is necessary to be established.

Assume that the switching period of the primary full-bridge inverter shown in Fig. 1 is T under steady-state conditions. Then the input voltage of the primary resonant tank can be described as:

$$v_i = S(t)E_{dc} \tag{1}$$

$$S(t) = \begin{cases} 1 & S_1, S_4 \text{ on, } mT < t < (2m+1)T/2 \\ -1 & S_2, S_3 \text{ on, } (2m+1)T/2 < t < (m+1)T \end{cases} \tag{2}$$

where, m is zero or a positive integer.

In the secondary circuit shown in Fig.1, switch transitions of the full-bridge SR network are determined by the polarity change of the resonant voltage v_{C_s} . Consequently, a sign function $\text{Sgn}(v_{C_s})$ can be used to represent operation of the full-bridge SR network:

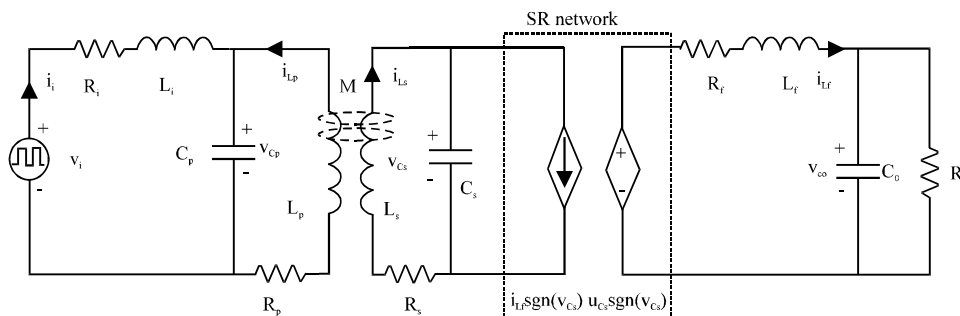


Fig. 4: Equivalent circuit of the IPT resonant converter used SR

$$\text{Sgn}(v_{C_s}) = \begin{cases} 1 & v_{C_s} > 0 \\ -1 & v_{C_s} \leq 0 \end{cases}$$

After such that representations, the circuit diagram shown in Fig. 1 is simplified as an equivalent circuit shown in Fig. 4.

According to Kirchhoff's current and voltage laws, the differential equations of the equivalent circuit as shown in Fig. 4, can be presented as follows:

$$\frac{di_i}{dt} = \frac{1}{L_i} S(t)E_{dc} - \frac{R_i}{L_i} i_i - \frac{1}{L_i} v_{C_p} \tag{3}$$

$$\frac{dv_{C_p}}{dt} = \frac{1}{C_p} i_i - \frac{1}{C_p} i_{L_p} \tag{4}$$

$$\frac{di_{L_p}}{dt} = \frac{L_s}{\Delta} v_{C_p} - \frac{R_p L_s}{\Delta} i_{L_p} - \frac{MR_s}{\Delta} i_{L_s} - \frac{M}{\Delta} v_{C_s} \tag{5}$$

$$\frac{di_{L_s}}{dt} = \frac{M}{\Delta} v_{C_p} - \frac{MR_p}{\Delta} i_{L_p} - \frac{L_p R_s}{\Delta} i_{L_s} - \frac{L_p}{\Delta} v_{C_s} \tag{6}$$

$$\frac{dv_{C_s}}{dt} = \frac{1}{C_s} \text{Sgn}(v_{C_s}) i_{L_r} - \frac{1}{C_s} i_{L_s} \tag{7}$$

$$\frac{di_{L_r}}{dt} = \frac{1}{L_r} \text{Sgn}(v_{C_s}) v_{C_s} - \frac{R_r}{L_r} i_{L_r} - \frac{1}{L_r} v_{C_o} \tag{8}$$

$$\frac{dv_{C_o}}{dt} = \frac{1}{C_o} i_{L_r} - \frac{1}{R_L C_o} v_{C_o} \tag{9}$$

where, $\Delta = L_s L_r - M^2$. By choosing $x = [i_i \ v_{C_p} \ i_{L_p} \ i_{L_s} \ v_{C_s} \ i_{L_r} \ v_{C_o}]^T$ and $u = [E_{dc}]$ as the state vector and the input vector of the system, respectively. According to the differential Eq. 3-9, the system can be described by the following state space model:

$$\dot{x} = A_i x + B_i u \quad i = 1, 2, 3, 4 \tag{10}$$

where, i represent the figures of operation modes shown in Fig. 3:

$$A_1=A_2= \begin{bmatrix} \frac{-R_i}{L_i} & \frac{-1}{L_i} & 0 & 0 & 0 & 0 & 0 \\ \frac{1}{C_p} & 0 & \frac{-1}{C_p} & 0 & 0 & 0 & 0 \\ 0 & \frac{L_s}{\Delta} & \frac{-R_p L_s}{\Delta} & \frac{-MR_s}{\Delta} & \frac{-M}{\Delta} & 0 & 0 \\ 0 & \frac{M}{\Delta} & \frac{-MR_p}{\Delta} & \frac{-L_p R_s}{\Delta} & \frac{-L_p}{\Delta} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{C_s} & \frac{-1}{C_s} \\ 0 & 0 & 0 & 0 & \frac{1}{L_f} & \frac{-R_f}{L_f} & \frac{-1}{L_f} \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{C_o} & \frac{-1}{R_L C_o} \end{bmatrix}$$

$$x_1 = \phi_1 x_0 + A_1^{-1}(\phi_1 - I) B_1 u \quad (12)$$

$$x_2 = \phi_2 x_1 + A_2^{-1}(\phi_2 - I) B_2 u \quad (13)$$

$$x_3 = \phi_3 x_2 + A_3^{-1}(\phi_3 - I) B_3 u \quad (14)$$

$$x_4 = \phi_4 x_3 + A_4^{-1}(\phi_4 - I) B_4 u \quad (15)$$

where, $\phi_i = e^{A_i t}$, ($i = 1, 2, 3, 4$), I is a 7-order unit matrix and x_0 is the initial value of the circuit state vector.

Under steady-state conditions, the state vector repeats periodically which means the state vector results in a fixed point x^* is described as follows:

$$x^* = x_4 = x_0 \quad (16)$$

Substitute Eq. 13-15 into 12, the fixed point x^* can be expressed as follows:

$$x^* = \alpha [\phi_4 \phi_3 \phi_2 A_1^{-1}(\phi_1 - I) + \phi_4 \phi_3 A_2^{-1}(\phi_2 + \phi_4 A_3^{-1}(\phi_3 - I) + A_4^{-1}(\phi_4 - I))] \quad (17)$$

where, $\alpha = (I - \phi_4 \phi_3 \phi_2 \phi_1)^{-1}$.

Corresponding to the ZVS condition of the full-bridge SR network, the voltage v_{C_s} must be zero at the switching instants. Then from Eq. 17, ZVS operation cycle (T_{ZVS}) of the full-bridge SR network can be obtained as follows (Tang *et al.*, 2009; Sun *et al.*, 2011):

$$v_{C_s}(T_{ZVS}) = Y \bullet x^* = 0 \quad (18)$$

where, $Y = [0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$ is a selection matrix for the state variable v_{C_s} .

OPERATING PRINCIPLE OF CONTROL CIRCUIT

In order to achieve zero voltage soft switching state operation of the secondary full-bridge SR network, the working operation of control circuit as shown in Fig. 5.

The operation processes of the control circuit are described as follows. First of all, the AC voltage v_{C_s} through the sampling circuit, a weak signal (v_1) with the same frequency can be obtained. The phase of the signal (v_1) must be compensated, because the control circuit operation can lead to a delay of the signal. To precisely control switching pairs (Q_1, Q_4 and Q_2, Q_3) turned on or off, the zero-crossing detection circuit is designed for detecting of the AC voltage v_{C_s} . Therefore, after the previous circuit, the digital signal (G_{m2}) digital signal can be obtained. G_{m2} is used as the input of driving circuit for switches (Q_2, Q_4). In order to achieve the two SR switching pairs (Q_1, Q_4 and Q_2, Q_3) working in zero voltage soft switching state, the two drive voltage pairs (G_1, G_4

$$A_3=A_4= \begin{bmatrix} \frac{-R_i}{L_i} & \frac{-1}{L_i} & 0 & 0 & 0 & 0 & 0 \\ \frac{1}{C_p} & 0 & \frac{-1}{C_p} & 0 & 0 & 0 & 0 \\ 0 & \frac{L_s}{\Delta} & \frac{-R_p L_s}{\Delta} & \frac{-MR_s}{\Delta} & \frac{-M}{\Delta} & 0 & 0 \\ 0 & \frac{M}{\Delta} & \frac{-MR_p}{\Delta} & \frac{-L_p R_s}{\Delta} & \frac{-L_p}{\Delta} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{-1}{C_s} & \frac{-1}{C_s} \\ 0 & 0 & 0 & 0 & \frac{-1}{L_f} & \frac{-R_f}{L_f} & \frac{-1}{L_f} \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{C_o} & \frac{-1}{R_L C_o} \end{bmatrix}$$

$$B_1 = B_4 = \begin{bmatrix} \frac{-1}{L_i} & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T$$

$$B_2 = B_3 = \begin{bmatrix} \frac{1}{L_i} & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T$$

DETERMING ZVS-OPERATING CYCLE OF SR

The ZVS operating point of the SR circuit must be obtained to make full-bridge SR network of the secondary circuit work at zero voltage soft switching state.

The system matrix A_1, A_2, A_3, A_4 are invertible, so that the analytical solution of Eq. 1) has the following format:

$$x(t) = \phi(t)x_0 + A^{-1}(\phi(t) - I)Bu \quad (11)$$

where, $x_0 = x(t)|_{t=0}$ and $\phi(t) = e^{At}x(t)$.

As can be seen from Fig. 2 and 3, during one operational cycle, the final value of each mode equals to the initial value of the next mode. Therefore Eq. 11 can be extended into four stroboscopic mapping equations to cover all the four modes (Liu *et al.*, 2011):

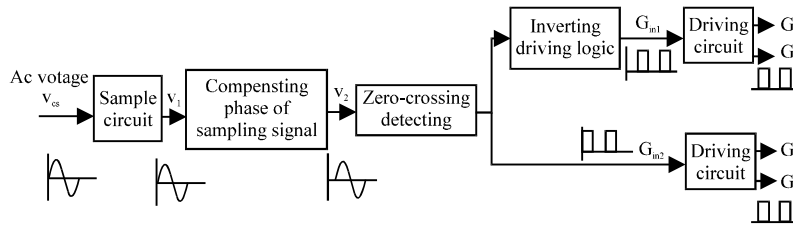


Fig. 5: ZVS control diagram of the full-bridge SR inverter

and G_2, G_3) must be complementary. So, invert G_{m2} and then G_{m1} is used as the input of driving circuit for switches (Q_1, Q_3).

EXPERIMENTAL STUDY

According to the Fig. 1 and operating principle of control circuit. The experimental circuit is built to validate the feasibility of control method proposed and the experimental parameters are shown in Table 1.

According to Eq. 18, the parameters shown in Table 1 are substituted into it. Therefore, the ZVS operation cycle (T_{ZVS}) of the full-bridge SR network can be obtained by solving M file in matlab. By solving Eq. 18, T_{ZVS} is equal to 13.21 μsec . It means that the frequency of the driving voltage (G_1, G_2, G_3 and G_4) is 75.7 kHz.

According to the result of T_{ZVS} , MOSFET IRFB4110 is selected as the component for SR and control circuit of the experiment for SR is well designed.

The experimental waveforms of the input voltage (v_{AB}) of the primary full-bridge converter and the flowing current (i_i) of inductor L_i are showed in Fig. 6. From Fig. 6, it can be seen that the polarity of voltage (v_{AB}) is changed when the current i_i is equal to zero. Hence, the conclusion that the two primary switching pairs (S_1, S_4 and S_2, S_3) works at zero current soft switching state can be clearly obtained.

Figure 7 shows the experimental waveforms of the waveforms of v_{cs}, G_1 and G_2 . From Fig. 7, it can be seen that the voltage v_{cs} is a sine wave. Meanwhile, when v_{cs} is greater than zero, switch Q_1 is turned on owing to G_1 driving but switch Q_2 is turned on owing to G_2 driving when v_{cs} is less than zero.

The experimental waveforms of $v_{cs}, v_{Q1}, v_{Q4}, G_1$ and G_4 are shown in Fig. 8. From Fig. 8, it can be seen that switches Q_1, Q_4 are simultaneously turned on or off because of the drive voltage G_1, G_4 , respectively. At same time, it also can be found that the switching states of Q_1 and Q_4 are changed when the drain to source voltage of Q_1 and Q_4 is equal to zero.

Figure 9 shows the experimental waveforms of the drive voltage G_2, G_3 , the AC voltage v_{cs} and the drain to

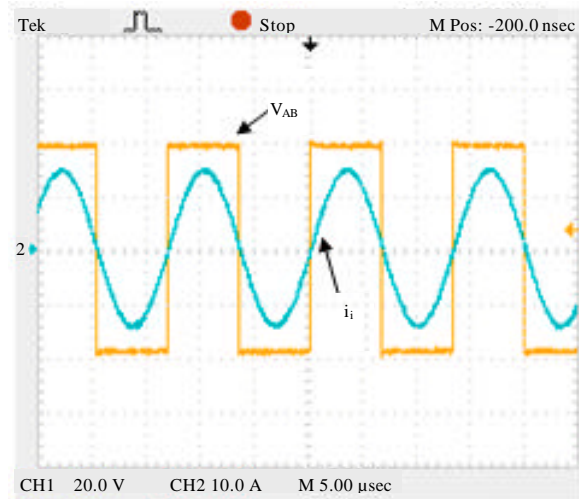


Fig. 6: Experimental waveforms of the current i_i and voltage v_{AB}

Table 1: Experimental parameters

Parameter	Values
Input dc voltage E_{dc} (V)	40.00
Primary resonant inductor L_1 (μH)	85.50
ESR of primary resonant inductor R_1 (Ω)	0.06
Primary resonant capacitor C_p (μF)	0.43
Primary resonant inductor L_p (μH)	159.00
ESR of primary resonant inductor R_p (Ω)	0.18
Mutual inductance M (μH)	61.90
Secondary resonant inductor L_s (μH)	111.20
ESR of secondary resonant inductor R_s (Ω)	0.12
Secondary resonant capacitor C_s (μF)	0.25
Filter inductor L_f (μH)	200.00
ESR of filter inductor R_f (Ω)	0.14
Filter capacitor C_o (μF)	100.00
Load R_L (Ω)	5.00

source voltage of Q_2, Q_3 . As it can be seen from Fig. 9, the drive voltage G_2, G_3 simultaneously drive switches Q_2, Q_3 which are turned on or off, respectively. Moreover, it can be found that the switching states of Q_2 and Q_3 are changed when the drain to source voltage of Q_2 and Q_3 is equal to zero.

Analyzing the Fig. 7-9, it can be seen that when v_{cs} is in the positive half cycle, switches Q_1, Q_4 are turned on and switches Q_2, Q_3 are turned off. When v_{cs} is in the

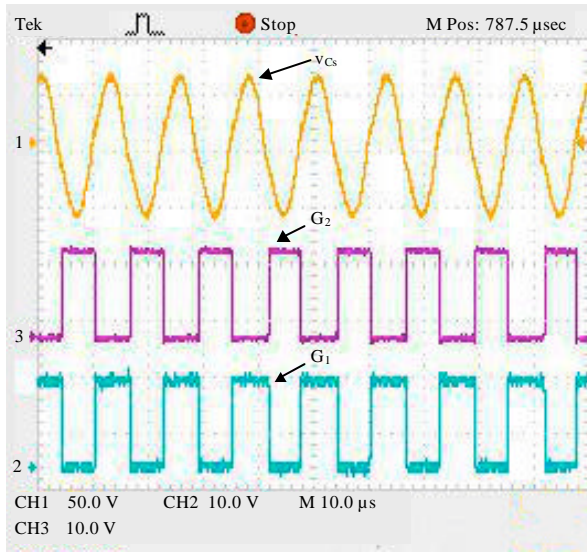


Fig. 7: Experimental waveforms of v_{Cs} , G_1 and G_2

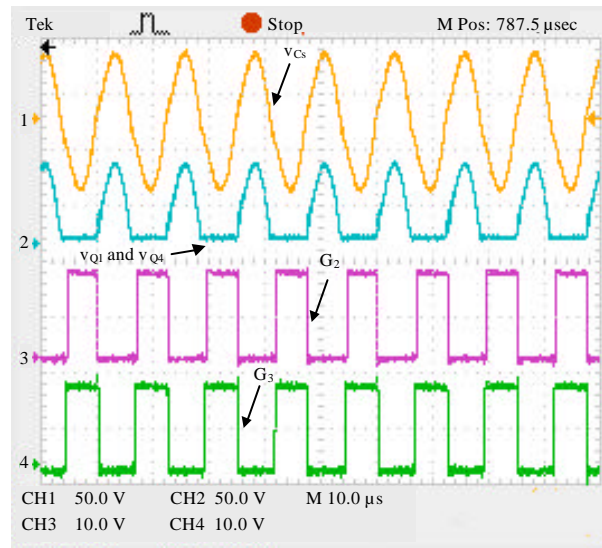


Fig. 9: Experimental waveforms of v_{Cs} , v_{Q2} , v_{Q3} , G_2 and G_3

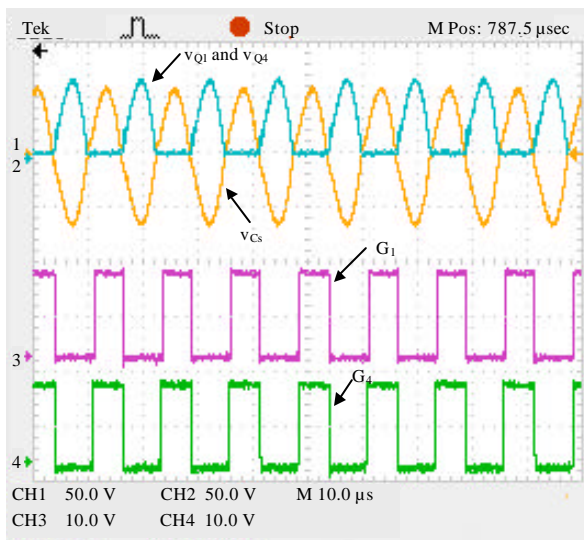


Fig. 8: Experimental waveforms of v_{Cs} , v_{Q1} , v_{Q4} , G_1 and G_4

negative half cycle, switches Q_2 , Q_3 are turned on and switches Q_1 , Q_4 are turned off. This means that the AC voltage v_{Cs} has been synchronously rectified. Moreover, all of the drain to source voltage of four switches Q_1 , Q_2 , Q_3 and Q_4 are equal to zero when switching states of four switches are changed. This means that the secondary full-bridge SR network works in zero voltage soft switching state.

Therefore, the experimental results show that zero current soft switching state of the primary full-bridge and

zero voltage soft switching state of the secondary full-bridge SR network have been achieved in the IPT resonant converter.

CONCLUSION

In this study, due to resonance characteristics of the resonant converter based on IPT, a novel control method has been proposed to achieve ZVS SR state operation for the AC-DC network of the resonant converter. A steady state mathematical model has been established to determine the ZVS operating point of SR network which is based on the analysis about ZVS operation principle of SR and stroboscopic mapping method. The control circuit working operation has also been presented to guide the design of corresponding hardware circuit. Finally, the method proposed in this study has been verified by experimental results.

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